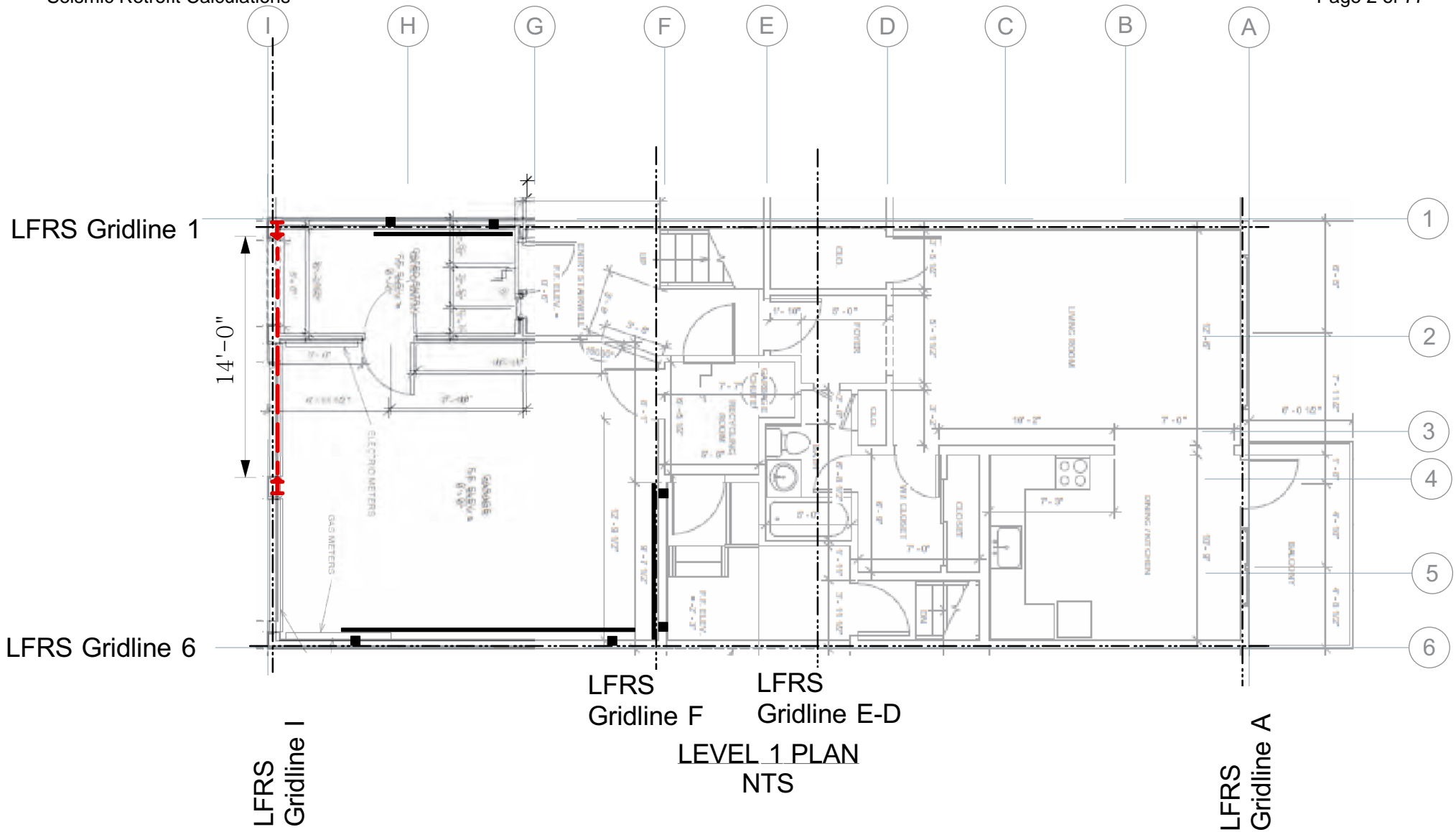


# AISC Special Moment Resisting Frame

## Analysis and Design

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Lateral Force Resisting System (LFRS) Elements :

- (N) Shear Wall
- AISC Welded Fixed Base Frame

SAP2000 ANALYSIS MODEL :  
SINGLE BAY SINGLE STORY  
SMRF FRAME 1 - GRIDLINE I - FIXED COLUMN

SMRF Centerline Dimensions:

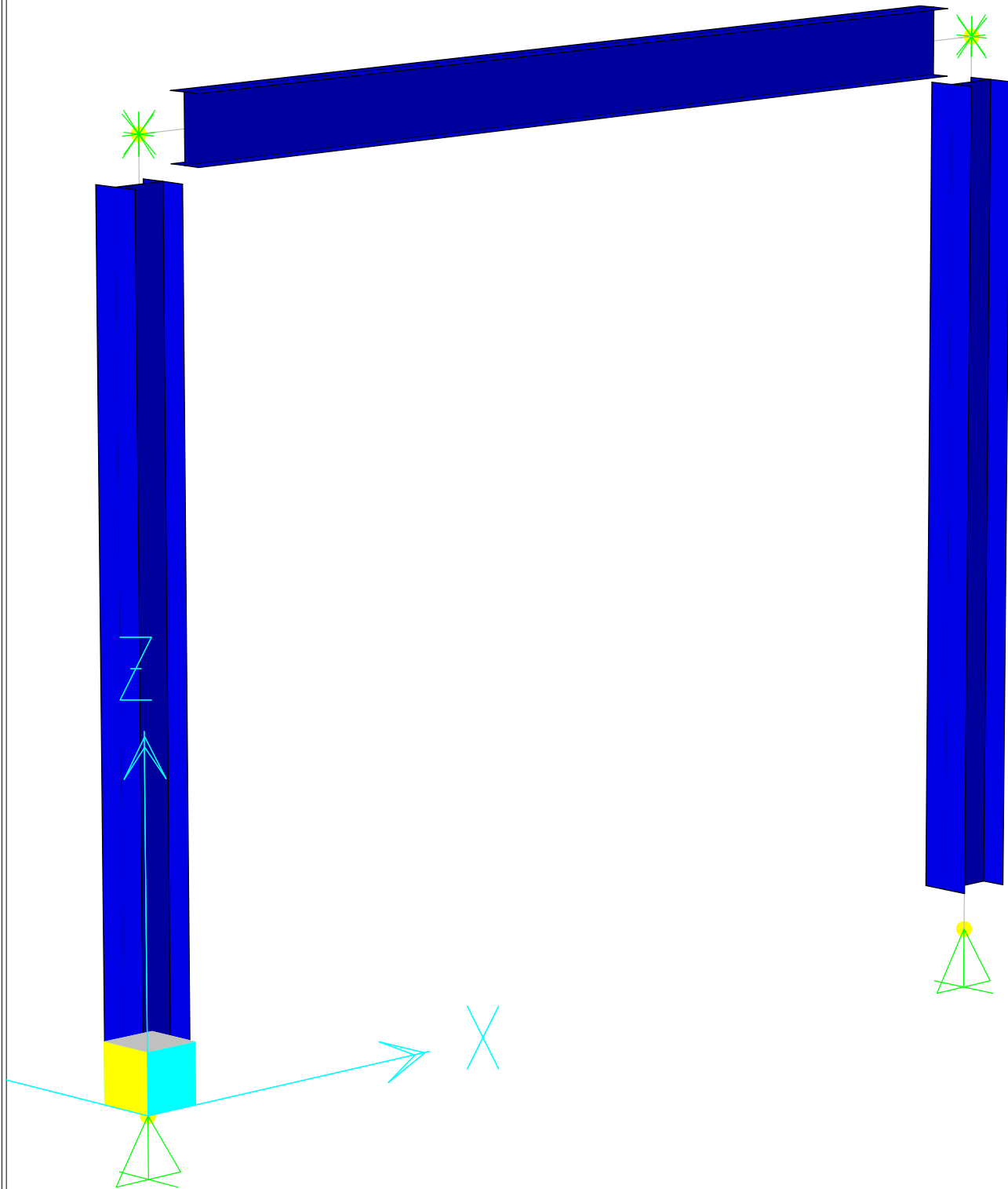
Height = 11.83'

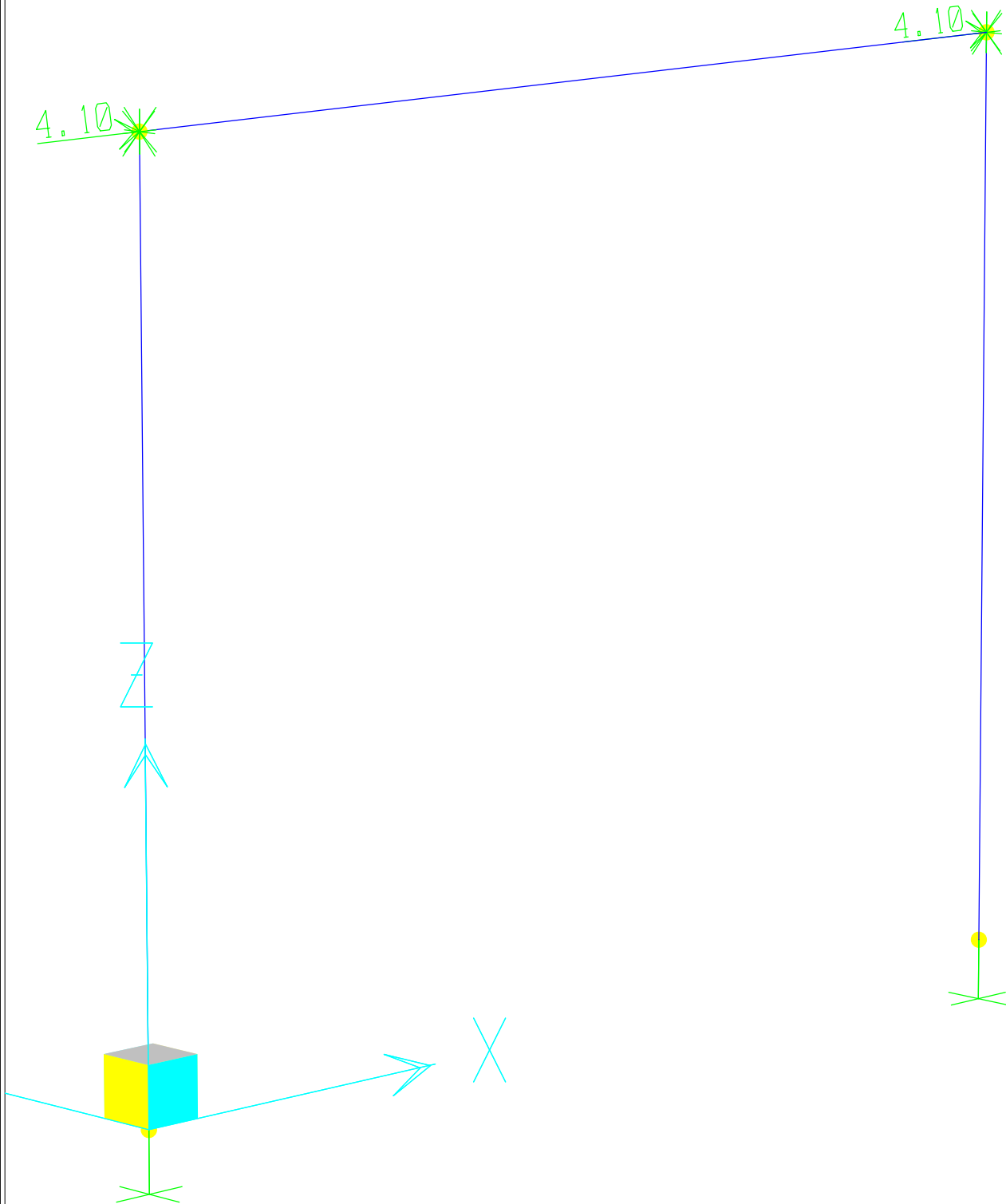
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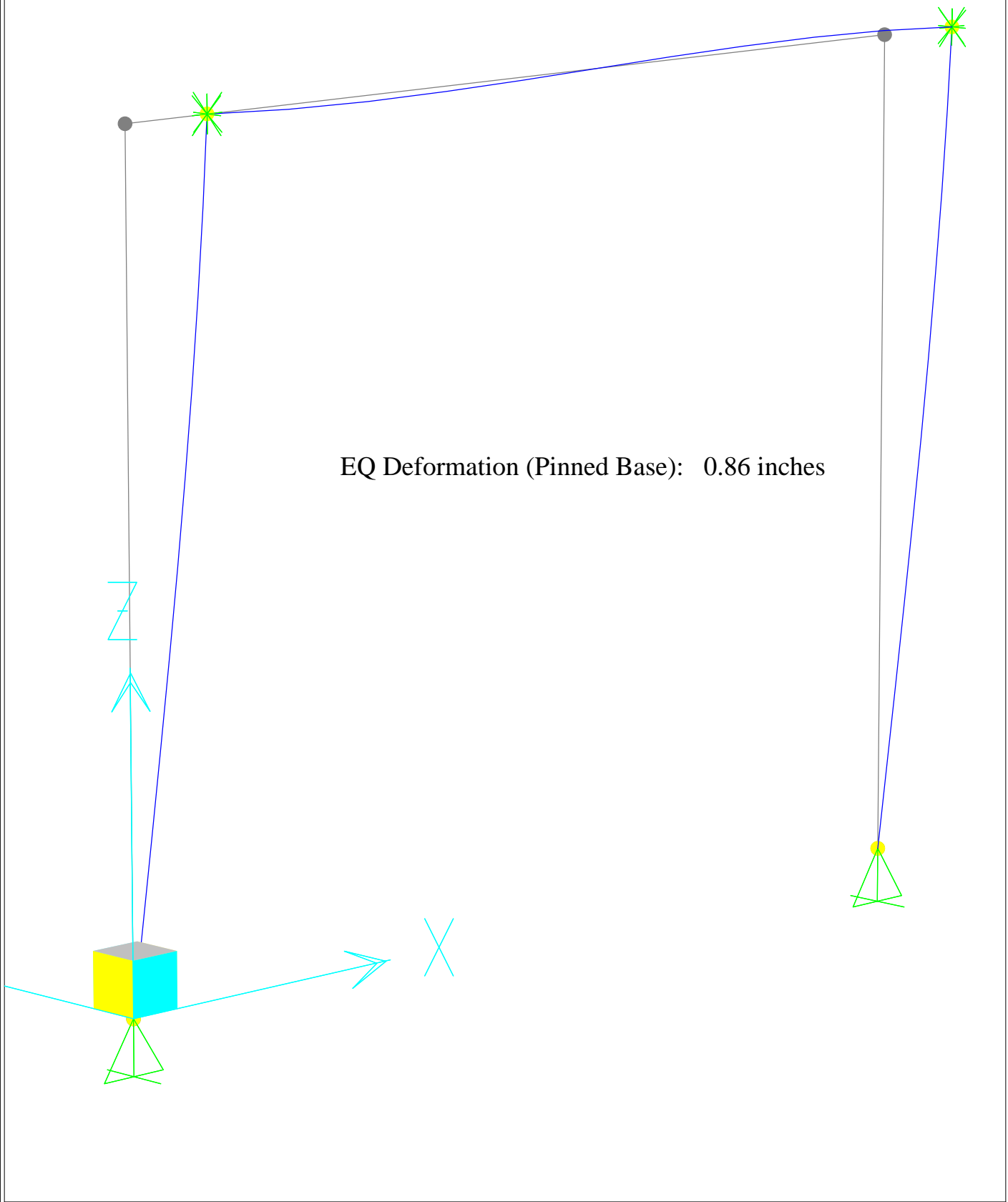
SMRF Members:

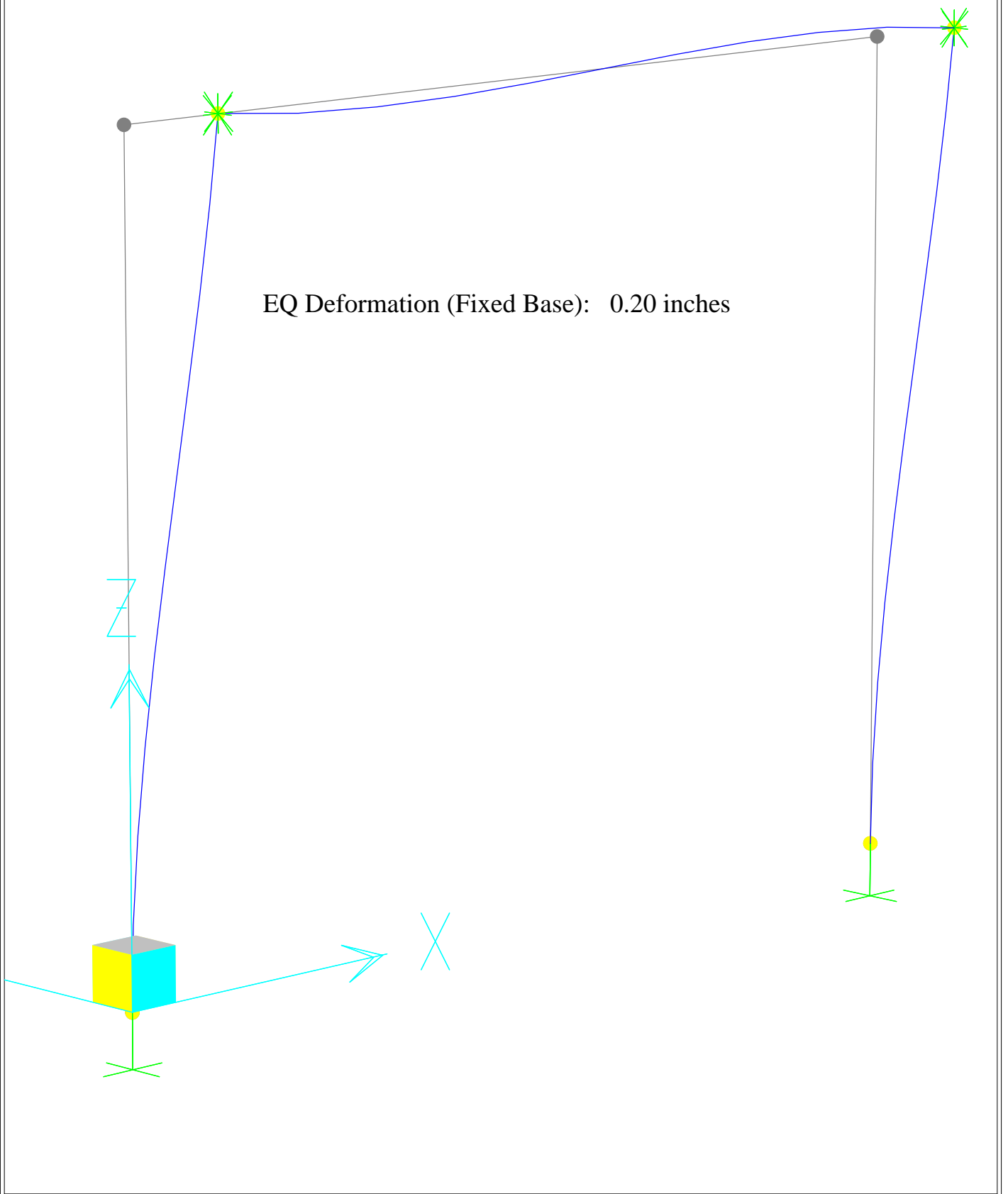
Columns = W8x67

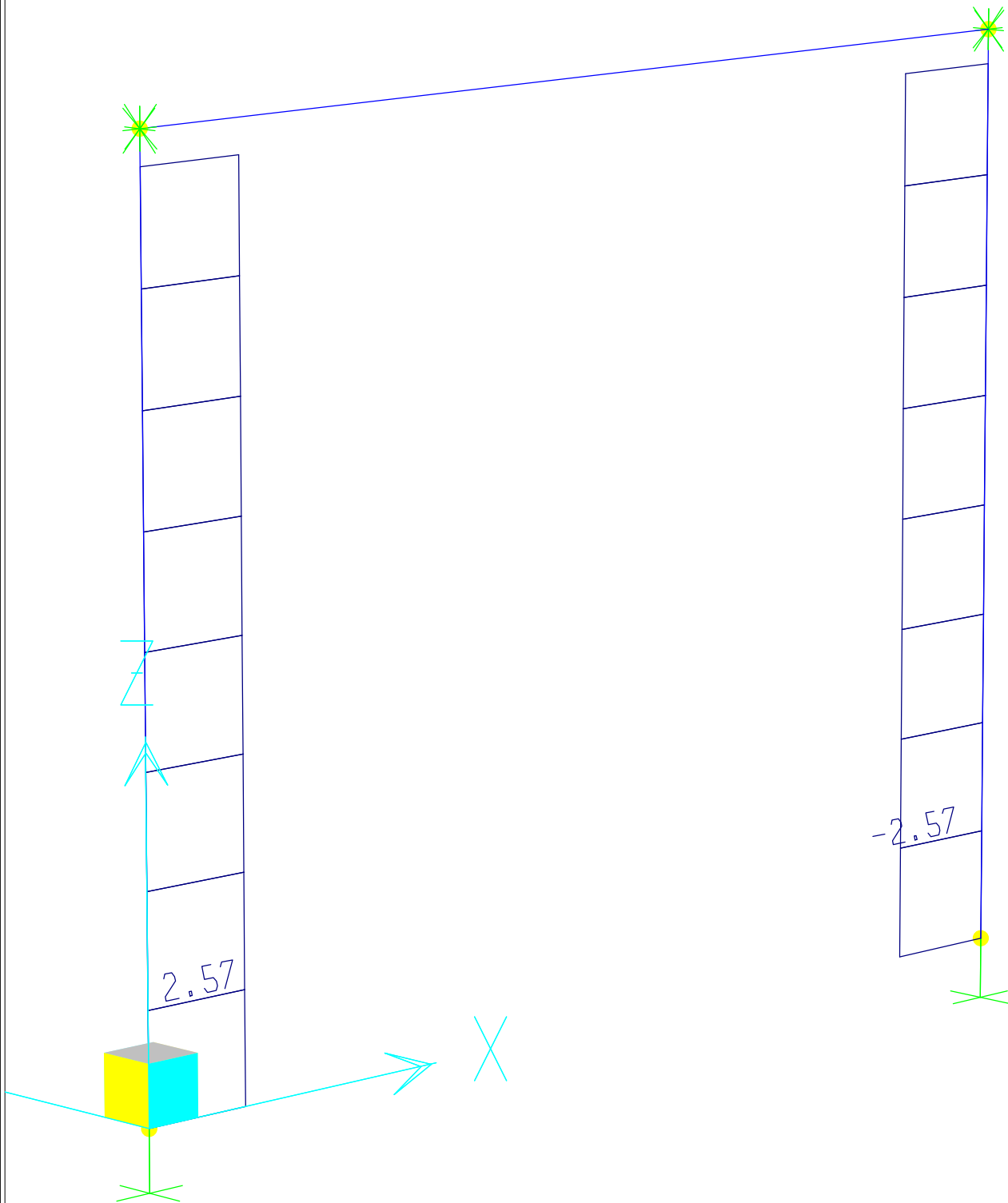
Beams = W10x30



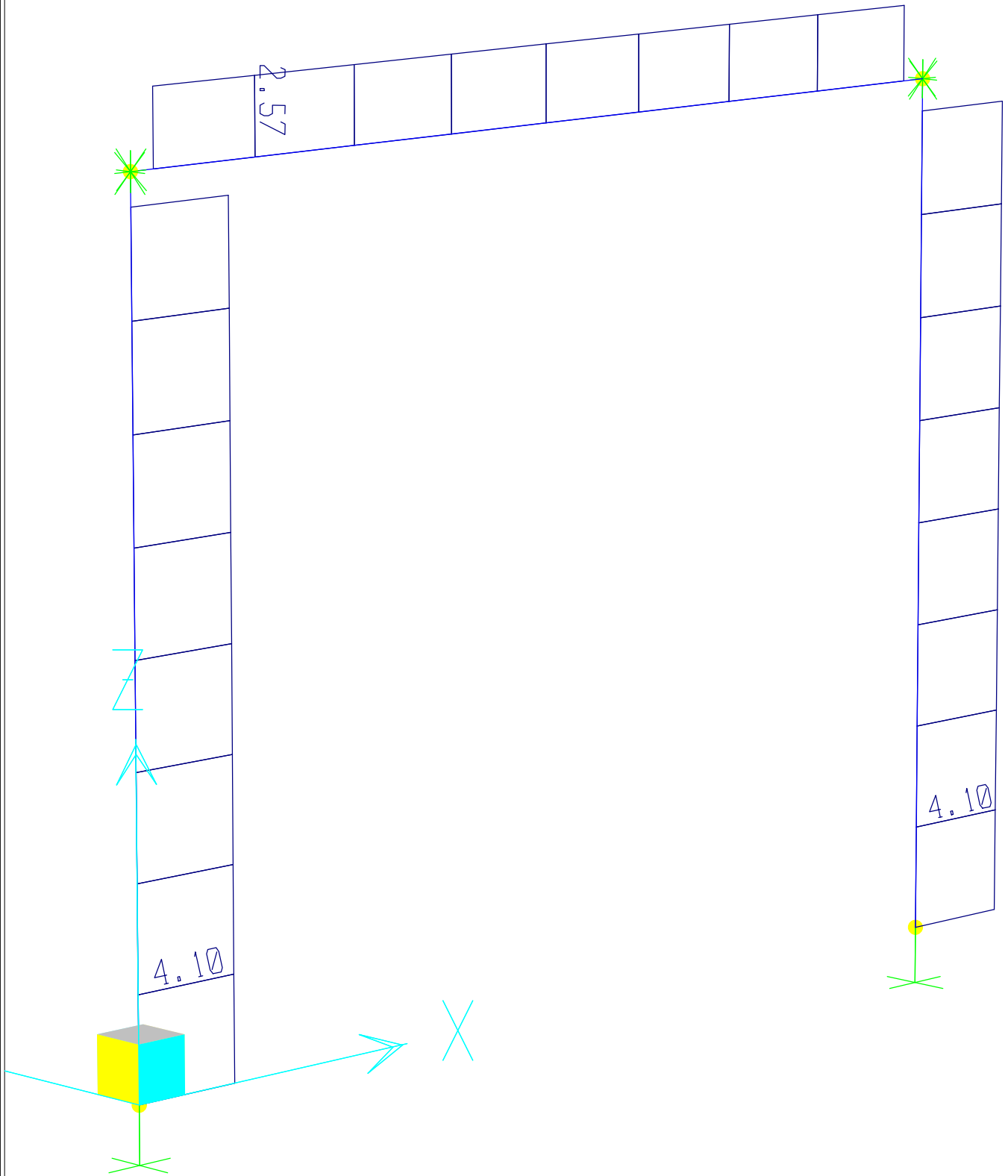


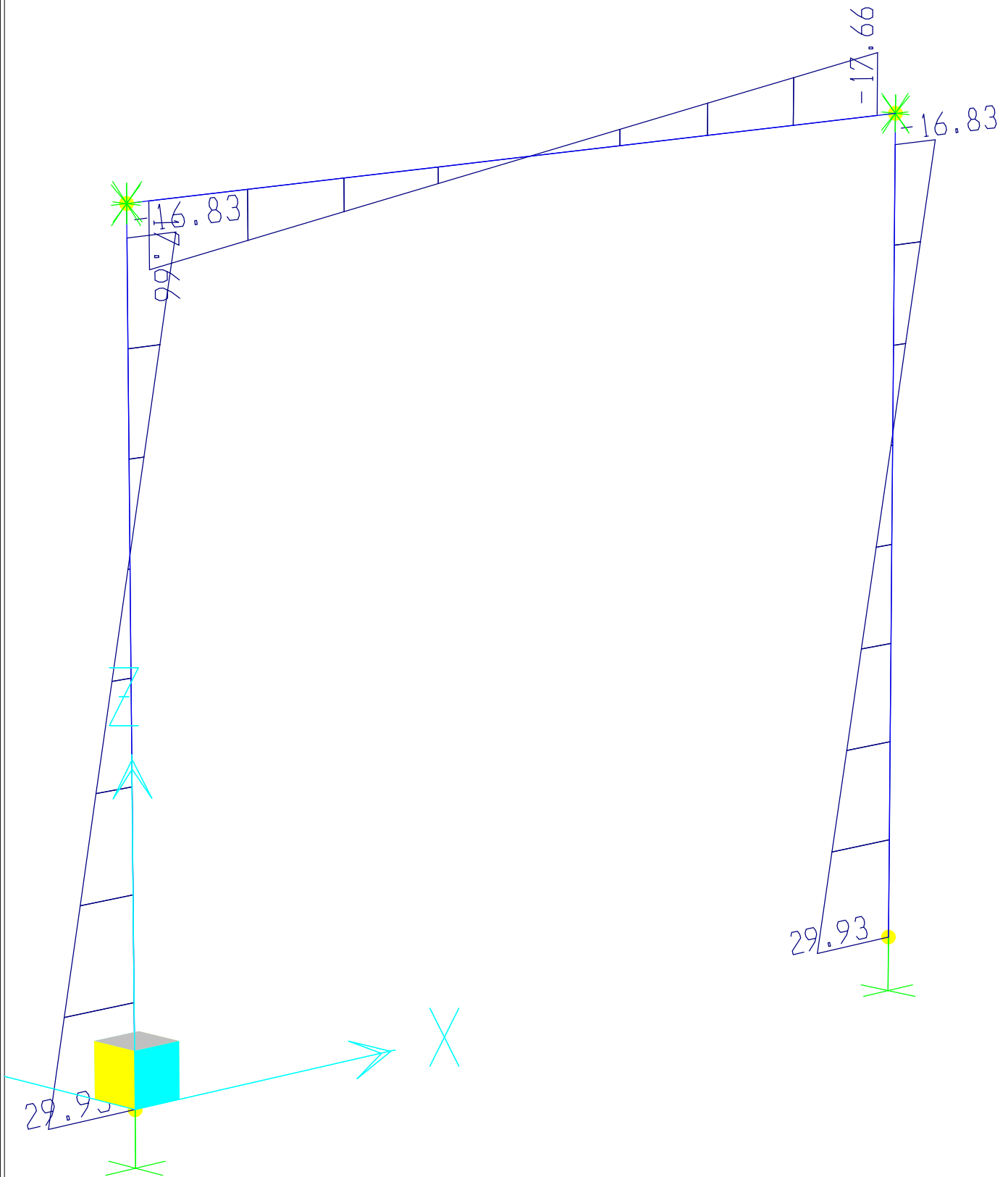


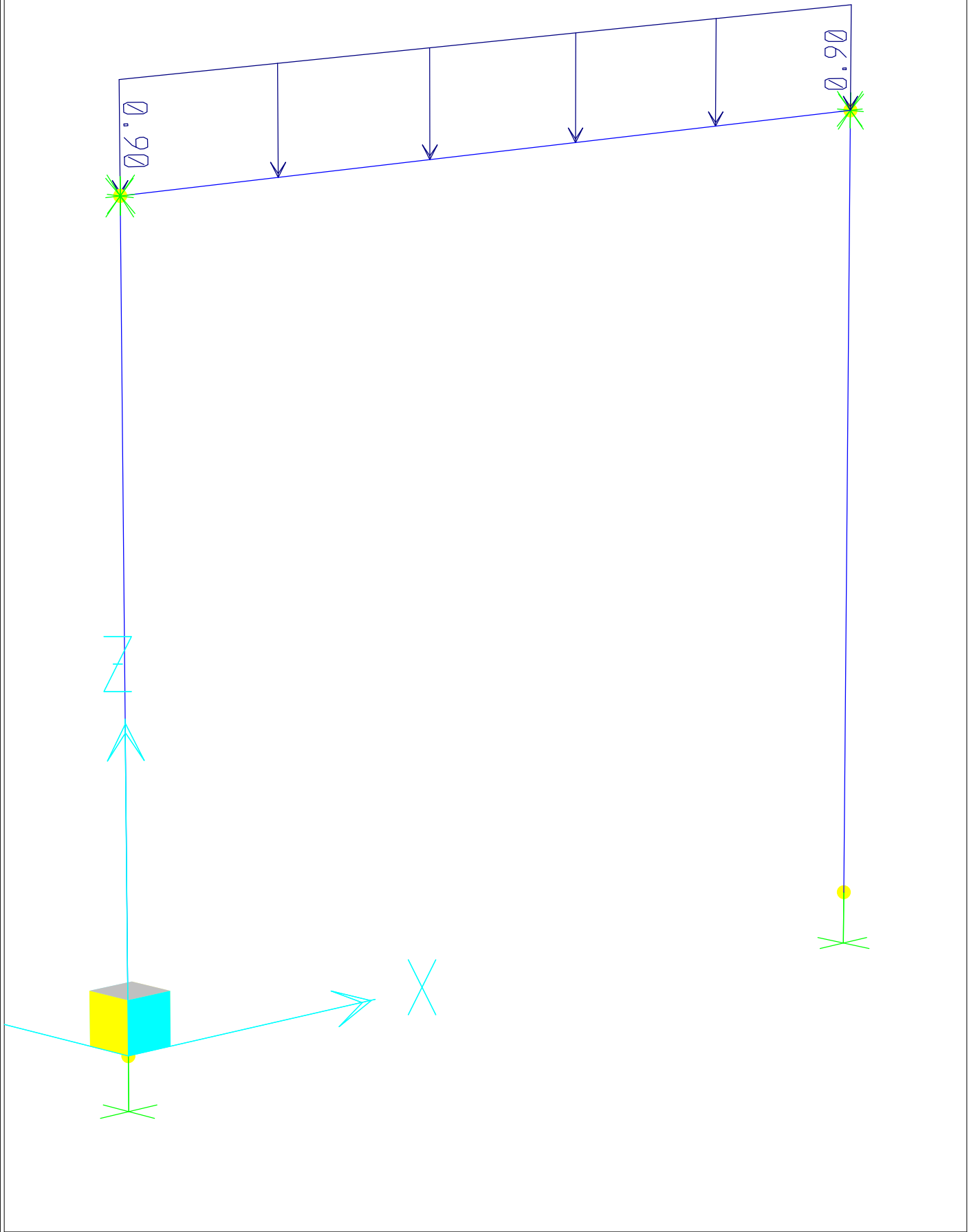


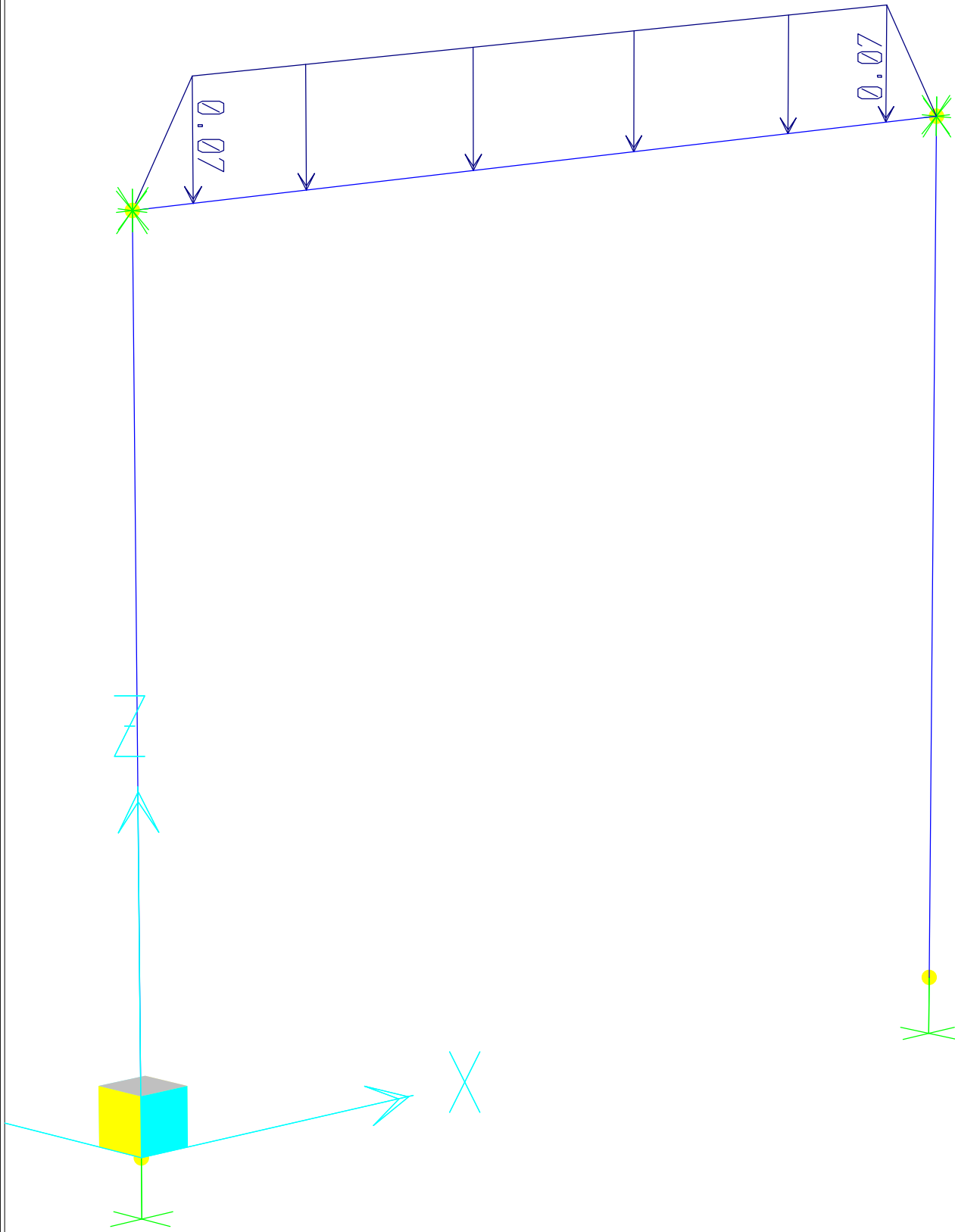


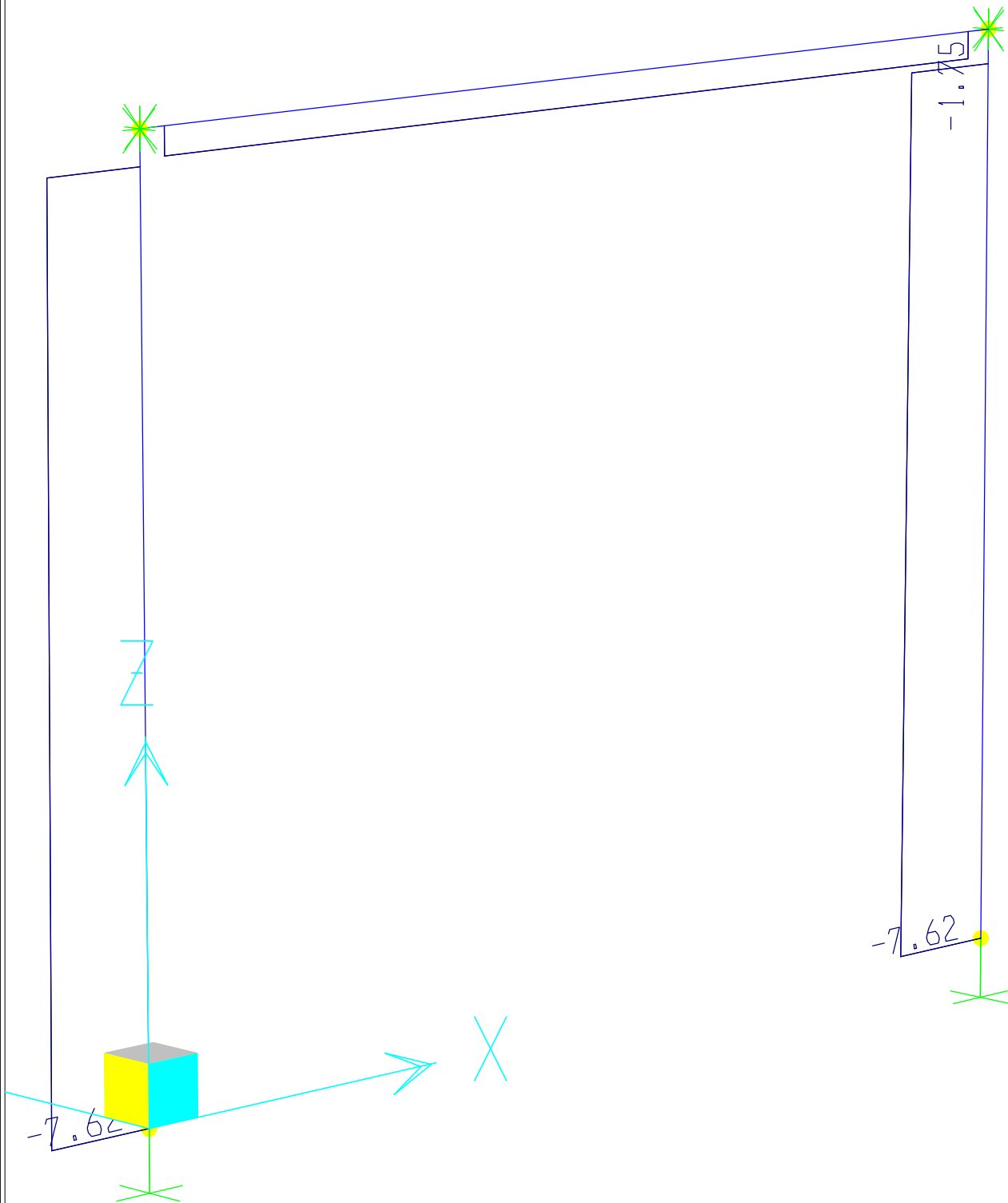


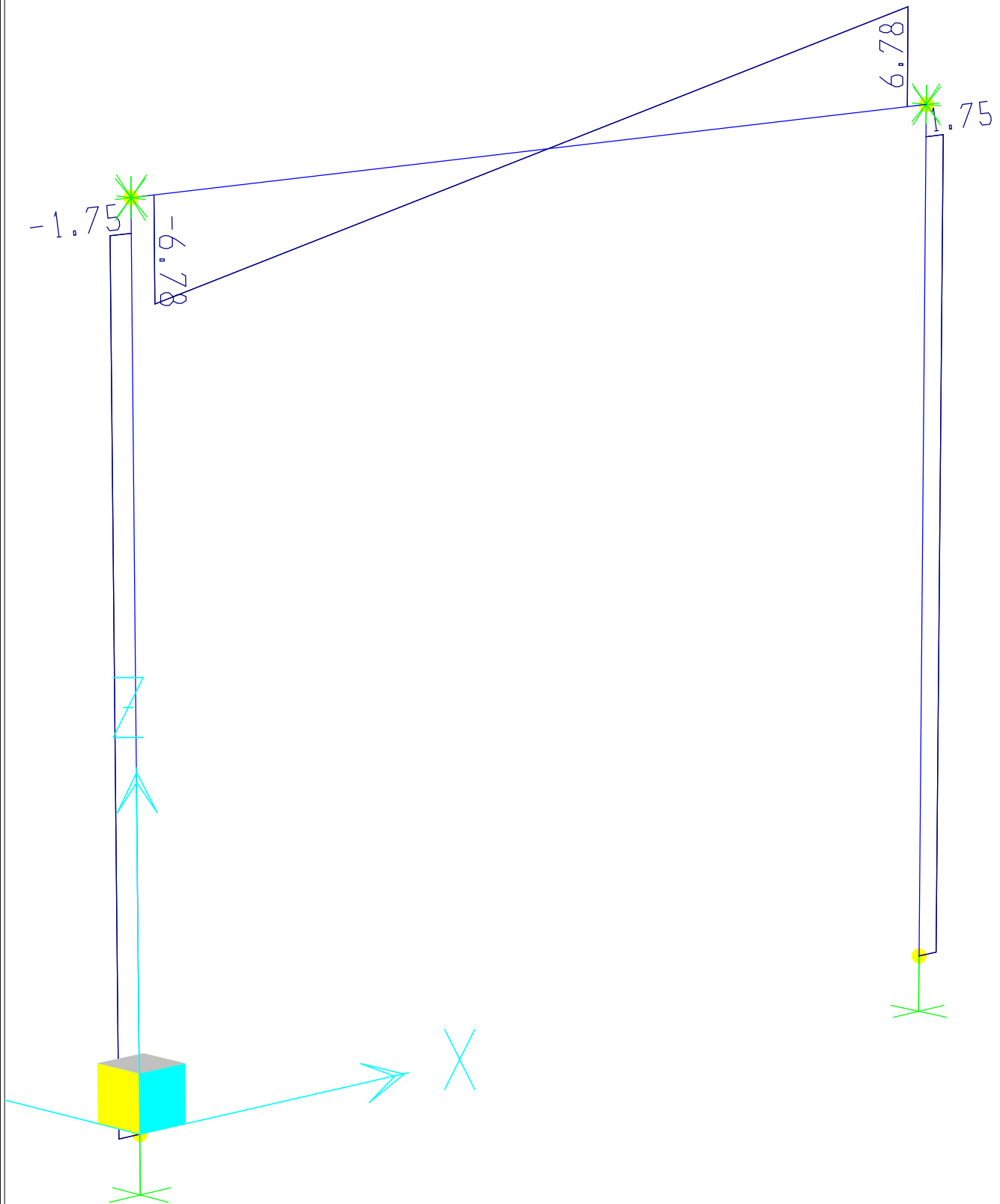


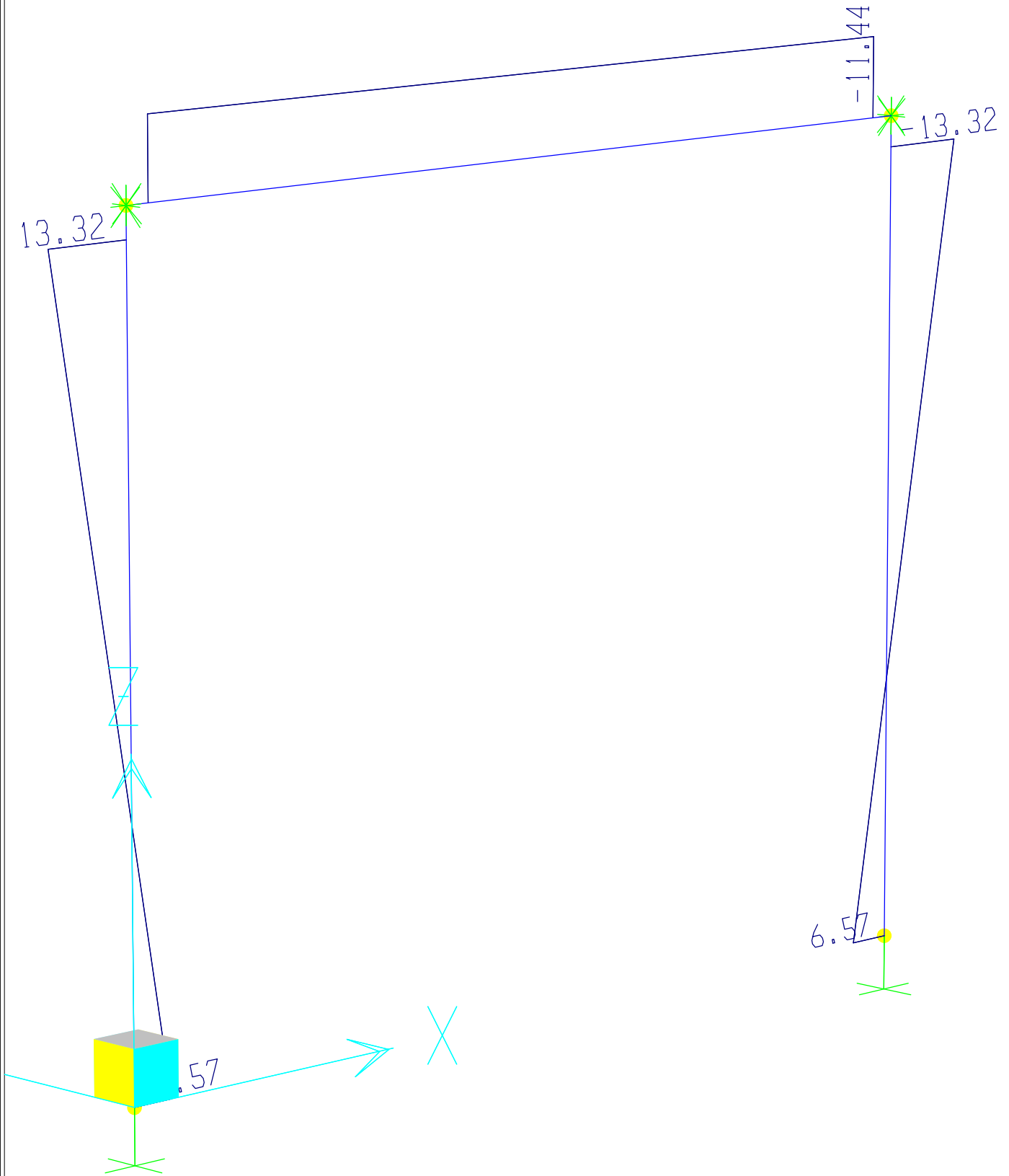


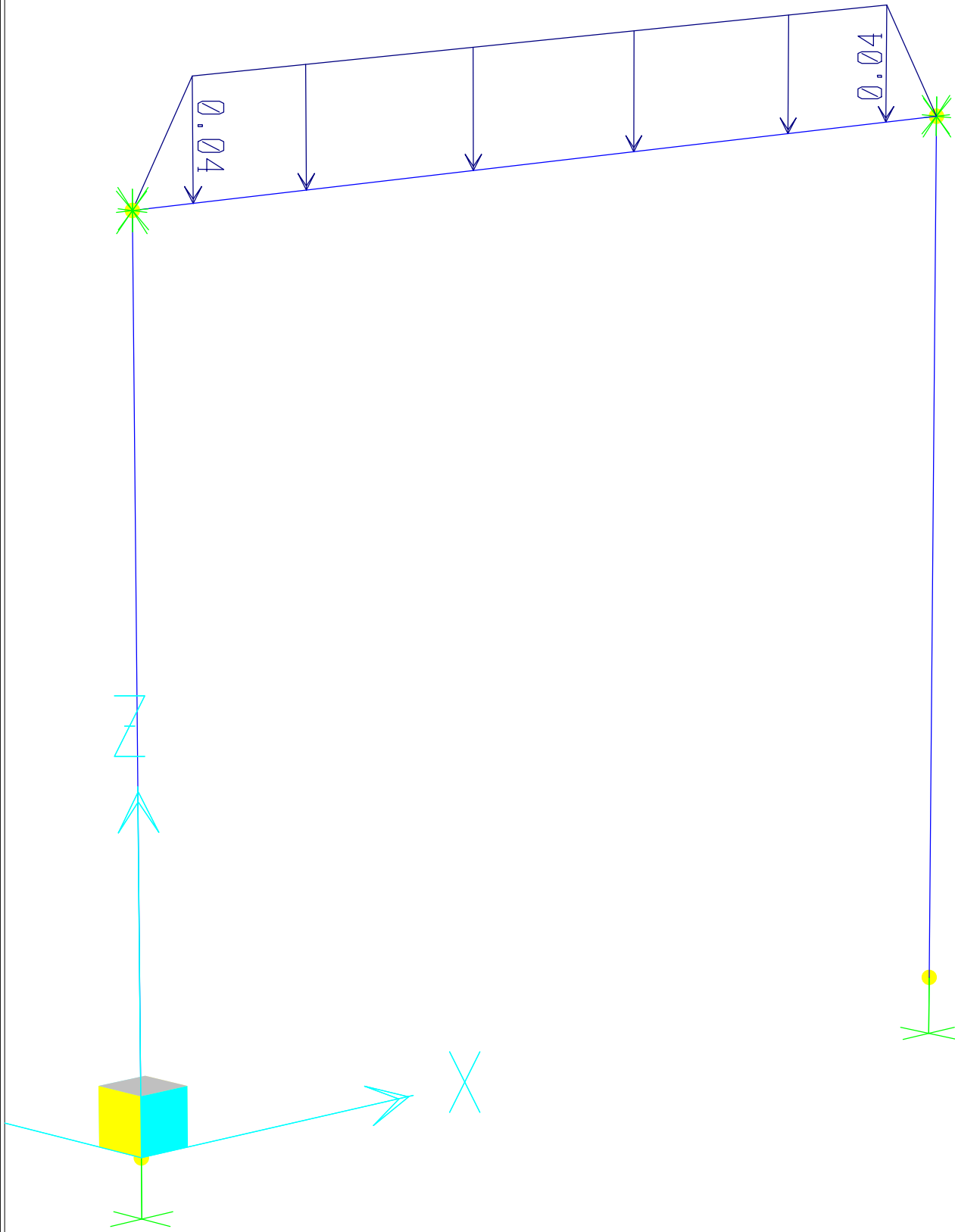




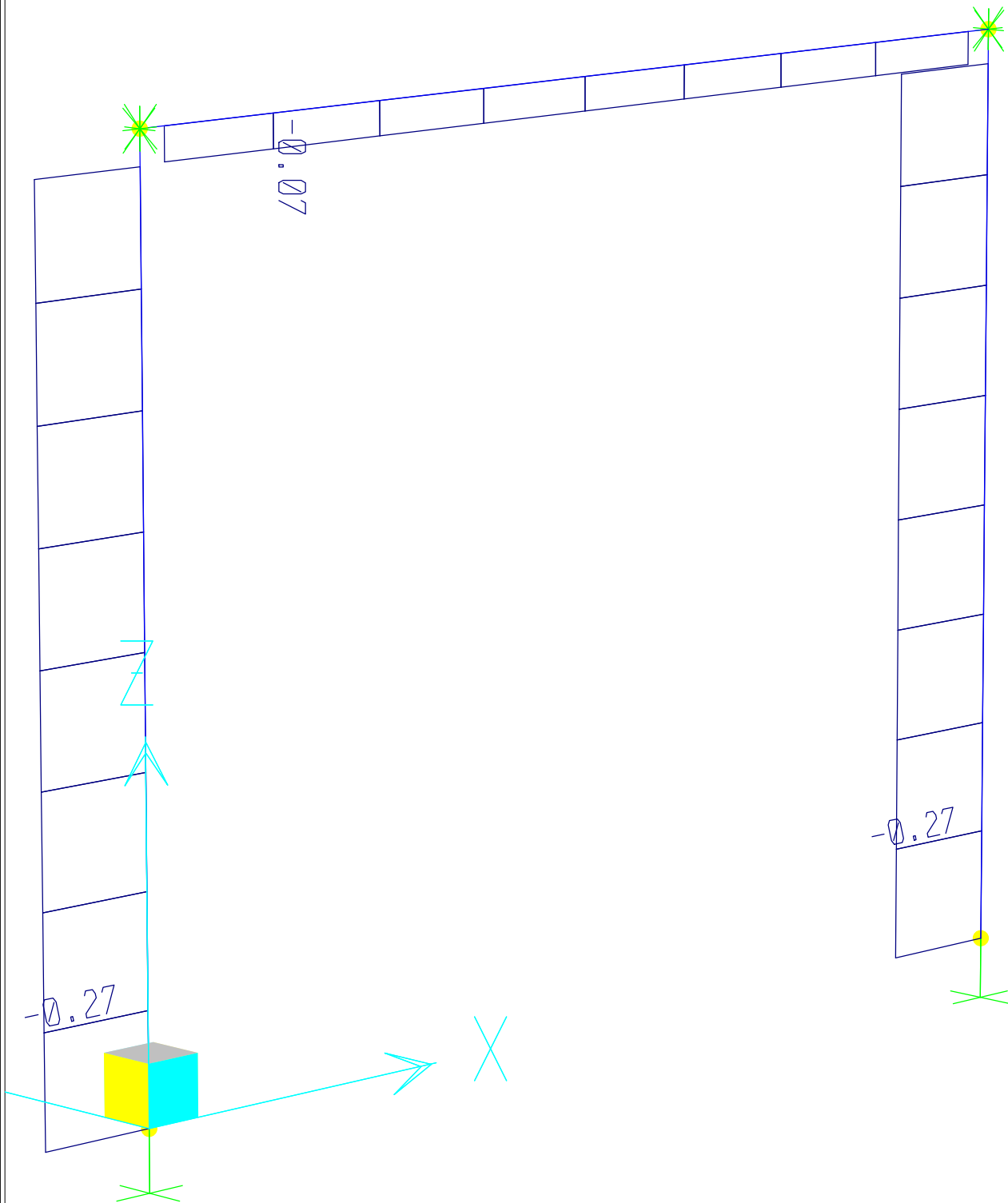


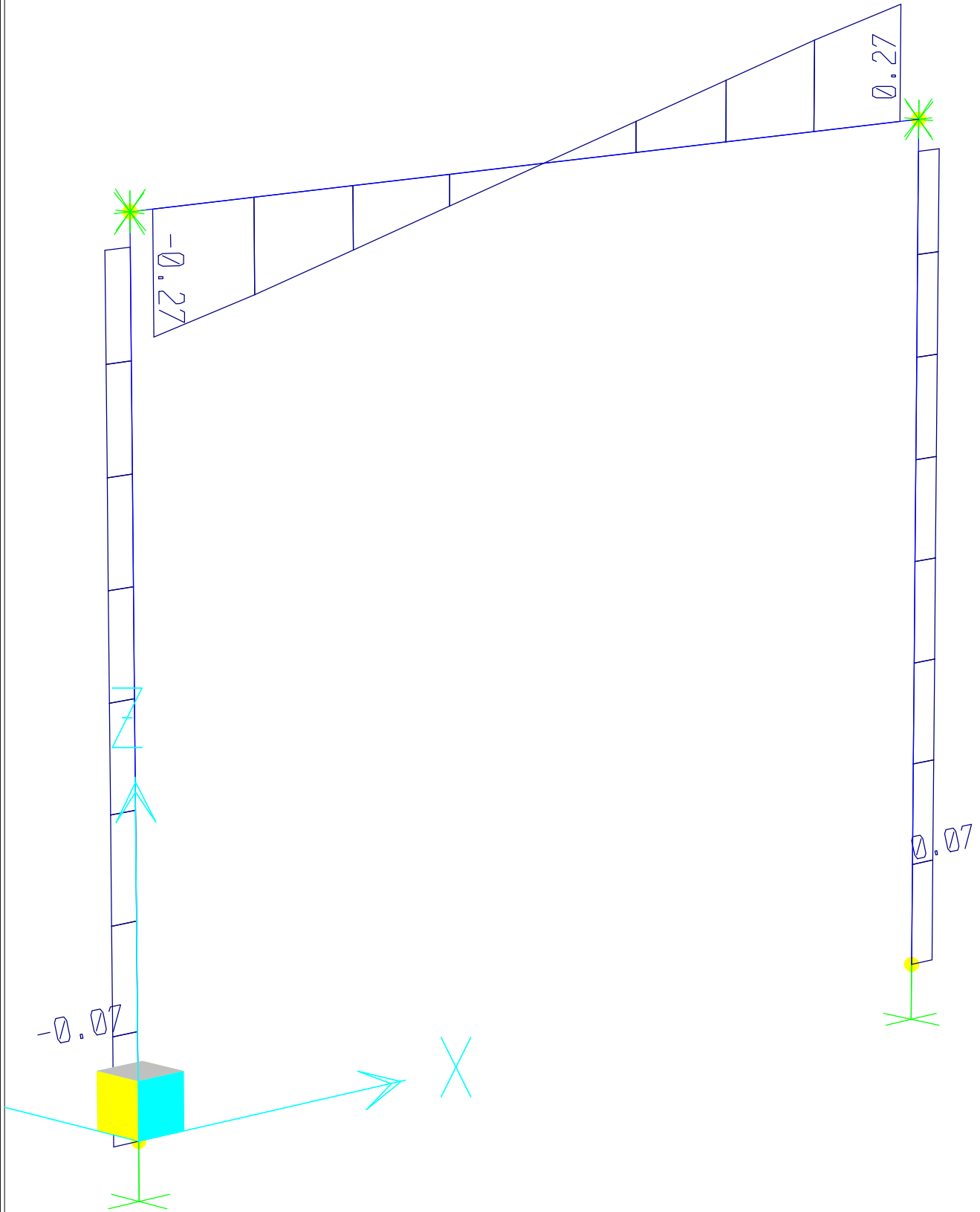


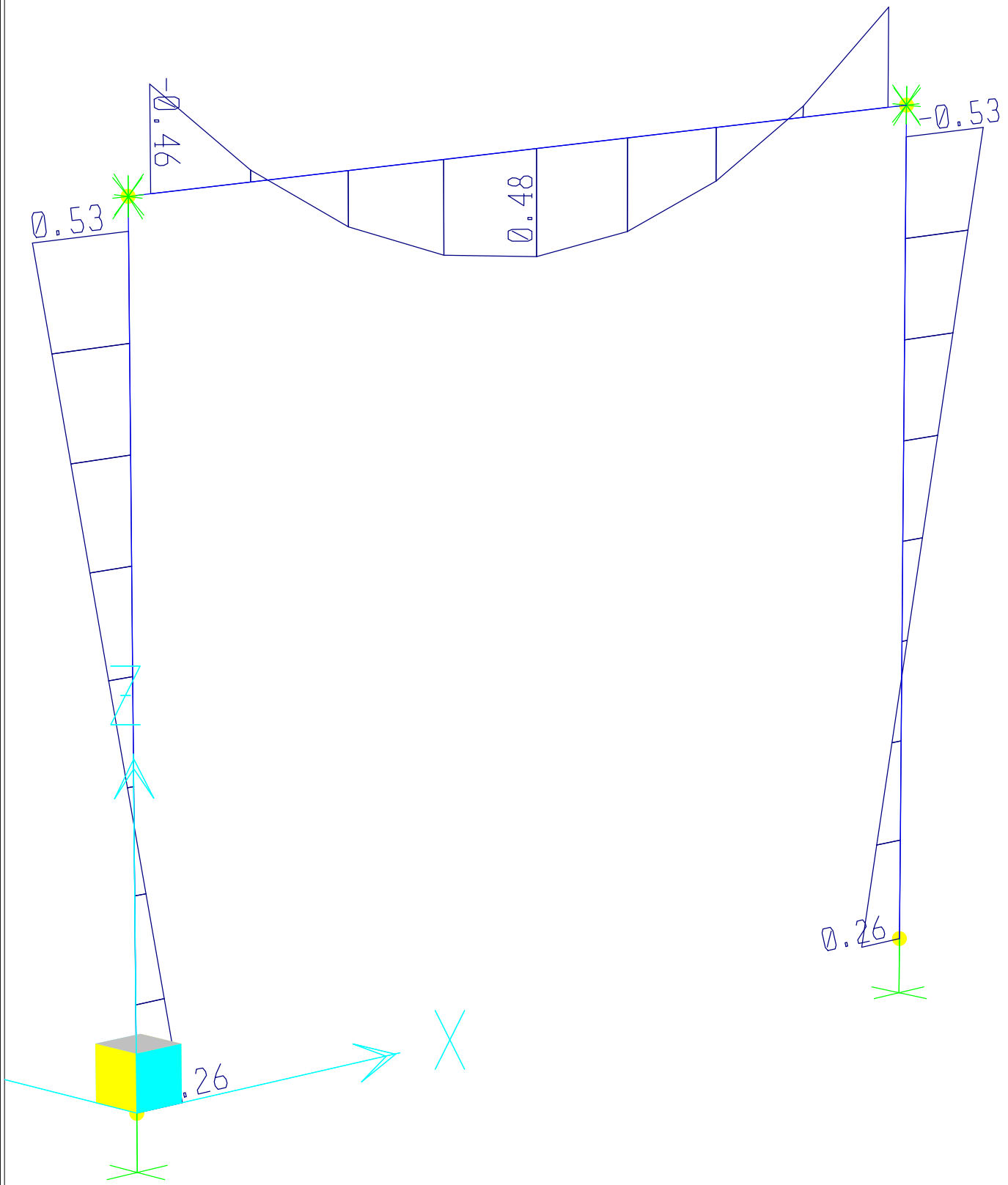












**AISC SMRF DESIGN -  
DRIFT AND STABILITY CHECK**

**SPECIAL MOMENT FRAME DESIGN - STORY DRIFT AND STABILITY CHECK**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - PINNED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S  
 Floor Level : 1  
 N<sub>S</sub> : 3 (Total Number of Stories)

**1. Special Moment Frame Data**

LRFS is comprised solely of MF's per ASCE 7-10 12.12.1.1 ? : N (Y/N)  
 New Structure ? : N (Y/N) (Non-structural components designed to accommodate EQ drift?)

Building and floor data

L = 57.00 feet (Building Length)  
 W = 25.00 feet (Building Width)  
 H<sub>a</sub> = 10.00 feet (Height of floor above)  
 H<sub>b</sub> = 12.00 feet (Height of floor below)

Results from Elastic Analysis :

Δ<sub>xe</sub> = 0.859 inches (Deformation for Level Above at Center of Mass, from elastic analysis)  
 Δ<sub>xe-1</sub> = 0.859 inches ( " for Level Below " )  
 V<sub>x</sub> = 8 Kips (Story Shear)

Seismic Deformation at Floor being evaluated:

Note: Reduced-Beam-Section connections are used at frame beam-to-column connections; per AISC 358-10 Section 5.8 Step 1, "...effective elastic drifts may be calculated by multiplying elastic drifts based on gross beam sections by 1.1 for flange reductions up to 50% of beam flange width".

Δ<sub>xe RBS</sub> = (1.0 + A<sub>RBS</sub>) Δ<sub>xe</sub> for 2c <= b<sub>f</sub> / 2 Where c = 1.00 inches (from RBS Beam Design)

Note: 2c = 2.00 inches b<sub>f</sub> = 5.81 inches (from moment Frame Beam selection below)  
 b<sub>f</sub> / 2 = 2.91 inches  
**OK**

A<sub>RBS</sub> = % Amplification in Elastic Drift due to RBS

= 4 c / b<sub>f</sub> x 10 Where c = 1.00 inches (from RBS Beam Design)  
 b<sub>f</sub> = 5.81 inches (from moment Frame Beam selection below)

= (1 + 0.069) x 0.859

A<sub>RBS</sub> = 6.88 % Amplification

Δ<sub>xe</sub> = 0.859 inches (Deformation at Level x at Center of Mass, from elastic analysis)

Δ<sub>xe RBS</sub> = 0.918 inches (Deformation at Level Above at Center of Mass - RBS)

Moment Frame Beams

N = 1 (Number of Identical Frames)

Section: W10x30  
 n : 1 (number of beams/frame)

A	8.84		in <sup>2</sup>
d	10.50		in
t <sub>w</sub>	0.30		in
b <sub>f</sub>	5.81		in
t <sub>f</sub>	0.51		in
r <sub>y</sub>	1.37		in
K	0.81		in
K <sub>1</sub>	0.69		in
T	8.88		in
Z <sub>x</sub>	37		in <sup>3</sup>

Seismic Parameters:

R = 8 Modification Response Coefficient (ASCE 7-10 Table 12.2-1)  
 C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Table 12.2-1)  
 ρ = 1.3 Redundancy Factor (ASCE 7-10 Section 12.3.4)

Occupancy Category: I (ASCE 7-10 Table 1-5-1: Residential Multi-unit Dwelling)  
 I = 1.0 Importance Factor, Table 11.5-2

SDC = E Seismic Design Category (ASCE 7-10 Section 11.4)  
 S<sub>DS</sub> = 1.09 g's (Site Design Coefficient - Short Period)

Gravity Loads - Unfactored

	Floor	Roof	
D	30.0	20.0	psf
L	40.0	20.0	psf

w<sub>w</sub> = 15 psf (Wall Load)

F<sub>y</sub> = 50 ksi

**SPECIAL MOMENT FRAME DESIGN - STORY DRIFT AND STABILITY CHECK**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - PINNED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S  
 Floor Level : 1  
 N<sub>S</sub> : 3 (Total Number of Stories)

**2. Check Story Drift**

**a) Allowable Story Drift (ASCE 7-10 Table 12.12-1)**

LRFS is comprised solely of MF's per ASCE 7-10 12.12.1.1 ? N (Y/N)

$$\Delta_a = h_{sx} (\Delta_g/h_{sx}) / \rho \quad (\text{SDC D-F for LRFS} = 100\% \text{ MF})$$

$$= h_{sx} (\Delta_g/h_{sx}) \quad (\text{All other SDC's})$$

Where  $h_{sx} = H_b = 12.00$  feet (Story height below level x)  
 SDC = E Seismic Design Category (ASCE 7-10 Section 11.4)  
 $\rho = 1.3$  Redundancy Factor (ASCE 7-10 Section 12.3.4)

$$\Delta_g/h_{sx} = 0.020 \quad \text{for Floors total : } 3$$

$$\text{Occupancy Category} = \text{I} \quad (\text{ASCE 7-10 T})$$

$$\Rightarrow \Delta_a = \begin{matrix} 0.24 & \text{feet} \\ = & 2.88 & \text{inches} \end{matrix}$$

**TABLE 12.12-1 ALLOWABLE STORY DRIFT,  $\Delta_a^{a,b}$**

Structure	Occupancy Category		
	I or II	III	IV
Structures, other than masonry shear wall structures, 4 stories or less with interior walls, partitions, ceilings and exterior wall systems that have been designed to accommodate the story drifts.	$0.025h_{sx}^c$	$0.020h_{sx}$	$0.015h_{sx}$
Masonry cantilever shear wall structures <sup>d</sup>	$0.010h_{sx}$	$0.010h_{sx}$	$0.010h_{sx}$
Other masonry shear wall structures	$0.007h_{sx}$	$0.007h_{sx}$	$0.007h_{sx}$
All other structures	$0.020h_{sx}$	$0.015h_{sx}$	$0.010h_{sx}$

<sup>a</sup> $h_{sx}$  is the story height below Level x.  
<sup>b</sup>For seismic force-resisting systems comprised solely of moment frames in Seismic Design Categories D, E, and F, the allowable story drift shall comply with the requirements of Section 12.12.1.1.  
<sup>c</sup>There shall be no drift limit for single-story structures with interior walls, partitions, ceilings, and exterior wall systems that have been designed to accommodate the story drifts. The structure separation requirement of Section 12.12.3 is not waived.  
<sup>d</sup>Structures in which the basic structural system consists of masonry shear walls designed as vertical elements cantilevered from their base or foundation support which are so constructed that moment transfer between shear walls (coupling) is negligible.

**b) Resulting Drift at Floor Level x (ASCE 7-10 12.8.6)**

$$\delta_x = \frac{C_d \delta_{xe}}{I} \quad (12.8-15) \Rightarrow \Delta_x = \frac{C_d \Delta_{xe}}{I}$$

Where  $C_d = 5.50$  Deflection Amplification Factor (ASCE Table 12.2-1)  
 $\delta_{xe} \Rightarrow \Delta_{x,RBS} = 0.918$  inches (Drift at Level Above at Center of Mass from elastic analysis)  
 $I = 1.0$  Importance Factor, Table 11.5-2

$$\Delta_x = 5.05 \text{ inches}$$

**NG, >  $\Delta_a$**

**NG, Drift is NOT acceptable!**

**3. Check Frame or Stability at Floor Level**

**a) Portion of Gravity loads at Columns beneath floor level**

**i) Roof and Floor Areas**

Where  $L = 57.00$  feet  
 $W = 25.00$  feet

$$A_{\text{floor}} = A_{\text{roof}} = L W$$

$$A_{\text{floor}} = A_{\text{roof}} = 1,425 \text{ ft}^2$$

**ii) Roof Loads**

$$D_r = D_r A_{\text{roof}} \quad \text{Where } D_r = 20.0 \text{ psf}$$

$$D_r = 29 \text{ kips}$$

$$L_r = L_r A_{\text{roof}} \quad \text{Where } L_r = 20.0 \text{ psf}$$

$$L_r = 29 \text{ kips}$$

$$A_{\text{roof}} = 1,425 \text{ ft}^2$$

$$A_{\text{roof}} = 1,425 \text{ ft}^2$$

**iii) Floor Loads**

$$D_f = D A_{\text{floor}} \quad \text{Where } D = 30.0 \text{ psf}$$

$$D_f = 43 \text{ kips}$$

$$L_f = L A_{\text{floor}} \quad \text{Where } L = 40.0 \text{ psf}$$

$$L_f = 57 \text{ kips}$$

$$A_{\text{floor}} = 1,425 \text{ ft}^2$$

$$A_{\text{floor}} = 1,425 \text{ ft}^2$$

**iv) Wall Loads**

$$W_w = w_w 2 (L + W) H$$

$$W_w = 27 \text{ kips}$$

Where  $w_w = 15$  psf (wall weight)  
 $L = 57.00$  feet  
 $W = 25.00$  feet  
 $H = (0.5 (H_a + H_b)) = 11$  feet and  $H_a = 10.00$  feet  
 $H_b = 12.00$  feet

**v) Story weight on columns**

$$P_D = D_r + N_{\text{floors}} (D_f + W_w)$$

$$P_D = 238 \text{ kips}$$

$$P_L = L_r + N_{\text{floors}} L_f$$

$$P_L = 200 \text{ kips}$$

Where  $D_r = 29$  kips (roof)  
 $N_{\text{floors}} = 3$   
 $D_f = 43$  kips (floor)  
 $W_w = 27$  kips (wall)  
 Where  $L_r = 29$  kips (roof)  
 $N_{\text{floors}} = 3$   
 $L_f = 57$  kips (floor)

**Note:** Per ASCE 7-10 Section 12.4.2.3 Note 1, 50% of live loads may be considered for Load Combination 5 for  $L_0 \leq 100$  psf

$$P_x = P_D + 0.5 P_L \quad \text{Where } P_D = 238 \text{ kips}$$

$$P_x = 338 \text{ kips} \quad \text{Where } P_L = 200 \text{ kips}$$

**SPECIAL MOMENT FRAME DESIGN - STORY DRIFT AND STABILITY CHECK**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - PINNED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S  
 Floor Level : 1  
 N<sub>S</sub> : 3 (Total Number of Stories)

**b) Check of P - Delta Effects (ASCE 7-10 Section 12.8.7)**

$$\theta = \text{Stability Coefficient per EQ 12.8-16}$$

$$= (P_x \Delta_{xe-1} I_b) / (V_x H_{sx} C_d) \leq 0.10$$

Where P<sub>x</sub> = 338 kips

$\Delta_{xe-1}$  = Seismic Design Story Drift of Level x-1 - RBS

$$= C_d (1.0 + A_{RBS}) \Delta x_{e-1} / I_b \quad (12.8-15) \quad \text{for } C_d = 5.50 \quad \text{Deflection Amplification Factor (ASCE 7-10 Ta)}$$

A<sub>RBS</sub> = 6.88 % Amplification

$$= 5.50 \times (1.069) \times 0.859 / 1.0$$

$\Delta_{xe-1}$  = 0.859 inches ( " for Level Below

I<sub>b</sub> = 1.0 Importance Factor, Table 11.5-2

$\Delta_{xe-1}$ = 5.05 inches
-------------------------------

I<sub>b</sub> = 1.0 Importance Factor, Table 11.5-2

V<sub>x</sub> = 8 kips (Story Shear)

H = 11.00 feet  
 = 132.00 inches

C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Table 12.2-1)

$\theta = 0.287$
------------------

NG

**c) Maximum Value for Stability Coefficient**

$$\theta_{MAX} = 0.5 / (\beta C_d) \leq 0.25 \quad (12.8-17)$$

Where  $\beta$  = Shear DCR for Level x

= 1.0 (Conservative assumption per 12.8.7)

C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Table 12.2-1)

$\theta_{MAX} = 0.091$
------------------------

OK

Note:  $\theta = 0.287$  radians

NG

<b>Floor Level is NOT Stable!</b>
-----------------------------------

**SPECIAL MOMENT FRAME DESIGN - STORY DRIFT AND STABILITY CHECK**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S  
 Floor Level : 1  
 N<sub>S</sub> : 3 (Total Number of Stories)

**1. Special Moment Frame Data**

LRFS is comprised solely of MF's per ASCE 7-10 12.12.1.1 ? : N (Y/N)  
 New Structure ? : N (Y/N) (Non-structural components designed to accommodate EQ drift?)

Building and floor data

L = 57.00 feet (Building Length)  
 W = 25.00 feet (Building Width)  
 H<sub>a</sub> = 10.00 feet (Height of floor above)  
 H<sub>b</sub> = 12.00 feet (Height of floor below)

Results from Elastic Analysis :

Δ<sub>xe</sub> = 0.196 inches (Deformation for Level Above at Center of Mass, from elastic analysis)  
 Δ<sub>xe-1</sub> = 0.196 inches ( " for Level Below " )  
 V<sub>x</sub> = 8 Kips (Story Shear)

Seismic Deformation at Floor being evaluated:

**Note:** Reduced-Beam-Section connections are used at frame beam-to-column connections; per AISC 358-10 Section 5.8 Step 1, "...effective elastic drifts may be calculated by multiplying elastic drifts based on gross beam sections by 1.1 for flange reductions up to 50% of beam flange width".

Δ<sub>xe RBS</sub> = (1.0 + A<sub>RBS</sub>) Δxe for 2c ≤ b<sub>f</sub> / 2 Where c = 1.00 inches (from RBS Beam Design)

Note: 2c = 2.00 inches b<sub>f</sub> = 5.81 inches (from moment Frame Beam selection below)  
 b<sub>f</sub> / 2 = 2.91 inches **OK**

A<sub>RBS</sub> = % Amplification in Elastic Drift due to RBS  
 = 4 c / b<sub>f</sub> x 10 Where c = 1.00 inches (from RBS Beam Design)  
 b<sub>f</sub> = 5.81 inches (from moment Frame Beam selection below)

= (1 + 0.069) x 0.196

A<sub>RBS</sub> = 6.88 % Amplification

Δ<sub>xe</sub> = 0.196 inches (Deformation at Level x at Center of Mass, from elastic analysis)

Δ<sub>xe RBS</sub> = 0.210 inches (Deformation at Level Above at Center of Mass - RBS)

Moment Frame Beams

N = 1 (Number of Identical Frames)

Section: W10x30  
 n : 1 (number of beams/frame)

A	8.84		in <sup>2</sup>
d	10.50		in
t <sub>w</sub>	0.30		in
b <sub>f</sub>	5.81		in
t <sub>f</sub>	0.51		in
r <sub>y</sub>	1.37		in
K	0.81		in
K <sub>1</sub>	0.69		in
T	8.88		in
Z <sub>x</sub>	37		in <sup>3</sup>

Seismic Parameters:

R = 8 Modification Response Coefficient (ASCE 7-10 Table 12.2-1)  
 C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Table 12.2-1)  
 ρ = 1.3 Redundancy Factor (ASCE 7-10 Section 12.3.4)

Occupancy Category: I (ASCE 7-10 Table 1-5-1: Residential Multi-unit Dwelling)  
 I = 1.0 Importance Factor, Table 11.5-2

SDC = E Seismic Design Category (ASCE 7-10 Section 11.4)  
 S<sub>DS</sub> = 1.09 g's (Site Design Coefficient - Short Period)

Gravity Loads - Unfactored

	Floor	Roof	
D	30.0	20.0	psf
L	40.0	20.0	psf

F<sub>y</sub> = 50 ksi

w<sub>w</sub> = 15 psf (Wall Load)



**SPECIAL MOMENT FRAME DESIGN - STORY DRIFT AND STABILITY CHECK**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S  
 Floor Level : 1  
 N<sub>S</sub> : 3 (Total Number of Stories)

**2. Check Story Drift**

**a) Allowable Story Drift (ASCE 7-10 Table 12.12-1)**

LRFS is comprised solely of MF's per ASCE 7-10 12.12.1.1 ? N (Y/N)

$$\Delta_a = h_{sx} (\Delta_g/h_{sx}) / \rho \quad (\text{SDC D-F for LRFS} = 100\% \text{ MF})$$

$$= h_{sx} (\Delta_g/h_{sx}) \quad (\text{All other SDC's})$$

Where  $h_{sx} = H_b = 12.00$  feet (Story height below level x)  
 SDC = E Seismic Design Category (ASCE 7-10 Section 11.4)  
 $\rho = 1.3$  Redundancy Factor (ASCE 7-10 Section 12.3.4)

$$\Delta_g/h_{sx} = 0.020 \quad \text{for Floors total : } 3$$

$$\text{Occupancy Category} = \text{I} \quad (\text{ASCE 7-10 T})$$

$$\Rightarrow \Delta_a = 0.24 \text{ feet}$$

$$= 2.88 \text{ inches}$$

**TABLE 12.12-1 ALLOWABLE STORY DRIFT,  $\Delta_a^{a,b}$**

Structure	Occupancy Category		
	I or II	III	IV
Structures, other than masonry shear wall structures, 4 stories or less with interior walls, partitions, ceilings and exterior wall systems that have been designed to accommodate the story drifts.	$0.025h_{sx}^c$	$0.020h_{sx}$	$0.015h_{sx}$
Masonry cantilever shear wall structures <sup>d</sup>	$0.010h_{sx}$	$0.010h_{sx}$	$0.010h_{sx}$
Other masonry shear wall structures	$0.007h_{sx}$	$0.007h_{sx}$	$0.007h_{sx}$
All other structures	$0.020h_{sx}$	$0.015h_{sx}$	$0.010h_{sx}$

<sup>a</sup> $h_{sx}$  is the story height below Level x.  
<sup>b</sup>For seismic force-resisting systems comprised solely of moment frames in Seismic Design Categories D, E, and F, the allowable story drift shall comply with the requirements of Section 12.12.1.1.  
<sup>c</sup>There shall be no drift limit for single-story structures with interior walls, partitions, ceilings, and exterior wall systems that have been designed to accommodate the story drifts. The structure separation requirement of Section 12.12.3 is not waived.  
<sup>d</sup>Structures in which the basic structural system consists of masonry shear walls designed as vertical elements cantilevered from their base or foundation support which are so constructed that moment transfer between shear walls (coupling) is negligible.

**b) Resulting Drift at Floor Level x (ASCE 7-10 12.8.6)**

$$\delta_x = \frac{C_d \delta_{xe}}{I} \quad (12.8-15) \Rightarrow \Delta_x = \frac{C_d \Delta_{xe}}{I}$$

Where  $C_d = 5.50$  Deflection Amplification Factor (ASCE Table 12.2-1)  
 $\delta_{xe} \Rightarrow \Delta_{x,RBS} = 0.210$  inches (Drift at Level Above at Center of Mass from elastic analysis)  
 $I = 1.0$  Importance Factor, Table 11.5-2

$$\Delta_x = 1.15 \text{ inches}$$

OK, <  $\Delta_a$

Resulting Drift is acceptable

**3. Check Frame or Stability at Floor Level**

**a) Portion of Gravity loads at Columns beneath floor level**

**i) Roof and Floor Areas**

$$A_{\text{floor}} = A_{\text{roof}} = L W$$

Where  $L = 57.00$  feet  
 $W = 25.00$  feet

$$A_{\text{floor}} = A_{\text{roof}} = 1,425 \text{ ft}^2$$

**ii) Roof Loads**

$$D_r = D_r A_{\text{roof}}$$

Where  $D_r = 20.0$  psf  
 $A_{\text{roof}} = 1,425$  ft<sup>2</sup>

$$D_r = 29 \text{ kips}$$

$$L_r = L_r A_{\text{roof}}$$

Where  $L_r = 20.0$  psf  
 $A_{\text{roof}} = 1,425$  ft<sup>2</sup>

$$L_r = 29 \text{ kips}$$

**iii) Floor Loads**

$$D_f = D A_{\text{floor}}$$

Where  $D = 30.0$  psf  
 $A_{\text{floor}} = 1,425$  ft<sup>2</sup>

$$D_f = 43 \text{ kips}$$

$$L_f = L A_{\text{floor}}$$

Where  $L = 40.0$  psf  
 $A_{\text{floor}} = 1,425$  ft<sup>2</sup>

$$L_f = 57 \text{ kips}$$

**iv) Wall Loads**

$$W_w = w_w 2 (L + W) H$$

Where  $w_w = 15$  psf (wall weight)  
 $L = 57.00$  feet  
 $W = 25.00$  feet  
 $H = (0.5 (H_a + H_b)) = 11$  feet and  $H_a = 10.00$  feet  
 $H_b = 12.00$  feet

$$W_w = 27 \text{ kips}$$

**v) Story weight on columns**

$$P_D = D_r + N_{\text{floors}} (D_f + W_w)$$

Where  $D_r = 29$  kips (roof)  
 $N_{\text{floors}} = 3$   
 $D_f = 43$  kips (floor)  
 $W_w = 27$  kips (wall)

$$P_D = 238 \text{ kips}$$

$$P_L = L_r + N_{\text{floors}} L_f$$

Where  $L_r = 29$  kips (roof)  
 $N_{\text{floors}} = 3$   
 $L_f = 57$  kips (floor)

$$P_L = 200 \text{ kips}$$

**Note:** Per ASCE 7-10 Section 12.4.2.3 Note 1, 50% of live loads may be considered for Load Combination 5 for  $L_0 \leq 100$  psf

$$P_x = P_D + 0.5 P_L$$

Where  $P_D = 238$  kips  
 $P_L = 200$  kips

$$P_x = 338 \text{ kips}$$

**SPECIAL MOMENT FRAME DESIGN - STORY DRIFT AND STABILITY CHECK**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S  
 Floor Level : 1  
 N<sub>S</sub> : 3 (Total Number of Stories)

**b) Check of P - Delta Effects (ASCE 7-10 Section 12.8.7)**

$$\theta = \text{Stability Coefficient per EQ 12.8-16}$$

$$= (P_x \Delta_{xe-1} I_b) / (V_x H_{sx} C_d) \leq 0.10$$

Where P<sub>x</sub> = 338 kips

$\Delta_{xe-1}$  = Seismic Design Story Drift of Level x-1 - RBS

$$= C_d (1.0 + A_{RBS}) \Delta x_{e-1} / I_b \quad (12.8-15)$$

for C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Ta

A<sub>RBS</sub> = 6.88 % Amplification

$$= 5.50 \times (1.069) \times 0.196 / 1.0$$

$\Delta_{xe-1}$  = 0.196 inches ( " for Level Below

I<sub>b</sub> = 1.0 Importance Factor, Table 11.5-2

$\Delta_{xe-1} = 1.15$ inches
-------------------------------

I<sub>b</sub> = 1.0 Importance Factor, Table 11.5-2

V<sub>x</sub> = 8 kips (Story Shear)

H = 11.00 feet  
 = 132.00 inches

C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Table 12.2-1)

$\theta = 0.066$
------------------

OK

**c) Maximum Value for Stability Coefficient**

$$\theta_{MAX} = 0.5 / (\beta C_d) \leq 0.25 \quad (12.8-17)$$

Where  $\beta$  = Shear DCR for Level x

= 1.0 (Conservative assumption per 12.8.7)

C<sub>d</sub> = 5.50 Deflection Amplification Factor (ASCE 7-10 Table 12.2-1)

$\theta_{MAX} = 0.091$
------------------------

OK

Note:  $\theta = 0.066$  radians

OK

<b>Level 1 is considered stable</b>
-------------------------------------

AISC SMRF DESIGN -  
RBS BEAM DESIGN

**SPECIAL MOMENT FRAME DESIGN - SMF REDUCED BEAM SECTION BEAM DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : N-S  
 Floor Level : 2

Beam ID: BM-1  
 Gridline: 10

**1. Member Selection and Moment Frame Column Geometry**

**Girder Data:**

S = 14.00 feet (Girder Span)  
 $L_{trib} = 4.00$  feet (Tributary Width - for beam bracing)

**SMF Members**

	Girders			Beam Bracing	
	Column	Left	Right		
	W8x67	W10x30		L4x4x3/8	
A	19.70	8.84		2.86	in <sup>2</sup>
d	9.00	10.50		-	in
t <sub>w</sub>	0.57	0.30		-	in
b <sub>f</sub>	8.28	5.81		4.00	in
t <sub>f</sub>	0.94	0.51		0.38	in
r <sub>x</sub>	3.72	4.38		1.23	in
r <sub>y</sub>	2.12	1.37		1.23	in
K	1.33	0.81		-	in
K <sub>1</sub>	0.94	0.69		-	in
T	5.75	8.25		-	in
Z <sub>x</sub>	70	37		-	in <sup>3</sup>
I <sub>x</sub>	272	170		-	in <sup>4</sup>

RBS Beam Designed:

**Note:** Both girders shown (if selected), only one checked; default is **Left** girder.

**Material Properties (Seismic Design Manual as referenced)**

E = 29,000 ksi

	Beams	Angle Bracing
Type	A572, Gr. 50	A36
F <sub>y</sub> (ksi)	50	36
F <sub>u</sub> (ksi)	65	
R <sub>y</sub>	1.10	
R <sub>t</sub>	1.10	

(F<sub>y</sub> min specified, AISC 360-10 Table 2-4, pg 2-48)  
 (F<sub>u</sub> stress specified, AISC 360-10 Table 2-4, pg 2-48)  
 (Ratio of Expected F<sub>y</sub> to min F<sub>y</sub> specified; AISC 341-10 Table A3.1)  
 (Ratio of Expected F<sub>u</sub> to min F<sub>u</sub> specified; AISC 341-10 Table A3.1)

**Reduced Beam Section Geometry**

Parameter	Left Beam	Right Beam
a (inches)	3.50	3.50
b (inches)	7.50 <b>OK</b>	7.50
c (inches)	1.00 <b>OK</b>	1.00
R (inches)	7.53	

**AISC 358-10 Section 5.3.1 - Beam Limitations :**

Parameter	Limit	Member	
d	36.00	10.5	inches (Beam Depth)
Weight	300	30	P/lf (Beam weight)
t <sub>f</sub>	1.75	0.94	inches (Flange thickness)
Span-Depth Ratio	7.0	15.1	

**Note:** W10x30 Beam OK

Where  $R = (b^2/4 + c^2) / 2c$

**Reduced Beam Section Limits (AISC 358-10 Section 5.8)**

Parameter	Limits	Left Beam		Right Beam	
		Lower (inches)	Upper (inches)	Lower (inches)	Upper (inches)
a	$0.50 b_{bf} \leq a \leq 0.75 b_{bf}$	2.91	4.36		
b	$0.65 d \leq b \leq 0.85 d$	6.83	8.93		
c	$0.10 b_{bf} \leq c \leq 0.25 b_{bf}$	0.58	1.45		

(AISC 358-10 Eq. 5.8-1)  
 (AISC 358-10 Eq. 5.8-2)  
 (AISC 358-10 Eq. 5.8-3)

**2. Member and System Demands**

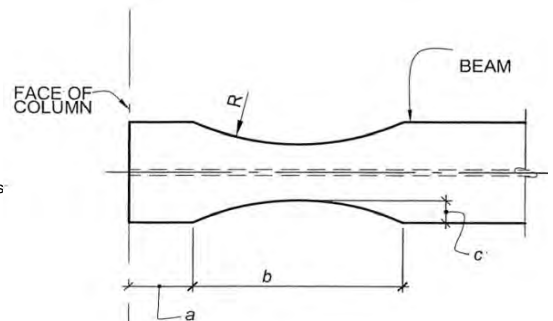
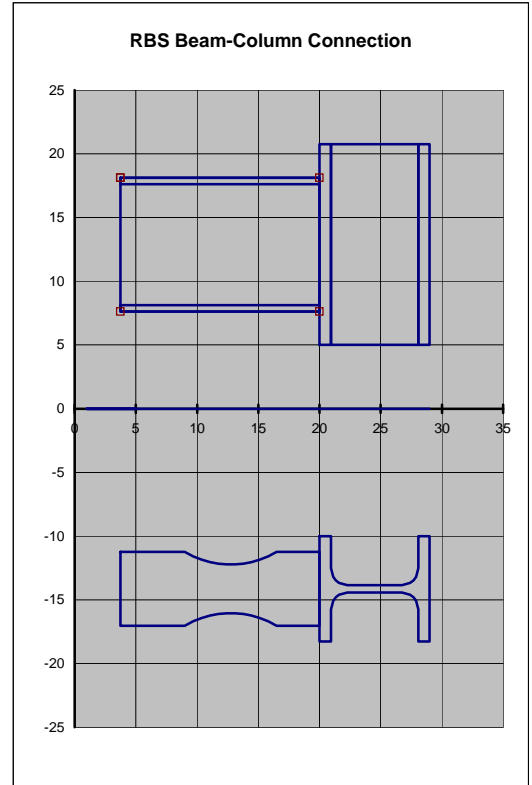
**Girder Demands - Unfactored**

	Dead	Live	Snow	EQ	
V	7.0	0.5		3.0	Kips
M	12.0	1.0		20.0	Kip-ft

3.63125  
 7.875  
 1.01675

**Seismic Parameters:**

$\Omega_o = 3.0$  Overstrength Factor (ASCE Table 12.2-1)  
 $\rho = 1.30$  Redundancy Factor (ASCE Section 12.3.4)  
 SD C = E Seismic Design Category (ASCE 7-05 Section 11.4)  
 $S_{DS} = 1.091$  g's (Site Design Coefficient - Short Period)



**SPECIAL MOMENT FRAME DESIGN - SMF REDUCED BEAM SECTION BEAM DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : N-S  
 Floor Level : 2

Beam ID: BM-1  
 Gridline: 10

**3. Factored Loads**

Note: Factored Loads - Basic Combinations for Strength Design (ASCE 7-05 Section 12.4.2.3)

**i) Shear Force Demands**

$$V_u = (1.2 + 0.2 S_{DS}) V_D + \rho V_{EQ} + 0.5 V_L + 0.2 V_S$$

Where  $V_D = 7.0$  Kips (Dead Load)  
 $V_L = 0.5$  Kips (Live Load)\*  
 $V_S = 0.0$  Kips (Snow Load)  
 $V_E = 3.0$  Kips

and  $\rho = 1.3$  Redundancy Factor (ASCE Section 12.3.4)  
 $S_{DS} = 1.091$  g's (Site Design Coefficient - Short Period)

$$V_u = 14.1 \text{ kips}$$

**ii) Flexural Demands**

$$M_u = (1.2 + 0.2 S_{DS}) M_D + \rho M_{EQ} + 0.5 M_L + 0.2 M_S$$

Where  $M_D = 12.0$  Kip-ft (Dead Load)  
 $M_L = 1.0$  Kip-ft (Live Load)\*  
 $M_S = 0.0$  Kip-ft (Snow Load)  
 $M_{EQ} = M_u = 20$  Kip-ft

and  $\rho = 1.3$  Redundancy Factor (ASCE Section 12.3.4)  
 $S_{DS} = 1.091$  g's (Site Design Coefficient - Short Period)

$$M_u = 44 \text{ kip-ft}$$

**4. Seismic b/t Ratio Check (AISC 341-10 Table D1.1) - Left Girder**

at Flanges (Table D1.1):

$$\lambda_f = \frac{b_f}{2t_f}$$

and  $b_{f,RBS} = b_f - c$

$$b_{f,RBS} = 4.81 \text{ inches}$$

$$t_f = 0.51 \text{ inches}$$

$$\lambda_f = 4.72$$

$$\lambda_{hd} = 0.30 \sqrt{\frac{E}{F_y}}$$

Where  $E = 29,000$  Ksi  
 $F_y = 50$  Ksi (Fy min specified, AISC 360-10 Table 2-3, pg 2-40)

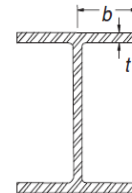
$$\lambda_{hd} = 7.22$$

**OK, Flanges satisfy Seismic b/t Ratio**

for  $b_f = 5.81$  inches  
 $c = 1.00$  inches

Note: Neglecting RBS cut, thus  $c = 0.0$ , is more conservative.

**Quick Check:**  
 Use AISC 341-10 **Table 1-3** for SMF sections that satisfy Seismic b/t requirements.



at Web (Table D1.1):

$$\lambda_w = \frac{h}{t_w}$$

and  $h = T = 8.25$  inches (from AISC Manual Table 1-1)  
 $t_w = 0.30$  inches ( " " )

$$\lambda_w = 27.50$$

Note: No Axial load in beam, therefore  $C_a = 0$ , and  $\lambda_{hd}$  as follows:

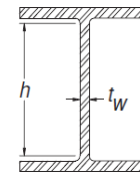
$$\lambda_{hd} = 2.45 \sqrt{\frac{E}{F_y}}$$

Where  $E = 29,000$  Ksi  
 $F_y = 50$  Ksi (Fy min specified, AISC 360-10 Table 2-3, pg 2-40)

$$\lambda_{hd} = 59.00$$

**OK, Web satisfies Seismic b/t Ratio**

**WF Section satisfies Seismic b/t Ratio for Highly Ductile Beam**



**SPECIAL MOMENT FRAME DESIGN - SMF REDUCED BEAM SECTION BEAM DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : N-S  
 Floor Level : 2

Beam ID: BM-1  
 Gridline: 10

**5. Flexural Strength (AISC 360-10 Section F2) - Left Girder**

**a) Unbraced length limits for Flexural members - Limit state of yielding - Gross Section**

$$L_p = 1.76 r_y \sqrt{\frac{E}{F_y}} \quad (F2 - 5)$$

Where  $r_y = 1.37$  inches  
 $E = 29,000$  Ksi  
 $F_y = 50$  Ksi

$L_p = 58.1$ inches $= 4.84$ feet
--------------------------------------

**Quick Check:**  
 Use AISC 360-10 **Table 4-1** for  $L_p$  and  $L_r$  values.

**b) Unbraced length limits for Flexural members - Limit state of Lateral Torsional Buckling - Gross Section**

**Note:**  $r_{ts}$  provided on AISC Table 1-1,  $L_r$  provided on AISC Table 3-6 for WF shapes, but not provided in Spreadsheet database and therefore calculated here.

$$r_{ts} = \frac{b_f}{\sqrt{12 \left( 1 + \frac{h t_w}{6 b_f t_f} \right)}}$$

and  $b_f = 5.81$  inches (from AISC Manual Table 1-1)  
 $h = T = 8.25$  inches (from AISC Manual Table 1-1)  
 $t_w = 0.30$  inches  
 $t_f = 0.51$  inches

$r_{ts} = 1.57$ inches
------------------------

No

$$L_r = 1.95 r_{ts} \frac{E}{0.7 F_y} \sqrt{\frac{J c}{S_x h_o} + \sqrt{\left( \frac{J c}{S_x h_o} \right)^2 + 6.76 \left( \frac{0.7 F_y}{E} \right)^2}} \quad (F2 - 6)$$

$L_r = 190.0$ inches $= 15.83$ feet
--

Where  $r_{ts} = 1.57$  inches  
 $E = 29,000$  Ksi  
 $F_y = 50$  Ksi  
 $J = 0.622$  in<sup>4</sup> (Table 1-1)  
 $c = 1$  (F2-8a)  
 $S_x = 32.4$  in<sup>3</sup>  
 $h_o = d - t_f = 9.99$  inches (Distance between flange centroids)

**c) Flexural Capacity - Yield Limit - Gross Section**

$$M_p = F_y Z_x$$

Where  $F_y = 50$  ksi  
 $Z_x = 36.60$  in<sup>3</sup>

$M_p = 1,830$ kip-in $= 153$ kip-ft
--

**d) Flexural Capacity reduced by Lateral-Torsional Buckling Effects**

**Unbraced length**

**Note:** Per AISC 341-10 Section D2b, both flanges must be laterally braced at intervals not to exceed:

$$L_b = 0.086 r_y E / F_y$$

Where  $r_y = 1.37$  inches  
 $E = 29,000$  Ksi  
 $F_y = 50$  Ksi

$L_b = 68.3$ inches $= 5.69$ feet
--------------------------------------

**Quick Check:**  
 Use AISC 341-10 **Table 4-2** (or **Table 1-3**) for  $L_b$  values for shape selected.

i) for  $L_p < L_b < L_r$ :

$$M_n = C_b \left[ M_p - (M_p - 0.7 F_y S_x) \left( \frac{L_b - L_p}{L_r - L_p} \right) \right] \leq M_p \quad (F2 - 2)$$

$M_n = 1,776$ Kip-in $= 148$ Kip-ft
--

and  $C_b = 1$  (AISC Section F1;  $C_b = 1.0$  Conservative, calculated otherwise)  
 $M_p = 1,830$  kip-in and  $L_b = 5.69$  feet  
 $F_y = 50$  Ksi  $L_p = 4.84$  feet  
 $S_x = 32.4$  in<sup>3</sup>  $L_r = 15.83$  feet

ii) for  $L_b > L_r$ :

$$M_n = F_{cr} Z_x$$

Where  $F_{cr} = \frac{C_b \pi^2 E}{\left( \frac{L_b}{r_{ts}} \right)^2} \sqrt{1 + 0.078 \frac{J c}{S_x h_o} \left( \frac{L_b}{r_{ts}} \right)^2}$  (F2 - 4)

$F_{cr} = 50.00$ Ksi
----------------------

$Z_x = 65.00$  in<sup>3</sup>

$M_n = 3,250$ Kip-in
----------------------

and  $C_b = 1$  (AISC Section F1; Conservative)  
 $E = 29,000$  Ksi  
 $L_b = 68.34$  inches  
 $r_{ts} = 1.57$  inches  
 $J = 0.622$  in<sup>4</sup> (Table 1-2)  
 $c = 1$  (F2-8a)  
 $S_x = 32.4$  in<sup>3</sup>  
 $h_o = d - t_f = 9.99$  inches (Distance between flange centroids)

**SPECIAL MOMENT FRAME DESIGN - SMF REDUCED BEAM SECTION BEAM DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : N-S  
 Floor Level : 2

Beam ID: BM-1  
 Gridline: 10

**e) Governing Flexural Capacity - Gross Section**

$M_n = 1,776$	Kip-in
$= 148$	Kip-ft

for  $L_b = 5.69$  feet  
 $L_p = 4.84$  feet  
 $L_r = 15.83$  feet

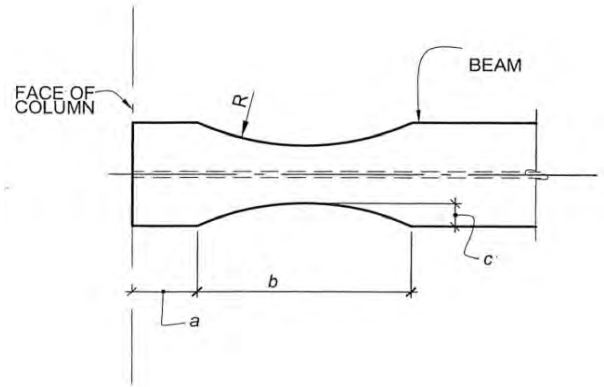
**f) Flexural Capacity - Reduced Beam Section (AISC 358-10 Section 5.8)**

$M_{pr} = Z_e F_y$       Where  $Z_e = Z_x - 2 c t_f (d - t_f)$       and  $Z_x = 36.60$  in<sup>3</sup>  
 $c = 1.00$  inches  
 $t_f = 0.51$  inches  
 $d = 10.50$  inches

$Z_e = 26$	in <sup>3</sup>
------------	-----------------

$F_y = 50$  Ksi

$M_{pr} = 1,321$	kip-in
$= 110$	kip-ft



**g) Girder Flexural Capacity - Left Girder**

$\phi_b M_x = \phi_b \text{ Min } (M_n, M_{pr})$       Where  $\phi_b = 0.90$  (AISC 360-10 Section F1)

$M_n = 148$  Kip-ft (Gross Section)  
 $M_{pr} = 110$  kip-ft (RBS Section)

$\phi_b M_x = 99$	kip-ft
-------------------	--------

**OK, > Mu**

Note:  $M_u = 44$  kip-ft

**6. Shear Capacity (AISC 360-10 Section G2) - Left Girder**

$\phi_v V = \phi_v 0.6 F_y A_w C_v$  for  $\frac{h}{t_w} \leq 2.24 \sqrt{\frac{E}{F_{yw}}}$  (G2-1)

Where  $\frac{h}{t_w} = 27.50$   
 $2.24 \sqrt{\frac{E}{F_{yw}}} = 53.95$

and  $h = T = 8.25$  inches (from AISC Manual Table 1-1)  
 $t_w = 0.30$  inches ( " " )  
 $E = 29,000$  ksi  
 $F_y = F_{yw} = 50$  Ksi

Where  $\phi_v = 1.00$  (AISC 360-10 Section G2.1)

$F_y = 50$  ksi

$A_w = d t_w = 3.15$  in<sup>2</sup>      and  $d = 10.50$  inches

$t_w = 0.30$  inches

$C_v = 1.0$  (G2-2)

$\phi_v V_n = 95$	kips
-------------------	------

**OK, > Vu**

Note:  $V_u = 14$  kips

**Use W10x30 for SMRF Left Girder**

**Quick Check:**

Use AISC 341-10 **Table 4-2** to get  $\phi R_{r1}$  value for WF shape value.

**SPECIAL MOMENT FRAME DESIGN - SMF REDUCED BEAM SECTION BEAM DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : N-S  
 Floor Level : 2

Beam ID: BM-1  
 Gridline: 10

**7. Lateral Girder Bracing Requirements (AISC 341-05 Section 9.8) - Left Girder**

a) Nodal Lateral Bracing (AISC 360-10 Appendix 6 and AISC 341-10 Section D2a) at expected plastic hinge location

$P_{br} = 0.02 M_r C_d / h_o$  (A-6-7)      Where  $M_r = R_y F_y Z$  (D1-1a)      and  $R_y = 1.10$  (Ratio of Expected  $F_y$  to min  $F_y$  specified; AISC 341-10 Table A3.1)  
 $F_y = 50$  Ksi  
 $Z_x = 36.60$  in<sup>3</sup>

$M_r = 2,013$  kip-in

$C_d = 1.0$  (AISC 360-10 Appendix 6.3.1a)

$h_o = d - t_f = 9.99$  inches (Distance between flange centroids)

$P_{br} = 4.03$  kips

b) Length of Angle Brace

$L_a = (L_{trib}^2 + d^2)^{0.5}$

Where  $L_{trib} = 4.00$  feet (Girder Tributary Width)  
 $= 48$  inches  
 $d = 10.50$  inches

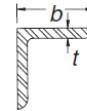
$L_a = 49$  inches  
 $= 4.09$  feet

**Quick Check:**  
 Use AISC 360-10 Table 4-12 to get  $\phi P_n$  values for eccentrically loaded single angles (use resulting  $KL = L$  value).

c) Brace Slenderness Check (AISC 360-10 Section B4.1a and Table B4.1a)

at Flanges (Table B4.1 Case 1):

$\lambda_y = b/t$       and  $b = 4.00$  inches (from AISC Manual Table 1-1)  
 $t = 0.38$  inches ( " " )  
 $\lambda_t = 10.67$   
 $\lambda_r = 0.45 \sqrt{\frac{E}{F_y}}$       Where  $E = 29,000$  Ksi  
 $F_y = 36$  Ksi ( $F_y$  min specified, AISC 360-10 Table 2-4, pg 2-48)  
 $\lambda_r = 12.77$   
**OK, Flanges are not Slender**



d) Determination of Brace Slenderness Ratio (AISC 360-10 Section E5(a))

Slenderness parameter:  $L_d/r_x = 39.9$       where  $L_a = 49$  inches  
 $r_x = 1.23$  inches

i) When  $0 \leq L_d/r_x \leq 80$  :       $KL/r = 72 + 0.75 L_d/r_x$  (E5-1)

$KL/r = 102.0$

ii) When  $L_d/r_x > 80$  :       $KL/r = 32 + 1.25 L_d/r_x \leq 200$  (E5-2)

$KL/r = 81.9$

=>  $KL/r = 102.0$

e) Brace Compressive Strength (AISC 360-10 Section E3)

$F_{cr} = \left[ 0.658 \frac{F_y}{E_c} \right] F_y$       when  $\frac{KL}{r} \leq 4.71 \sqrt{\frac{E}{F_y}}$  (E3-2)      Where  $4.71 \sqrt{\frac{E}{F_y}} = 134$       for  $E = 29,000$  ksi  
 $F_y = 36$  ksi

$F_{cr} = 20.83$  ksi (Governs)

$\frac{KL}{r} = 102.0$

$F_{cr} = 0.877 F_c$       when  $\frac{KL}{r} > 4.71 \sqrt{\frac{E}{F_y}}$  (E3-3)       $F_c = \frac{\pi^2 E}{\left[ \frac{KL}{r} \right]^2} = 27.53$  ksi

$F_{cr} = 24.15$  ksi

$F_{cr} = 20.83$  ksi

$\phi_c P_n = \phi_c F_{cr} A_g$       Where  $\phi_c = 0.90$  (AISC 360-10 Section E1)

$F_{cr} = 20.83$  ksi

$A_g = 2.86$  in<sup>2</sup>

$\phi_c P_n = 54$  kips

**OK, > P<sub>br</sub>**

**Note:** Compressive strength determined does **NOT** include connection eccentricity, and could therefore be unconservative. Check AISC 360-10 **Table 4-12** for angle brace capacity w/ connection eccentricity.



**SPECIAL MOMENT FRAME DESIGN - SMF REDUCED BEAM SECTION BEAM DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : N-S  
 Floor Level : 2

Beam ID: BM-1  
 Gridline: 10

f) Required Brace Stiffness (AISC 360-10 Appendix 6)

$$\beta_{br} = \frac{1}{\phi} \left( \frac{10 M_r C_d}{L_b h_o} \right)$$

Where  $\phi = 0.75$

$M_r = 2,013$  kip-in

$C_d = 1.0$

$L_b = 68.3$  inches (max girder unbraced length)

$h_o = d - t_f = 9.99$  inches (Distance between flange centroids)

$\beta_{br} = 39.3$ kip/in
----------------------------

g) Actual Brace Stiffness

$$K = \frac{A_g E}{L_a} \cos^2 \theta$$

Where  $\theta = \tan^{-1} (d/L_a)$

and  $d = 10.50$  inches

$L_a = 49$  inches

$\theta = 12.06$ degrees
--------------------------

$A_g = 2.86$  in<sup>2</sup>

$E = 29,000$  ksi

$L_a = 49$  inches

$K = 1650.7$ kip/in
---------------------

OK, >  $\beta$

<b>Use L4x4x3/8 kickers to brace beam bottom flange at a Maximum spacing of 5.75 feet on-center</b>
---

AISC SMRF DESIGN -  
COLUMN DESIGN

**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1      Gridline: 10

N<sub>s</sub> : 3 (Total Number of Stories)

**1. Member Selection and Moment Frame Column Geometry**

Note: This worksheet is meant for regular Moment Frame geometries consisting of the following:  
 - all frames identical in loading direction considered;  
 - same girder for each floor level, max of two floor levels framing into column;  
 - same span length each bay, variable number of interior bays, AISC shapes defined for typical exterior and interior columns.  
 - **Story vertical loads previously calculated for "1. SMF Story Drift, Stability" worksheet.**

Building Dimensions:

L = 57.00 feet  
 W = 25.00 feet

R<sub>L</sub> = 0.50 (Live load reduction for columns, ASCE Section 4.8)

Note: R<sub>L</sub> is used for determination of total vertical load supported by story.

Tributary Area for Lateral Force Resisting System:

Location Gridline	Length (feet)	Width (feet)	Area (ft <sup>2</sup> )
10	57.00	22.00	1,254

A<sub>LFRS</sub> = 1,254 ft<sup>2</sup>

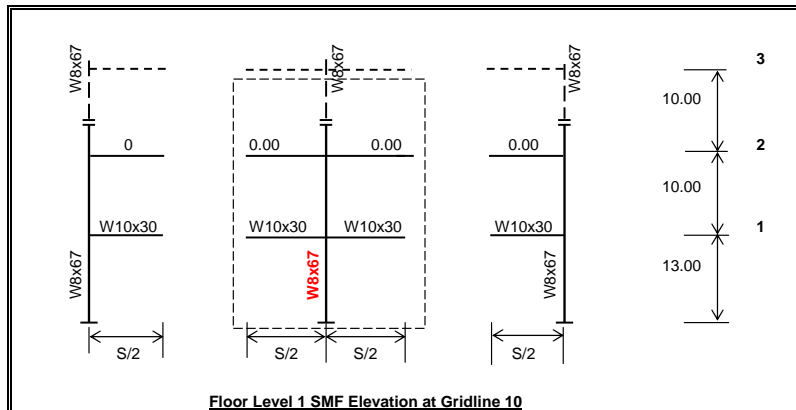
Moment Frame Data:

S = 14.00 feet (Span, typical)

N<sub>frames</sub> = 1 (# identical frames)

N<sub>int cols</sub> = 2 (# interior columns)

Floor Level	Height (feet)	AISC Shape	I <sub>x</sub> (in <sup>4</sup> )
3	10.00	-	-
2	10.00	-	-
1	13.00	W10x30	170



	Exterior Columns		Interior Columns		
	Top	Bottom	Top	Bottom*	
	W8x67	W8x67	W8x67	W8x67	
A	19.70	19.70	19.70	19.70	in <sup>2</sup>
d	9.00	9.00	9.00	9.00	in
t <sub>w</sub>	0.57	0.57	0.57	0.57	in
b <sub>t</sub>	8.28	8.28	8.28	8.28	in
t <sub>f</sub>	0.94	0.94	0.94	0.94	in
r <sub>x</sub>	3.72	3.72	3.72	3.72	in
r <sub>y</sub>	2.12	2.12	2.12	2.12	in
K	1.33	1.33	1.33	1.33	in
K <sub>1</sub>	0.94	0.94	0.94	0.94	in
T	5.75	5.75	5.75	5.75	in
Z <sub>x</sub>	70	70	70	70	in <sup>3</sup>
I <sub>x</sub>	272	272	272	272	in <sup>4</sup>
J	5.05	5.05	5.05	5.05	in <sup>4</sup>

AISC 358-10 Section 5.3.2 - Column Limitations :

d<sub>MAX</sub> = 36.00 inches (Max Column Depth)

Note : d<sub>c</sub> = 9.00 inches

W8x67 Column OK

Material Properties (Seismic Design Manual as referenced)

E = 29,000 ksi

Type	Columns	Beams	
	A992, Gr. 50	A572, Gr. 50	
F <sub>y</sub> (ksi)	50	50	(F <sub>y</sub> min specified, AISC 360-10 Table 2-4, pg 2-48)
F <sub>u</sub> (ksi)	65	65	(F <sub>u</sub> stress specified, AISC 360-10 Table 2-4, pg 2-48)
R <sub>y</sub>	1.10	1.10	(Ratio of Expected F <sub>y</sub> to min F <sub>y</sub> specified; AISC 341-10 Table A3.1)
R <sub>t</sub>	1.10	1.10	(Ratio of Expected F <sub>u</sub> to min F <sub>u</sub> specified; AISC 341-10 Table A3.1)

Column Demands - Unfactored

	Dead	Live	Snow	EQ	
P	8.0	1.0		3.0	Kips
V	2.0	1.0		5.0	Kips
M <sub>x, top</sub>	15.0	1.0		20.0	Kip-ft
M <sub>x, bot</sub>	7.0	0.5		30.0	Kip-ft

Results from Elastic Analysis :

Δ<sub>xe</sub> = 0.196 inches (Deformation for Level Above at Center of Mass, from elastic analysis)

Δ<sub>xe-1</sub> = 0.196 inches ( " for Level Below " )

V<sub>x</sub> = 8 Kips (Story Shear)

Assumptions:

- There is no transverse loading between the column supports in the plane of bending.
- Non-translation forces are due to Dead and Live loads, while Translation Forces due to Seismic Loads.
- Column tributary areas are constant across floor levels.
- Distributed load is applied uniformly over entire area for purposes of evaluating axial loads.

Seismic Parameters:

Ω<sub>p</sub> = 3.00 Overstrength Factor (ASCE Table 12.2-1)

ρ = 1.30 Redundancy Factor (ASCE Section 12.3.4)

SDC = E Seismic Design Category (ASCE 7 Section 11.4)

S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1              Gridline: 10

N<sub>s</sub> : 3 (Total Number of Stories)

**2. Factored Loads on Column or Story**

**a) Shear Demands:**

$$V_u = (1.2 + 0.2 S_{DS}) V_D + \rho V_{EQ} + 0.5 V_L + 0.2 V_S$$

Where V<sub>D</sub> = 2.00 Kips  
 V<sub>L</sub> = 1.00 Kips  
 V<sub>S</sub> = 0.00 Kips  
 V<sub>E</sub> = 5.00 Kips

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$V_u = 9.8 \text{ kips}$$

**b) Non-translation Forces (Gravity Loads):**

$$P_{nt} = (1.2 + 0.2 S_{DS}) P_D + \rho P_{EQ} + 0.5 P_L + 0.2 P_S$$

Where P<sub>D</sub> = 8.00 Kips  
 P<sub>L</sub> = 1.00 Kips  
 P<sub>S</sub> = 0.00 Kips  
 P<sub>E</sub> = 0.00 Kips

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$P_{nt} = 11.8 \text{ kips}$$

$$M_{nt, top} = (1.2 + 0.2 S_{DS}) M_D + \rho M_{EQ} + 0.5 M_L + 0.2 M_S$$

Where M<sub>D</sub> = 15.00 Kip-ft  
 M<sub>L</sub> = 1.00 Kip-ft  
 M<sub>S</sub> = 0.00 Kip-ft  
 M<sub>E</sub> = 0.00 Kip-ft

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$M_{nt, top} = 21.8 \text{ kips}$$

$$M_{nt, bot} = (1.2 + 0.2 S_{DS}) M_D + \rho M_{EQ} + 0.5 M_L + 0.2 M_S$$

Where M<sub>D</sub> = 7.00 Kip-ft  
 M<sub>L</sub> = 0.50 Kip-ft  
 M<sub>S</sub> = 0.00 Kip-ft  
 M<sub>E</sub> = 0.00 Kip-ft

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$M_{nt, bot} = 10.2 \text{ kips}$$

**c) Translation Forces (EQ Loads):**

$$P_{it} = (1.2 + 0.2 S_{DS}) P_D + \rho P_{EQ} + 0.5 P_L + 0.2 P_S$$

Where P<sub>D</sub> = 0.00 Kips  
 P<sub>L</sub> = 0.00 Kips  
 P<sub>S</sub> = 0.00 Kips  
 P<sub>E</sub> = 3.00 Kips

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$P_{it} = 3.9 \text{ kips}$$

$$M_{it, top} = (1.2 + 0.2 S_{DS}) M_D + \rho M_{EQ} + 0.5 M_L + 0.2 M_S$$

Where M<sub>D</sub> = 0.00 Kip-ft  
 M<sub>L</sub> = 0.00 Kip-ft  
 M<sub>S</sub> = 0.00 Kip-ft  
 M<sub>E</sub> = 20.00 Kip-ft

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$M_{it, top} = 26.0 \text{ kips}$$

$$M_{it, bot} = (1.2 + 0.2 S_{DS}) M_D + \rho M_{EQ} + 0.5 M_L + 0.2 M_S$$

Where M<sub>D</sub> = 0.00 Kip-ft  
 M<sub>L</sub> = 0.00 Kip-ft  
 M<sub>S</sub> = 0.00 Kip-ft  
 M<sub>E</sub> = 30.00 Kip-ft

and ρ = 1.3 Redundancy Factor  
 S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

$$M_{it, bot} = 39.0 \text{ kips}$$

**d) Total vertical load resisted by Story (AISC 360-10 Section C2.1(2), Appendix 8) and SMRF Columns:**

Note: Total vertical and SMF component are calculated here and used later in Section 6 (Second Order Effects).

**i) Total Vertical Load Supported by Story**

$$P_{Story} = (1.2 + 0.2 S_{DS}) P_D + \rho P_{EQ} + 0.5 R_L P_L + 0.2 P_S$$

Note: Gravity loads determined in "SMF Story Drift, Stability", copied here.

Where P<sub>D</sub> = D<sub>r</sub> + N<sub>floors</sub> (D<sub>r</sub> + W<sub>w</sub>) (Story Column Dead load - roof + floors)

and D<sub>r</sub> = 29 kips (roof)  
 N<sub>floors</sub> = 3  
 D<sub>r</sub> = 43 kips (floor)  
 W<sub>w</sub> = 27 kips (wall)

$$P_D = 238 \text{ Kips}$$

S<sub>DS</sub> = 1.091 g's (Site Design Coefficient - Short Period)

P<sub>L</sub> = L<sub>r</sub> + N<sub>floors</sub> L<sub>r</sub> (Story Column Live load - roof + floors)

and L<sub>r</sub> = 29 kips (roof)  
 N<sub>floors</sub> = 3  
 L<sub>r</sub> = 57 kips (floor)

$$P_L = 200 \text{ Kips}$$

R<sub>L</sub> = 0.50 (Live load reduction for columns, ASCE Section 4.8)

P<sub>S</sub> = 0.00 Kips

P<sub>E</sub> = 3.00 Kips

and ρ = 1.3 Redundancy Factor

$$P_{Story} = 391 \text{ kips}$$

**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1              Gridline: 10  
 N<sub>s</sub> : 3 (Total Number of Stories)

ii) Total Vertical Load Supported by SMF Columns

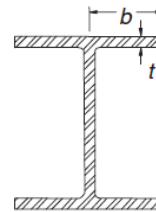
$P_{mf} = P_{Story} A_{LFRS} / A_{Floor}$       Where  $P_{Story} = 391$  Kips  
 $A_{LFRS} = 1,254$  ft<sup>2</sup> (Tributary Area for Lateral Force Resisting System)  
 $A_{floor} = A_{roof} = L W$       Where  $L = 57.00$  feet  
 $W = 25.00$  feet  
 $= 391 (0.88)$        $A_{floor} = A_{roof} = 1,425$  ft<sup>2</sup>  
 $P_{mf} = 344$  Kips

**3. Column Slenderness Check**

Note: Seismic Provisions Section E3.5a states that Beam and Column Members shall meet requirements of Section D1.1 for Highly ductile elements.

a) Flange Width-thickness Ratio - Actual (AISC 341-10 Table D1.1).

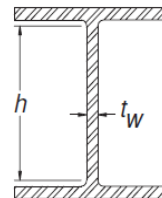
$\lambda_f = b_f / (2 t_f)$       Where  $b_f = 8.28$  inches  
 $t_f = 0.94$  inches  
 $\lambda_f = 4.43$



**Quick Check:**  
 Use AISC 341-10 Table 1-3 for SMF Sections that satisfy Seismic b/t requirements.

b) Flange Width-thickness Ratio - Highly Ductile Member

$\lambda_{hdfr} = 0.30 (E / F_y)^{0.5}$  (AISC 341-10 Table D1.1)      Where  $E = 29,000$  Ksi  
 $F_y = 50$  Ksi  
 $\lambda_{hdfr} = 7.22$  **OK**  
**Limiting b/t Ratios OK for Flanges**



c) Width-thickness Ratio for Web - Actual (AISC 341-10 Table D1.1).

$\lambda_w = h / t_w$       Where  $h = d - 2 K = 6.34$  inches  
 $t_w = 0.57$  inches  
 $\lambda_w = 11.12$

d) Limiting Width-thickness Ratio for Web in Flexural/Axial Compression - Highly Ductile Members

i) Axial Load Ratio

$C_a = P_u / (\phi_b P_y) = P_u / (\phi_b F_y A_g)$  (AISC 341-10 Table D1.1)

Where  $P_u = P_{nt} + B_2 P_t$       and  $P_{nt} = 11.8$  kips  
 $B_2 = 1.07$  (Calculated later)  
 $P_t = 3.9$  kips

$P_u = 16.0$  kips

$\phi_b = 0.90$  (AISC 350-10 Section E1)  
 $F_y = 50.00$  ksi  
 $A_g = 19.70$  in<sup>2</sup>

$C_a = 0.0181$

ii) Low Axial Loading

$\lambda_{hdw} = 2.45 (E / F_y)^{0.50} (1 - 0.93 C_a)$  for  $C_a \leq 0.125$

Where  $E = 29,000$  Ksi  
 $F_y = 50.0$  Ksi  
 $C_a = 0.018$

$\lambda_{hdw} = 58.0$  **(Controls!)**

iii) Axial Loading - All other cases

$\lambda_{hdw} = 0.77 (E / F_y)^{0.50} (2.93 - C_a) \geq 1.49 (E / F_y)^{0.50}$  for  $C_a \geq 0.125$

Where  $E = 29,000$  Ksi  
 $F_y = 50.0$  Ksi  
 $C_a = 0.018$

$\lambda_{hdw} = 54.0$

$\lambda_{hdw} = 58.0$  **OK**

**Limiting b/t Ratios OK for Web**

**WF Section satisfies Seismic b/t Ratio for Highly Ductile Column**

**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1      Gridline: 10

N<sub>s</sub> : 3 (Total Number of Stories)

**4. Flexural Strength (AISC 360-10 Section F2)**

**a) Unbraced length limits for Flexural members - Limit state of yielding**

$$L_p = 1.76 r_y \sqrt{\frac{E}{F_y}} \quad (F2 - 5) \quad \text{Where } r_y = 2.12 \text{ inches}$$

$$E = 29,000 \text{ Ksi}$$

$$F_y = 50 \text{ Ksi}$$

$$L_p = 89.9 \text{ inches}$$

$$= 7.49 \text{ feet}$$

**Quick Check:**  
 Use AISC 360-10 **Table 4-1** for L<sub>p</sub> and L<sub>r</sub> values.

**b) Unbraced length limits for Flexural members - Limit state of Lateral Torsional Buckling**

**Note:** r<sub>ts</sub> provided on AISC Table 1-1, L<sub>r</sub> provided on AISC Table 3-6 for WF shapes, calculated here conservatively per Specification Section F2.

$$r_{ts} = \frac{b_f}{\sqrt{12 \left( 1 + \frac{h t_w}{6 b_f t_f} \right)}} \quad \text{and } b_f = 8.28 \text{ inches (from AISC Manual Table 1-1)}$$

$$h = T = 5.75 \text{ inches (from AISC Manual Table 1-1)}$$

$$t_w = 0.57 \text{ inches}$$

$$t_f = 0.94 \text{ inches}$$

$$r_{ts} = 2.31 \text{ inches}$$

$$L_r = 1.95 r_{ts} \frac{E}{0.7 F_y} \sqrt{\frac{J c}{S_x h_o} + \sqrt{\left( \frac{J c}{S_x h_o} \right)^2 + 6.76 \left( \frac{0.7 F_y}{E} \right)^2}} \quad (F2 - 6)$$

$$L_r = 543.4 \text{ inches}$$

$$= 45.29 \text{ feet}$$

Where r<sub>ts</sub> = 2.31 inches  
 E = 29,000 Ksi  
 F<sub>y</sub> = 50 Ksi  
 J = 5.05 in<sup>4</sup> (Table 1-1)  
 c = 1 (F2-8a)  
 S<sub>x</sub> = 60.4 in<sup>3</sup>  
 h<sub>o</sub> = d - t<sub>f</sub> = 8.07 inches (Distance between flange centroids)

**c) Flexural Capacity - Yield Limit**

$$M_p = F_y Z_x \quad \text{Where } F_y = 50 \text{ ksi}$$

$$Z_x = 70 \text{ in}^3$$

$$M_p = 3,505 \text{ kip-in}$$

$$= 292 \text{ kip-ft}$$

**d) Flexural Capacity reduced by Lateral-Torsional Buckling Effects**

**Unbraced length**

$$L_b = \text{Max}(H_1, H_2) \quad \text{Where } H_2 = 10.00 \text{ feet}$$

$$H_1 = 13.00 \text{ feet}$$

$$L_b = 13.00 \text{ feet}$$

$$= 156.0 \text{ inches}$$

**i) for L<sub>p</sub> < L<sub>b</sub> < L<sub>r</sub>:**

$$M_n = C_b \left[ M_p - (M_p - 0.7 F_y S_x) \left( \frac{L_b - L_p}{L_r - L_p} \right) \right] \leq M_p \quad (F2 - 2)$$

and C<sub>b</sub> = 1 (AISC Section F1; Conservative)  
 M<sub>p</sub> = 3,505 kip-in      and L<sub>b</sub> = 13.00 feet  
 F<sub>y</sub> = 50 Ksi      L<sub>p</sub> = 7.49 feet  
 S<sub>x</sub> = 60.4 in<sup>3</sup>      L<sub>r</sub> = 45.29 feet

$$M_n = 3,302 \text{ Kip-in}$$

**ii) for L<sub>b</sub> > L<sub>r</sub>:**

$$M_n = F_{cr} Z_x \quad \text{Where } F_{cr} = \frac{C_b \pi^2 E}{\left( \frac{L_b}{r_{ts}} \right)^2} \sqrt{1 + 0.078 \frac{J c}{S_x h_o} \left( \frac{L_b}{r_{ts}} \right)^2} \quad (F2 - 4)$$

$$F_{cr} = 50.0 \text{ Ksi}$$

$$Z_x = 70 \text{ in}^3$$

$$M_n = 3,505 \text{ Kip-in}$$

and C<sub>b</sub> = 1 (AISC Section F1; Conservative)  
 E = 29,000 Ksi  
 L<sub>b</sub> = 156.00 inches  
 r<sub>ts</sub> = 2.31 inches  
 J = 5.05 in<sup>4</sup> (Table 1-1)  
 c = 1 (F2-8a)  
 S<sub>x</sub> = 60.4 in<sup>3</sup>  
 h<sub>o</sub> = d - t<sub>f</sub> = 8.07 inches (Distance between flange centroids)

**e) Governing Flexural Capacity**

$$\phi_b M_n = \phi_b M_n \quad \text{Where } \phi_b = 0.90 \text{ (AISC 360-10 Section F1)}$$

$$M_n = 3,302 \text{ Kip-in}$$

$$= 275 \text{ Kip-ft}$$

for L<sub>b</sub> = 13.00 feet  
 L<sub>p</sub> = 7.49 feet  
 L<sub>r</sub> = 45.29 feet

$$\phi_b M_n = 2,972 \text{ kip-ft}$$

$$= 248 \text{ kip-ft}$$

**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1      Gridline: 10

N<sub>s</sub> : 3 (Total Number of Stories)

**5. Compressive Strength (AISC 360-10 Section E3)**

**a) Determination of Column Available Nominal Compressive Strength (Capacity)**

Note: The Direct Analysis Method of Design (AISC 360-10 Section C1.1) consists of the following: ...  
 - Required Strength (Demands) in accordance with Section C2;  
 - Available Strength (Capacity) in accordance with Section C3, as performed here;

Column Available Nominal Compressive Strength (Capacity)

**i) Slenderness Ratio Check:**

$$\left(\frac{KL}{r}\right)_x = 41.9 \quad \text{for } K_x = 1.00 \text{ (AISC 360-10 Section C3)}$$

L<sub>x</sub> = L = 156 inches  
 r<sub>x</sub> = 3.72 inches

**OK, < 200**

Note: Effective Length calcs no longer performed in AISC 360-10.

$$\left(\frac{KL}{r}\right)_y = 73.6 \quad \text{for } K_y = 1.00 \text{ (AISC 360-10 Section C3)}$$

L<sub>y</sub> = L = 156 inches  
 r<sub>y</sub> = 2.12 inches

**OK, < 200**

**ii) Compressive Strength (Specification Section E3):**

$$F_{cr} = \left[0.658 \frac{F_y}{E}\right] F_y \quad \text{when } \frac{KL}{r} \leq 4.71 \sqrt{\frac{E}{F_y}} \quad \text{(E3-2)}$$

Where  $4.71 \sqrt{\frac{E}{F_y}} = 113$       for E = 29,000 ksi  
 F<sub>y</sub> = 50 ksi

$F_{cr} = 33.65 \text{ ksi}$  (Governs)

$\frac{KL}{r} = 73.6$

$$F_{cr} = 0.877 F_c \quad \text{when } \frac{KL}{r} > 4.71 \sqrt{\frac{E}{F_y}} \quad \text{(E3-3)}$$

$$F_c = \frac{\pi^2 E}{\left[\frac{KL}{r}\right]^2} = 52.86 \text{ ksi} \quad \text{(E3-4)}$$

$F_{cr} = 46.36 \text{ ksi}$

$F_{cr} = 33.65 \text{ ksi}$

$\phi_c P_n = \phi_c F_{cr} A_g$

Where  $\phi_c = 0.90$  (AISC 360-10 Section E1)

F<sub>cr</sub> = 33.65 ksi  
 A<sub>g</sub> = 19.70 in<sup>2</sup>

$\phi_c P_n = 597 \text{ kips}$

**Quick Check:**

Use AISC 360-10 **Table 4-22** for  $\phi$  F<sub>cr</sub> values for limiting KL/r.

**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1      Gridline: 10  
 N<sub>s</sub> : 3 (Total Number of Stories)

**6. Second Order Effects (AISC 360-10 Section C2.1(2) and Appendix 8):**

**a) Approximate Second Order Analysis (AISC 360-10 Appendix 8)**

$$M_r = B_1 M_{nt} + B_2 M_{lt} \quad (A.8-1)$$

$$P_r = P_{nt} + B_2 P_{lt} \quad (A.8-2)$$

Where  $M_{nt} = M_u =$  Required Flexural strength w/o lateral translation  
 = 22 kip-ft

$M_{lt} =$  Required Flexural strength due to lateral translation of frame  
 = 39.0 kip-ft

$B_1 =$  Amplification factor for P-Δ due to gravity loads

$$B_1 = \frac{C_m}{1 - \frac{\alpha P_r}{P_{e1}}} \geq 1.0$$

Where  $C_m = 0.6 - 0.4 (M_1/M_2)$  (A.8-4)

and  $M_1 = 21.77$  kip-ft  
 $M_2 = M_u = 21.77$  kip-ft

$$C_m = 0.20 \quad (\text{AISC 360-10 Section C2.1(2), Appendix 8})$$

$\alpha = 1.00$  (LRFD Approach)

$P_r = P_{nt} + B_2 P_{lt}$       and  $P_{nt} = 12$  kips (axial load w/o translation)  
 $B_2 = 1.07$  (Calculated below)  
 $P_{lt} = P_u = 3.9$  kips (axial load with translation)

$$P_r = 16.0 \text{ kips}$$

$P_{e1} = \frac{\pi^2 EI}{(K_1 L)^2}$  (A.8-5)      for  $E = 29,000$  ksi  
 $I_{xc} = 272$  in<sup>4</sup>  
 $K_1 = 1.00$  (AISC 360-10 Section C3)  
 $L = L_u = 156$  inches

$$= 0.201$$

$$B_1 = 1.00$$

$$P_{e1} = 3,199 \text{ kips}$$

$B_2 =$  Amplification factor for P-Δ due to Lateral Movement

**Note:** Effective Length calcs no longer performed in AISC 360-10.

$$B_2 = \frac{1}{1 - \left[ \frac{\alpha P_{\text{Story}}}{P_{e\text{Story}}} \right]} \geq 1.0$$

Where  $\alpha = 1.00$  (LRFD Approach)

$P_{\text{Story}} = 391$  kips

$P_{e\text{Story}} =$  Elastic Critical Buckling Strength for Story

$= R_M H L / \Delta_H$  (A-8-7)      and  $R_M = 1 - 0.15 P_{nt} / P_{\text{Story}}$       for  $P_{\text{Story}} = 391$  kips  
 $P_{nt} = 344$  Kips

$$R_M = 0.87$$

$H = V_x = 8$  Kips (Story Shear)

$L = H_f = 13.00$  feet  
 = 156 inches

$\Delta_H = \Delta_{xe} = 0.196$  inches (Deformation for Level Above at Center of Mass, from elastic analysis)

$$P_{e\text{Story}} = 5,649 \text{ kips}$$

$$B_2 = 1.07$$

$$M_r = 64 \text{ kip-ft}$$

$$P_r = 16.0 \text{ kips}$$



**SPECIAL MOMENT FRAME DESIGN - SMF COLUMN DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : N-S      Column ID: C-1  
 Floor Level : 1      Gridline: 10  
 N<sub>s</sub> : 3 (Total Number of Stories)

**7. Combined Flexure and Axial loads**

(a) For  $\frac{P_r}{P_c} \geq 0.2$

$$\frac{P_r}{P_c} + \frac{8}{9} \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad \text{(H1-1a)}$$

(b) For  $\frac{P_r}{P_c} < 0.2$

$$\frac{P_r}{2P_c} + \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad \text{(H1-1b)}$$

Where P<sub>r</sub> = 16 kips  
 φ<sub>c</sub> P<sub>n</sub> = 597 kips  
 M<sub>r</sub> = 64 kip-ft  
 φ<sub>b</sub> M<sub>n</sub> = 248 kip-ft

Note: M<sub>vx</sub> and M<sub>vy</sub> not considered.

P<sub>r</sub>/φ<sub>c</sub> P<sub>n</sub> = 0.027 **Therefore EQ H1-1b Applies!**

$$\frac{P_r}{P_c} + \frac{8}{9} \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) = \text{NA}$$

$$\frac{P_r}{2P_c} + \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) = 0.271 \quad \text{OK, < 1.0}$$

Note: Per comments on AISC 341-05 Example 4.9, decreasing column size to optimize drift control and least weight solution might not result in the least cost solution, as column might require use of thick doubler plates and large heavily welded column stiffeners.

**W8x67 OK thus far!**

**8. Shear Capacity**

$$\phi_v V = \phi_v 0.6 F_y A_w C_v \quad \text{for} \quad \frac{h}{t_w} \leq 2.24 \sqrt{\frac{E}{F_{yw}}} \quad \text{(G2-1)}$$

Where  $\frac{h}{t_w} = 10.09$       and h = T = 5.75 inches (from AISC Manual Table 1-1)  
 $t_w = 0.57$  inches ( " )  
 $2.24 \sqrt{\frac{E}{F_{yw}}} = 53.95$       E = 29,000 ksi  
 F<sub>y</sub> = F<sub>yw</sub> = 50 Ksi

**OK**

and φ<sub>v</sub> = 1.00 (AISC 360-10 Section G2.1)  
 F<sub>y</sub> = 50.00 ksi  
 A<sub>w</sub> = d t<sub>w</sub> = 5.13 in<sup>2</sup>      and d = 9.00 inches  
 $t_w = 0.57$  inches  
 C<sub>v</sub> = 1.0 (G2-2)

φ<sub>v</sub> V<sub>n</sub> = 154 kips

**OK, > V<sub>u</sub>**

**Use W8x67 for SMF Column Member**

**Quick Check:**

Use AISC 341-10 **Table 4-2** to get φ R<sub>v1</sub> value for WF shape value.

AISC SMRF DESIGN -  
BEAM-COLUMN CONNECTION DESIGN

**SPECIAL MOMENT FRAME DESIGN BEAM - COLUMN CONNECTION DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : **N-S**  
 Floor Level : **1**

Connection ID: **JT-1**  
 Gridline: **10**

$N_s$  : **3** (Total Number of Stories)

**1. Member Selection and Moment Frame Column Geometry**

Girder Data:

H = **0.00** feet (floor height above connection)  
 $L_1$  = **14.00** feet (Left Girder Span)  
 $L_2$  = **0.00** feet (Right Girder Span)

SMF Members

	Girders		
	Column	Left	
	<b>W8x67</b>	<b>W10x30</b>	
A	19.70	8.84	in <sup>2</sup>
d	9.00	10.50	in
$t_w$	0.57	0.30	in
$b_f$	8.28	5.81	in
$t_f$	0.94	0.51	in
$r_x$	3.72	4.38	in
$r_y$	2.12	1.37	in
K	1.33	0.81	in
$K_1$	0.94	0.69	in
T	5.75	8.25	in
$Z_x$	70	37	in <sup>3</sup>
$I_x$	272	170	in <sup>4</sup>

Material Properties (Seismic Design Manual as referenced)

E = **29,000** ksi

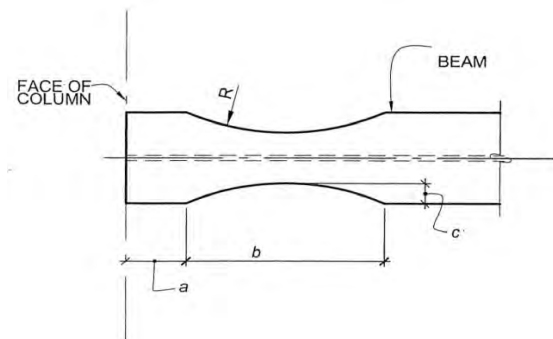
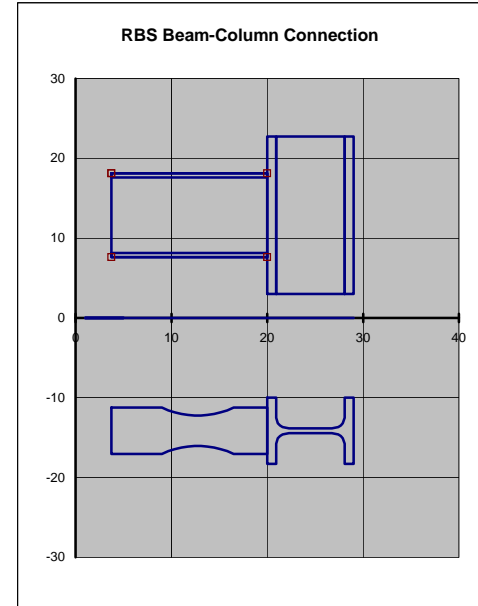
Type	Column	Beams	
	A572, Gr. 50	A572, Gr. 50	
$F_y$ (ksi)	50	50	( $F_y$ min specified, AISC 360-10 Table 2-4, pg 2-48)
$F_u$ (ksi)	65	65	( $F_u$ stress specified, AISC 360-10 Table 2-4, pg 2-48)
$R_y$	1.10	1.10	(Ratio of Expected $F_y$ to min $F_y$ specified; AISC 341-10 Table A3.1)
$R_t$	1.10	1.10	(Ratio of Expected $F_u$ to min $F_u$ specified; AISC 341-10 Table A3.1)

Reduced Beam Section Geometry (if used):

Parameter	Left Beam	Right Beam
a (inches)	3.50	3.50
b (inches)	7.50	7.50
c (inches)	1.00	1.00
R (inches)	7.53	

Where  $R = (b^2/4 + c^2) / 2c$

Reduced Beam Section Limits (AISC 358-10 Section 5.8)							
Parameter	Limits	Left Beam			Right Beam		
		Lower (inches)	Upper (inches)	Average (inches)	Lower (inches)	Upper (inches)	Average (inches)
a	$0.50 b_{bf} \leq a \leq 0.75 b_{bf}$	2.91	4.36	3.63			
b	$0.65 d \leq b \leq 0.85 d$	6.83	8.93	7.88			
c	$0.10 b_{bf} \leq c \leq 0.25 b_{bf}$	0.58	1.45	1.02			



**2. Member and System Demands**

Girder Gravity Loads - Unfactored

	Dead	Live	Snow	
$W_{left}$	0.98	0.04		Kip/ft
$W_{right}$	0.98	0.04		Kip/ft

$P_u$  = **12** kips

Seismic Parameters:

$\Omega_o$  = **3.0** Overstrength Factor (ASCE Table 12.2-1)  
 $\rho$  = **1.30** Redundancy Factor (ASCE Section 12.3.4)  
 SDC = **E** Seismic Design Category (ASCE 7-05 Section 11.4)  
 $S_{DS}$  = **1.091** g's (Site Design Coefficient - Short Period)

**SPECIAL MOMENT FRAME DESIGN BEAM - COLUMN CONNECTION DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : **N-S**  
 Floor Level : **1**

Connection ID: **JT-1**  
 Gridline: **10**

N<sub>s</sub> : **3** (Total Number of Stories)

**3. Panel Zone Required Strength**

Frame Rotation: **R**

Notes: 1. L for Left rotation (Counterclockwise); Right rotation (Clockwise) is default.  
 2. Only effect of frame rotation is sign reversal of beam plastic hinges, which act with or against gravity loads.

**3.1 Probable Moments at Plastic Hinges**

Note: Source is AISC 358-10, "Prequalified Connections for Special and Intermediate Steel Moment Frames for Seismic Applications" standard, Section 2.4.3.

a) **Left Beam**

$$M_{pr1} = C_{pr} R_y F_y Z_{e1} \quad (2.4.3-1)$$

Where  $C_{pr} = 0.5 (F_y + F_u) / F_y \leq 1.20$  (2.4.3-2) and  $F_y = 50$  Ksi  
 $F_u = 65$  Ksi

$$C_{pr} = 1.15$$

$R_y = 1.10$  (Ratio of Expected  $F_y$  to min  $F_y$  specified; AISC 341-10 Table A3.1)  
 $F_y = 50$  Ksi

$Z_{e1} = Z_{x1} - 2 c_1 t_1 (d_1 - t_1)$  (5.8-4) and  $Z_{x1} = 37$  in<sup>3</sup>  
 $c_1 = 1.00$  inches  
 $t_1 = 0.51$  inches  
 $d_1 = 10.50$  inches

$$Z_{e1} = 26 \text{ in}^3$$

$$M_{pr1} = 1,670 \text{ kip-in (Left Beam)}$$

$$= 139 \text{ kip-ft}$$

b) **Right Beam (Not Used!)**

$$M_{pr2} = C_{pr} R_y F_y Z_{e2} \quad (2.4.3-1)$$

Where  $C_{pr} =$

$R_y =$   
 $F_y =$  Ksi

$Z_{e2} = Z_{x2} - 2 c_2 t_2 (d_2 - t_2)$  and  $Z_{x2} =$  in<sup>3</sup>  
 $c_2 =$  inches  
 $t_2 =$  inches  
 $d_2 =$  inches

$$Z_{e2} = \text{in}^3$$

$$M_{pr2} = \text{kip-in (Right Beam)}$$

$$= \text{kip-ft}$$

**3.2 Expected Shear Force at Plastic Hinges**

a) **Left Beam**

$$V_{p1} = \frac{2 M_{pr1}}{L_1} + \frac{W_{u1} L_1}{2} \quad (5.8-9)$$

Where  $M_{pr1} = 1,670$  kip-in  
 $= 139$  kip-ft

$L_1 = L_1 - d_c - 2 S_{h1}$  and  $L_1 = 14.00$  feet

$d_c = 9.00$  inches (Column Depth)

$S_{h1} = a_1 + b_1/2$  for  $a_1 = 3.50$  inches  
 $b_1 = 7.50$  inches

$$S_{h1} = 7.25 \text{ inches}$$

$$L_1' = 12.04 \text{ feet}$$

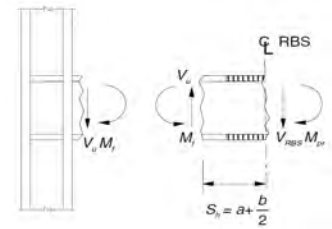
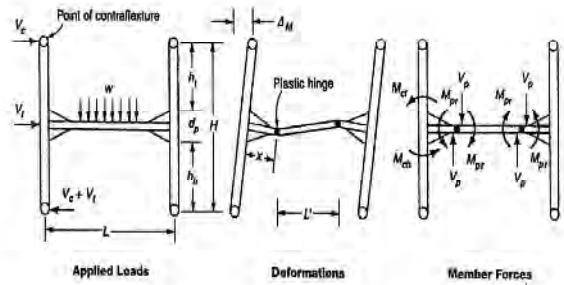
$W_{u1} = 1.2 w_{D1} + 0.5 w_{L1} + 0.2 w_{S1}$  and  $w_{D1} = 0.98$  kip/ft  
 $w_{L1} = 0.04$  kip/ft  
 $w_{S1} = 0.00$  kip/ft

$$W_{u1} = 1.20 \text{ kip/ft}$$

$L_1 = 14.00$  feet

$$V_{p1} = 32 \text{ kips}$$

Note:  $\phi_v V_n = 95$  kips (from SMF RBS Beam Design)  
**OK**



b) **Right Beam (Not Used!)**

$$V_{p2} = \frac{2 M_{pr2}}{L_2} + \frac{W_{u2} L_2}{2}$$

Where  $M_{pr2} =$  kip-in  
 $=$  kip-ft

$L_1' = L_1 - d_c - 2 S_{h2}$  and  $L_2 =$  feet

$d_c =$  inches (Column Depth)

$S_{h2} = a_2 + b_2/2$  for  $a_2 =$  inches  
 $b_2 =$  inches

$$S_{h2} = \text{inches}$$

$$L_2 = \text{feet}$$

$W_{u2} = 1.2 w_{D2} + 0.5 w_{L2} + 0.2 w_{S2}$  and  $w_{D2} =$  kip/ft  
 $w_{L2} =$  kip/ft  
 $w_{S2} =$  kip/ft

$$W_{u2} = \text{kip/ft}$$

$L_2 =$  feet

$$V_{p2} = \text{kips}$$

**SPECIAL MOMENT FRAME DESIGN BEAM - COLUMN CONNECTION DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE I - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : **N-S** Connection ID: **JT-1**  
 Floor Level : **1** Gridline: **10**  
 N<sub>s</sub> : **3** (Total Number of Stories)

**3.3 Probable Maximum Moment at Column Face**

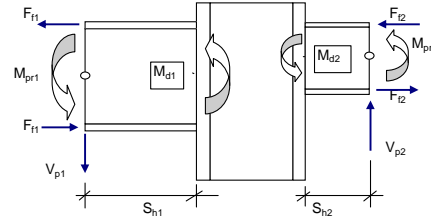
**a) Left Beam**

$$M_{d1} = M_{pr1} + M_{uv1} + M_g$$

$$= M_{pr1} + V_{p1} S_{h1} + 0.5 W_{u1} S_{h1}^2$$

Where  $M_{pr1} = 1,670$  kip-in  
 $V_{p1} = 32$  kips  
 $S_{h1} = 7.25$  inches  
 $W_{u1} = 1.20$  kip/ft  
 $= 0.10$  kip/in

$M_{d1} = 1,902$ kip-in $= 158$ kip-ft
---



**Check Unreduced section capacity at column face (AISC 358 5.8-8):**

$$M_{pe1} = R_y F_y Z_{x1}$$

Where  $R_y = 1.10$  (Ratio of Expected  $F_y$  to min  $F_y$  specified; SDM Table I-6-1)  
 $F_y = 50$  Ksi  
 $Z_{x1} = 37$  in<sup>3</sup>

$M_{pe1} = 2,013$ kip-in <b>OK, &gt; M<sub>d1</sub></b>
--

**b) Right Beam (Not Used!)**

$$M_{d2} = M_{pr2} + M_{uv2} + M_g$$

$$= M_{pr2} + V_{p2} S_{h2} + 0.5 W_{u2} S_{h2}^2$$

Where  $M_{pr2} =$  kip-ft  
 $V_{p2} =$  kips  
 $S_{h2} =$  inches  
 $W_{u2} =$  kip/ft  
 $=$  kip/in

$M_{d2} =$ kip-ft $=$ kip-ft
---------------------------------

**Quick Check:**  
 Use AISC 341-10 **Table 4-2** for  $R_y M_p$  value (Kip-ft), multiply by 12 for Kip-in .

**Check Unreduced section capacity at column face (AISC 358 5.8-8):**

$$M_{pe2} = R_y F_y Z_{x2}$$

Where  $R_y =$  (Ratio of Expected  $F_y$  to min  $F_y$  specified; SDM Table I-6-1)  
 $F_y =$  Ksi  
 $Z_{x2} =$  in<sup>3</sup>

$M_{pe2} =$ kip-in
--------------------

**3.4 Forces Developed in Beam Flanges (AISC 341-10 Section E3.6e(1))**

**a) Left Beam (Expected Beam Plastic Hinge forces at Column)**

$$F_{f1} = M_{d1} / (d_1 - t_{f1})$$

Where  $M_{d1} = 1,902$  kip-ft  
 $d_1 = 10.50$  in  
 $t_{f1} = 0.51$  in

$F_{f1} = 190$ kips
---------------------

**b) Right Beam (Expected Beam Plastic Hinge forces at Column) (Not Used!)**

$$F_{f2} = M_{d2} / (d_2 - t_{f2})$$

Where  $M_{d2} =$  kip-ft  
 $d_2 =$  in  
 $t_{f2} =$  in

$F_{f2} =$ kips
-----------------

**3.5 Required Shear Strength in Panel Zone (AISC 341-10 Section E3.6e (1))**

$$V_u = F_{f1} + F_{f2}$$

Where  $F_{f1} = 190$  kips  
 $F_{f2} = 0$  kips

$V_u = 190$ kips
------------------

**4. Check Column Beam Moment Ratio (AISC 341-10 Section E3.4a)**

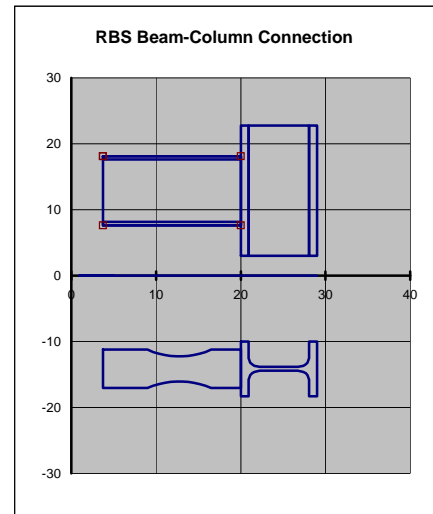
**4.1 Column Strength**

$$\Sigma M_{pc}^* = \Sigma Z_c (F_{yc} - P_u / A_g)$$

$$= n_c Z_c (F_{yc} - P_u / A_g)$$

Where  $n_c = 1$  Number of columns (1 for Roof Column, 2 otherwise)  
 $Z_c = 70$  in<sup>3</sup>  
 $F_{yc} = 50$  Ksi  
 $P_u = 12$  kips  
 $A_g = 19.70$  in<sup>2</sup>

$\Sigma M_{pc}^* = 3,463$ kip-in $= 289$ kip-ft
--



**SPECIAL MOMENT FRAME DESIGN BEAM - COLUMN CONNECTION DESIGN**  
**2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

Loading Direction : **N-S** Connection ID: **JT-1**  
 Floor Level : **1** Gridline: **10**  
 N<sub>s</sub> : **3** (Total Number of Stories)

**4.2 Expected Flexural Demands from Beams at Column Centerline**

$$\Sigma M_{pb}^* = \{ M_{pr1} + V_{p1} (S_{h1} + d_c/2) \} + \{ M_{pr2} + V_{p2} (S_{h2} + d_c/2) \}$$

Where M<sub>pr1</sub> = 1,670 kip-in  
 V<sub>p1</sub> = 32 kips  
 S<sub>h1</sub> = 7.25 inches  
 d<sub>c</sub> = 9.00 inches  
 M<sub>pr2</sub> = 0 kip-in  
 V<sub>p2</sub> = 0 kips  
 S<sub>h2</sub> = 0.00 inches

Σ M <sub>pb</sub> <sup>*</sup> = 2,041 kip-in
= 170 kip-ft

**4.3 Strong Column - Weak Beam Check**

Note: AISC 341-10 Section E3.4a requires that SMF connections satisfy the following strong-column/weak-beam criterion:

$$\frac{\Sigma M_{pc}^*}{\Sigma M_{pb}^*} > 1.0 \quad (E3-1)$$

Where Σ M<sub>pc</sub><sup>\*</sup> = 3,463 kip-in  
 Σ M<sub>pb</sub><sup>\*</sup> = 2,041 kip-in      0.589363

=>  $\frac{\Sigma M_{pc}^*}{\Sigma M_{pb}^*} = 1.70$  **OK, > 1.0**

**Strong Column - Weak Beam Criteria Satisfied!**

**9.7a. Braced Connections**  
 AISC 341-10 Section E3.4c      Equation E3-1  
 Column flanges at beam-to-column connections require lateral bracing only at the level of the top flanges of the beams, when the webs of the beams and column are co-planar, and a column is shown to remain elastic outside of the panel zone. It shall be permitted to assume that the column remains elastic when the ratio calculated using Equation 9-3 is greater than 2.0.

When a column cannot be shown to remain elastic outside of the panel zone, the following requirements shall apply:

- (1) The column flanges shall be laterally braced at the levels of both the top and bottom beam flanges. Lateral bracing shall be either direct or indirect.
- (2) Each column-flange lateral brace shall be designed for a required strength that is equal to 2 percent of the available beam flange strength  $F_y b_f t_{bf}$  (LRFD) or  $F_y b_f t_{bf} / 1.5$  (ASD), as appropriate.

**4.4 Column Bracing Requirements (AISC 341-10 Section E3.4c)**

a) **Left Beam - Required Column Brace strength**

$$F_{cb1} = 0.02 F_y b_{f1} t_{f1} \quad (E3.1)$$

where F<sub>y</sub> = 50 ksi  
 b<sub>f1</sub> = 5.81 inches  
 t<sub>f1</sub> = 0.51 inches

F <sub>cb1</sub> = 2.96 kips
------------------------------

b) **Right Beam - Required Column Brace strength (Not Used!)**

$$F_{cb2} = 0.02 F_y b_{f2} t_{f2} \quad (E3.1)$$

where F<sub>y</sub> = ksi  
 b<sub>f2</sub> = inches  
 t<sub>f2</sub> = inches

F <sub>cb2</sub> = kips
-------------------------

=> **Column-Beam Moment Ratio ≤ 2.0, thus Column will NOT remain Elastic; Column flanges to be braced at the level of the Top and Bottom of Beam flanges.**

The connection configuration must comply with the requirements of the prequalified connection:

**5. Beam to Column Connections**

a) Beam Flange-to-Column Flange Connection (AISC 341-10 Section E3.4.6a, AISC 358-10 Section 5.5)  
 Note: The connection configuration must comply with requirements for Demand Critical Welds in Section A.3.4b:

**Use a Complete-Joint-Penetration Groove Weld to connect the Beam flanges to the Column flange. The weld-access-hole geometry must comply with Specification Section J1.6. The welds must also be considered Demand Critical per Section A.3.4b.**

b) Beam Web-to-Column Flange Connection (AISC 341-10 Section E3.4.6a, AISC 358-10 Section 5.6)

Note: A single plate shear connection shall extend between weld access holes.  
**With the single plate as backing (not shown, Min 3/8" Plate), use a Complete-Joint-Penetration Groove Weld to connect the Beam webs to the Column flange.**

**6. Misc Column Checks**

**6.1 Panel Zone Thickness Check (AISC 341-10 Section E3.6(2))**

$$t_z \geq (d_z + W_z)/90 \quad (E3-7) \quad \text{for } t_z = t_{wc} = 0.57 \text{ in}$$

Where d<sub>z</sub> = max(d<sub>1</sub> - 2 t<sub>f1</sub>, d<sub>2</sub> - 2 t<sub>f2</sub>)      and d<sub>1</sub> = 10.50 inches  
 t<sub>f1</sub> = 0.51 inches  
 d<sub>2</sub> = 0.00 inches  
 t<sub>f2</sub> = 0.00 inches

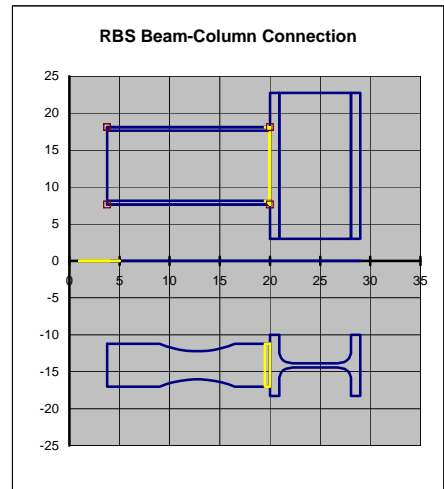
d <sub>z</sub> = 9.48 inches
------------------------------

W<sub>z</sub> = d<sub>c</sub> - 2 t<sub>c</sub>      and d<sub>c</sub> = 9.00 inches  
 t<sub>c</sub> = 0.94 inches

W <sub>z</sub> = 7.13 inches
------------------------------

(d<sub>z</sub> + W<sub>z</sub>)/90 = 0.18 in (Minimum panel zone thickness)

**OK, Column Web thickness is adequate**



**Quick Check:**  
 Use AISC 341-10 **Table 4-2** for W<sub>z</sub>/90 and d<sub>z</sub>/90 (W<sub>z</sub>/90 value for beams) values.

**SPECIAL MOMENT FRAME DESIGN BEAM - COLUMN CONNECTION DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : **N-S** Connection ID: **JT-1**  
 Floor Level : **1** Gridline: **10**  
 N<sub>s</sub> : **3** (Total Number of Stories)

**6.2 Column Panel Zone Shear Check (AISC 360-10 Section J10.6)**

**Note:** V<sub>u</sub> = 190 kips (Required shear strength in panel zone)

(i) For P<sub>r</sub> ≤ 0.75 P<sub>c</sub>

$$R_n = 0.60 F_y d_c t_w \left( 1 + \frac{3 b_{cf} t_{cf}^2}{d_b d_c t_w} \right) \quad (J10-11)$$

(ii) For P<sub>r</sub> > 0.75 P<sub>c</sub>

$$R_n = 0.60 F_y d_c t_w \left( 1 + \frac{3 b_{cf} t_{cf}^2}{d_b d_c t_w} \right) \left( 1.9 - \frac{1.2 P_r}{P_c} \right) \quad (J10-12)$$

**Quick Check:**

Use AISC 341-10 **Table 4-2** Panel Zone for 0.75 P<sub>y</sub>. φ R<sub>n</sub> = φ R<sub>v1</sub> + R<sub>v2</sub>/d<sub>b</sub>.

φ R<sub>n</sub> = 216 kips

**OK, R<sub>n</sub> > V<sub>u</sub> = 190 kips;**  
**Doubler Plates are not needed.**

Where P<sub>r</sub> = P<sub>u</sub> = 12 kips (maximum axial load)  
 P<sub>c</sub> = P<sub>y</sub> = 985 kips and F<sub>y</sub> = 50.00 Ksi  
 A<sub>g</sub> = 19.70 in<sup>2</sup>  
 0.75 P<sub>c</sub> = 0.75 P<sub>y</sub> = 739 kips **Note: EQ J10-11 Governs!**  
 F<sub>y</sub> = 50 ksi  
 φ<sub>v</sub> = 1.00 (AISC 341-10 Section E3.6e.(1) )  
 d<sub>c</sub> = 9.00 in  
 t<sub>wc</sub> = 0.57 in  
 b<sub>fc</sub> = 8.28 in  
 t<sub>fc</sub> = 0.94 in  
 d<sub>b</sub> = max(d<sub>1</sub>, d<sub>2</sub>) = 10.50 in for d<sub>1</sub> = 10.50 in  
 d<sub>2</sub> = 0.00 in

**6.3 Required Thickness of Doubler Plate**

a) Required Overall Thickness

$$t_{req} = t_{wc} \frac{V_u}{\phi R_n} \quad \text{Where } t_{wc} = 0.57 \text{ in}$$

$$V_u = 190 \text{ kips}$$

$$\phi R_n = 216 \text{ kips}$$

t<sub>req</sub> = 0.50 in

b) Required Plate Thickness

$$t_{pl} = \frac{t_{req} - t_{wc}}{2} \quad \text{Where } t_{req} = 0.50 \text{ in}$$

$$t_{wc} = 0.57 \text{ in}$$

t<sub>pl</sub> = -0.03 in

**Doubler Plates not Needed.**

Note: Extend Doubler Plates 6" above and below beams, if needed.

**7. Continuity Plate Requirements**

**Note:** Previous Source was AISC 358-10; now references AISC 341-10 Section E3.6f.

**7.1 Continuity Plate Requirements (AISC 358 Section 2.4.4 => AISC 341-10 Section E3.6f)**

**Note:** t<sub>fc</sub> = 0.94 inches

a) **Left** Beam

i) AISC 341-10 Section E3.6f Eq. E3-8

$$t_{cf} = 0.4 \sqrt{1.8 b_{bf} t_{bf} \frac{F_{yb} R_{yb}}{F_{yc} R_{yc}}} \quad (E3-8)$$

t<sub>cf</sub> = 0.92 in

Where b<sub>bf</sub> = b<sub>t1</sub> = 5.81 in  
 t<sub>bf</sub> = t<sub>t1</sub> = 0.51 in  
 F<sub>yb</sub> = 50 Ksi  
 R<sub>yb</sub> = 1.10  
 F<sub>yc</sub> = 50 Ksi  
 R<sub>yc</sub> = 1.10

ii) AISC 341-10 Section E3.6f Eq. E3-9

$$t_{cf} = b_{t1}/6 \quad (E3-9) \quad \text{Where } b_{t1} = 5.81 \text{ in}$$

t<sub>cf</sub> = 0.97 in

=> t<sub>cf</sub> = 0.97 in  
 < t<sub>fc</sub> = 0.94 in  
**Need Continuity Plates!**

b) **Right** Beam (Not Used!)

i) AISC 341-10 Section E3.6f Eq. E3-8

$$t_{cf} = 0.4 \sqrt{1.8 b_{bf} t_{bf} \frac{F_{yb} R_{yb}}{F_{yc} R_{yc}}} \quad (E3-8)$$

t<sub>cf</sub> = in

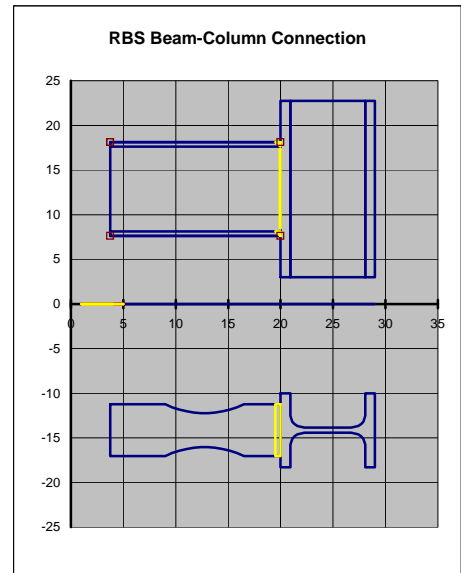
Where b<sub>bf</sub> = b<sub>t2</sub> = in  
 t<sub>bf</sub> = t<sub>t2</sub> = in  
 F<sub>yb</sub> = Ksi  
 R<sub>yb</sub> =  
 F<sub>yc</sub> = Ksi  
 R<sub>yc</sub> =

ii) AISC 341-10 Section E3.6f Eq. E3-9

$$t_{cf} = b_{t2}/6 \quad (E3-9) \quad \text{Where } b_{t2} = \text{in}$$

t<sub>cf</sub> = in

=> t<sub>cf</sub> = in



**SPECIAL MOMENT FRAME DESIGN BEAM - COLUMN CONNECTION DESIGN**  
 2010 AISC SEISMIC DESIGN MANUAL PROVISIONS - SMRF 1 AT GRIDLINE 1 - FIXED BASE CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

Loading Direction : **N-S** Connection ID: **JT-1**  
 Floor Level : **1** Gridline: **10**  
 N<sub>s</sub> : **3** (Total Number of Stories)

**7.2 Required Stiffener Plates - Left Beam**

**Notes:**

1. Use of full height stiffener plates means that most failure modes (J10.1 thru J10.7) do not have to be checked, except for Web Local Yielding (J10.2) and Web Compression Buckling (J10.5).
2. Web Compression Buckling applies only to compressive forces on both flanges, so does not apply.

a) Required Stiffener Plate Area (AISC 360-10 Section J10.2)

$$A_{st} = \frac{P_{bf} - F_{yc} t_{wc} (t_{f1} + 2.5 K_c)}{F_{yc}} \quad \text{(J10-3)} \quad \text{Where } P_{bf} = b_{f1} t_{f1} F_{y1}$$

$$P_{bf} = 148 \text{ kips}$$

F<sub>yc</sub> = 50 Ksi  
 t<sub>wc</sub> = 0.57 in  
 t<sub>f1</sub> = 0.51 in  
 K<sub>c</sub> = 1.33 in

and b<sub>f1</sub> = 5.81 in  
 t<sub>f1</sub> = 0.51 in  
 F<sub>y1</sub> = 50 Ksi

$$A_{st} = 0.78 \text{ in}^2 \text{ (Required Stiffener Plate Area)}$$

b) Required Continuity Plate Thickness (AISC 341-10 Section E3.6f (2))

$$t_{cp} = 0.5 t_b \quad \text{(One-sided connections)} \quad \text{Where } t_{f1} = 0.51 \text{ in}$$

$$t_{cp} = \max(t_{f1}, t_{f2}) \quad \text{(Two-sided connections)}$$

$$t_{cp} = 0.63 \text{ in}$$

c) Additional Stiffener Requirements for Concentrated Forces (AISC 360-10 Section J10.8, UON)

i) Plate Geometry (Section J10.8 (1) and (2)):

$$t_{min} = t_c / 2 \quad \text{Where } t_c = 0.94 \text{ in}$$

$$= 0.468 \text{ in}$$

NG, < t<sub>cp</sub> = 0.63

$$t_{min} = 0.63 \text{ in}$$

$$b_{min} = b_{f1} / 3 - t_{wc} / 2 \quad \text{Where } b_{f1} = 5.81 \text{ in}$$

$$t_{wc} = 0.57 \text{ in}$$

$$b_{min} = 1.65 \text{ in}$$

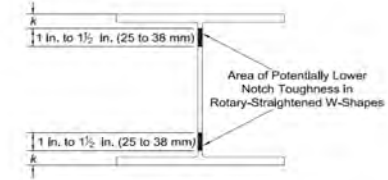
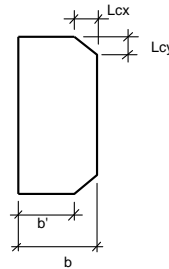


Fig. C-110.6. Representative "k-area" of a wide-flange shape.

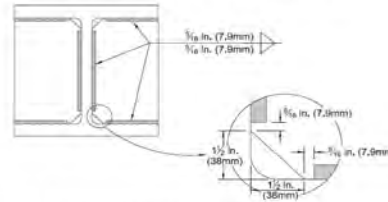


Fig. C-110.7. Recommended placement of stiffener fillet welds to avoid contact with "k-area."

ii) Check end distance (Section J10.8 (3)):

$$b_{max} = 0.50 (b_c - t_{wc}) \quad \text{and } b_c = 8.28 \text{ in}$$

$$t_{wc} = 0.57 \text{ in}$$

$$b_{max} = 3.86 \text{ in}$$

iii) Clip Dimensions (AISC 358 Section 3.6)

$$L_{cx} = K_1 + 0.50" \quad \text{where } K_1 = 0.94 \text{ inches}$$

$$L_{cx} = 1.44 \text{ in}$$

$$L_{cy} = K + 1.50" \quad \text{where } K = 1.33 \text{ inches}$$

$$L_{cy} = 2.83 \text{ in}$$

iv) Required Plate Dimensions

$$A_{req} = n_p (b' t) \quad \text{Where } A_{req} = A_{st} = 0.78 \text{ in}^2$$

$$b'_{req} = A_{req} / (n_p t) \quad n_p = 2 \text{ Number of plates}$$

$$t = t_{min} = 0.63 \text{ in}$$

$$b'_{req} = 0.62 \text{ in}$$

$$b_{req} = b'_{req} + L_{cx} \quad \text{Where } b'_{req} = 0.62 \text{ in}$$

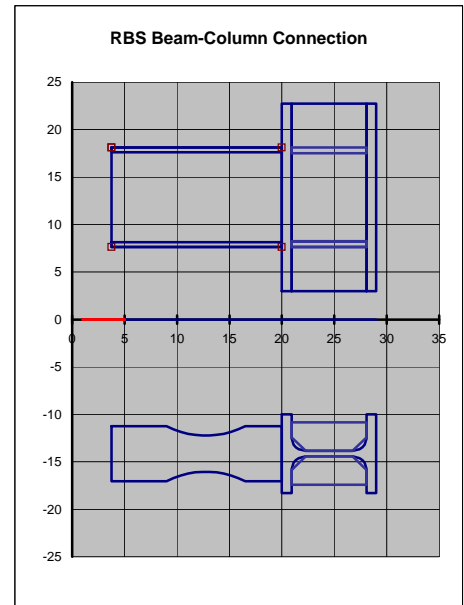
$$L_{cx} = 1.44 \text{ in}$$

$$b_{req} = 2.06 \text{ in}$$

$$\Rightarrow \text{Use } b_{req} = 3.00 \text{ in}$$

OK, > b<sub>min</sub> = 1.65 in  
 OK, < b<sub>max</sub> = 3.86 in

Use 3.00 in x 0.63 in Continuity Plates for Left Beam





**BASE PLATE DESIGN -  
DESIGN FOR LARGE MOMENTS**

**COLUMN BASE PLATE WITH LARGE MOMENT - SMRF 1 AT GRIDLINE I**  
**LRFD APPROACH - AISC 360-10 AND STEEL DESIGN GUIDE 1**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**1. Parameters**

Column: **W8x67** => d = 9.00 inches (Wide Flange - Depth)  
 b<sub>f</sub> = 8.28 inches (Wide Flange - Width)  
 t<sub>f</sub> = 0.94 inches (Wide Flange - Thickness)  
 Z<sub>x</sub> = 70.1 in<sup>3</sup> (Wide Flange - Plastic Section)  
 A = 19.70 in<sup>2</sup> (Wide Flange - Area)  
 F<sub>y</sub> = **50** Ksi

Bolts: D<sub>B</sub> = **1.00** inches (Bolt Diameter)  
 h<sub>ef</sub> = **24.00** inches (Bolt Embedment w/ Washer)  
 N<sub>BL</sub> = **4** (Number of Bolts - Longitudinal - Max 7)  
 N<sub>BT</sub> = **4** ( " - Transverse - " )  
 Grade of Bolt = **55** Ksi (Grade 36, 55, or 105)  
 d<sub>e</sub> = **2.00** inches (distance from bolt C<sub>L</sub> to edge of Plate)

AISC 360-10 Table 14-2 Requirements :

Max Hole Diameter = 1.81 inches  
 Min Washer Size = 3.00 inches  
 Min Washer Thickness = 0.38 inches

Loading :

S<sub>DS</sub> = **1.09** g's (Site Design Coefficient - Short Period)  
 P<sub>U</sub> = **15** Kips (+ is Compression, - is Tension)  
 M<sub>U</sub> = 115% of RBS Beam Flexural Capacity Where M<sub>pr</sub> = **1,321** kip-in

**M<sub>U</sub> = 1,519 Kip-in**

Base Plate Dimensions:

Trial Size :

N = **16.00** inches (Base Plate - Length)  
**OK**  
 B = **18.00** inches (Base Plate - Width)  
**OK**  
 A<sub>2</sub> = **288** in<sup>2</sup> (Area of Concrete Support)

Material Properties:

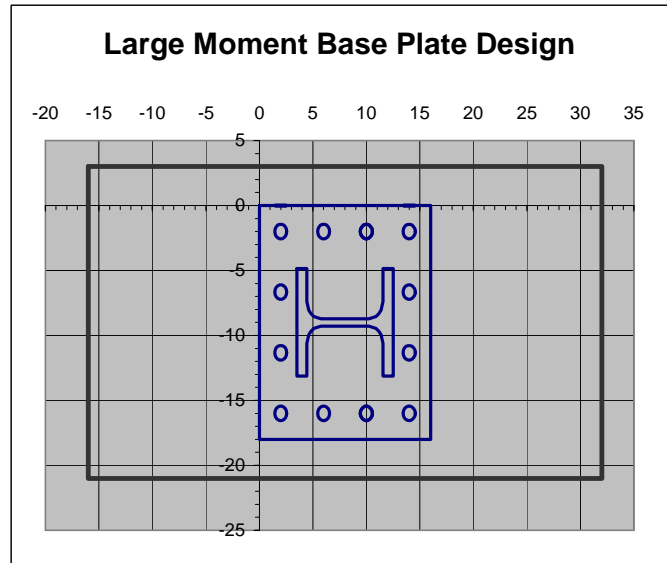
f<sub>y</sub> = **50.00** Ksi  
 f'<sub>c</sub> = **3.25** Ksi  
 Ψ<sub>3</sub> = **1.25** (ACI 318-08 Appendix D5.2.6 ;  
 Cast in place Anchors,  
 1.25 for uncracked concrete,  
 1.0 Otherwise)

Foundation Dimensions:

L<sub>F</sub> = **4.00** feet (foundation Length)  
 W<sub>F</sub> = **2.00** feet (foundation Width)  
 H<sub>F</sub> = **3.00** feet (foundation Depth)  
**OK**

Design Parameters :

φ<sub>b</sub> = **0.65** (AISC 360-10 Section J8; Bearing)  
 φ<sub>cb</sub> = **0.70** (ACI 318-08 Appendix D.4.4 ; Concrete Breakout Strength - Pullout or Pryout)  
 φ<sub>EQ</sub> = **0.75** (ACI 318-08 Appendix D.3.3 ; Anchor capacities reduced by 0.75 in Seismic Regions)



Thickness (t <sub>p</sub> )	Plate Availability
t <sub>p</sub> ≤ 4 in.	ASTM A36 <sup>(a)</sup> ASTM A572 Gr 42 or 50 ASTM A588 Gr 42 or 50
4 in. < t <sub>p</sub> ≤ 6 in.	ASTM A36 <sup>(a)</sup> ASTM A572 Gr 42 ASTM A588 Gr 42
t <sub>p</sub> > 6 in.	ASTM A36

<sup>(a)</sup> Preferred material specification

**COLUMN BASE PLATE WITH LARGE MOMENT - SMRF 1 AT GRIDLINE 1  
 LRFD APPROACH - AISC 360-10 AND STEEL DESIGN GUIDE 1  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**2. Loading Eccentricities**

a) Eccentricity of Resultant Force

$$e = M_U / P_U$$

$M_U = 1,519 \text{ Kip-in}$   
 $P_U = 15 \text{ Kips}$

$e = 101.24 \text{ inches}$

b) Ultimate Concrete Bearing Stress (AISC SDG-1 Section 3.1.1)

$$f_U = 0.85 \phi_b f'_c (A_1/A_2)^{0.50} \leq 1.7 f'_c$$

Where  $\phi_b = 0.65$  (AISC 360-10 Section J8)

$$A_1 = N B \quad \text{for } N = 16.00 \text{ inches (P}_L \text{ Length)}$$

$$B = 18.00 \text{ inches (P}_L \text{ Width)}$$

$A_1 = 288 \text{ in}^2$

$$A_2 = 288 \text{ in}^2 \text{ (Area of Concrete Support)}$$

$$f'_c = 3.25 \text{ Ksi} \Rightarrow 1.7 f'_c = 5.53 \text{ Ksi (Max Bearing Stress)}$$

$f_U = 1.80 \text{ Ksi}$

c) Determination of Critical Eccentricity (AISC SDG-1 Section 3.1.1)

$$e_{crit} = N/2 - P_U / 2q_{max} \quad (3.3.5) \quad \text{Where } N = 16.00 \text{ inches (P}_L \text{ Length)}$$

$$P_U = 15 \text{ Kips}$$

$$q_{max} = f_U B \quad (3.3.1) \quad \text{for } f_U = 1.80 \text{ Ksi}$$

$$B = 18.00 \text{ inches (P}_L \text{ Width)}$$

$q_{max} = 32.32 \text{ Kips/in}$

$e_{crit} = 7.77 \text{ inches}$

**OK  $\leq e$ , Base Plate w/ Large Moment**

d) Check if Real Solution exists (AISC SDG-1 Section 3.4.1)

$$\left(f + \frac{N}{2}\right)^2 \geq \frac{2P_r(e+f)}{q_{max}} \quad (3.4.4)$$

$$\text{Where } f = N/2 - d_e$$

$$\text{Where } N = 16.00 \text{ inches (P}_L \text{ Length)}$$

$$d_e = 2.00 \text{ inches (distance from bolt } C_L \text{ to edge of Plate)}$$

$f = 6.00 \text{ inches}$

$$N = 16.00 \text{ inches (P}_L \text{ Length)}$$

$$P_r = P_U = 15 \text{ Kips}$$

$$e = 101.24 \text{ inches}$$

$$q_{max} = 32.32 \text{ Kips/in}$$

Left Term :

$$\{f + N/2\}^2 = 196$$

Right Term :

$$2 P_U (e + f) / q_{max} = 100$$

**OK, Base Plate Dimensions Adequate**

e) Plate Bearing Length

$$Y = \left(f + \frac{N}{2}\right) \pm \sqrt{\left(f + \frac{N}{2}\right)^2 - \frac{2P_r(e+f)}{q_{max}}} \quad (3.4.3)$$

$$\text{Where } f = 6.00 \text{ inches}$$

$$N = 16.00 \text{ inches (P}_L \text{ Length)}$$

$$P_r = P_U = 15 \text{ Kips}$$

$$e = 101.24 \text{ inches}$$

$$q_{max} = 32.32 \text{ Kips/in}$$

$$Y = 14.00 \text{ +/- } 9.82$$

$$= \text{MIN}(23.82, 4.18)$$

$Y = 4.18 \text{ inches}$

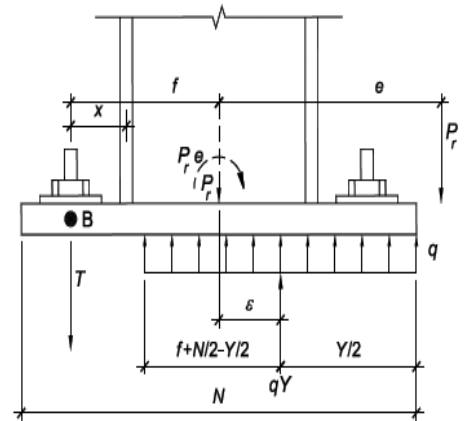
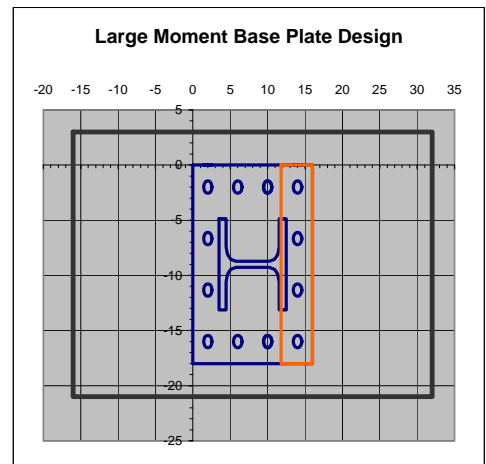


Figure 3.4.1. Base plate with large moment.



**COLUMN BASE PLATE WITH LARGE MOMENT - SMRF 1 AT GRIDLINE 1**  
**LRFD APPROACH - AISC 360-10 AND STEEL DESIGN GUIDE 1**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**3. Determination of Minimum Plate Thickness**

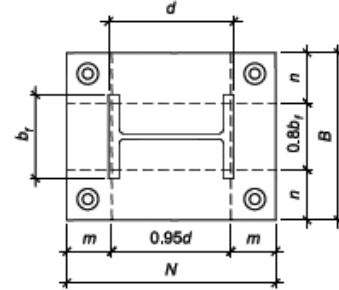
a) Critical Base Plate Cantilever Dimensions (SDG-1 3.1.2)

$m = 0.50 (N - 0.95 d)$  Where  $N = 16.00$  inches ( $P_L$  Length)  
 $d = 9.00$  inches (Wide Flange - Depth)

$m = 3.73$  inches

$n = 0.50 (B - 0.80 b_f)$  Where  $B = 18.00$  inches (Base Plate - Width)  
 $b_f = 8.28$  inches (Wide Flange - Width)

$n = 5.69$  inches



b) Required Base Plate Thickness - Yielding Limit at **Bearing** Interface (SDG-1 3.4.2)

**Note:** Per AISC Steel Design Guide 1 (SDG-1) 3.3.2, when n is larger than m, n may be substituted for m in the equations below:

For  $Y \geq m$ :  $t_p = 1.5 m' (f_p / f_y)^{0.5}$  (3.3.14a) Where  $m' = \text{MAX}(m, n)$  for  $m' = 3.73$  inches  
 $n = 5.69$  inches

$m' = 5.69$  inches

$f_p = f_u = 1.80$  Ksi (Bearing Stress at Limiting Value)  
 $f_y = 50.00$  Ksi

$t_p = \text{NA}$  inches

For  $Y < m$ :  $t_p = 2.11 [ (f_p Y (m' - Y/2)) / f_y ]^{0.5}$  (3.3.14b) Where  $m' = 5.69$  inches  
 $f_p = 1.80$  Ksi  
 $Y = 4.18$  inches  
 $f_y = 50.00$  Ksi

$t_p = 1.55$  inches **(Controls!)**

c) Required Base Plate Thickness - Yielding Limit at **Tension** Interface (SDG-1 3.4.3)

$t_p = 2.11 [ (T_U x) / (B f_y) ]^{0.5}$  (3.4.7a) Where  $T_U = q_{\text{max}} Y - P_U$  for  $q_{\text{max}} = 32.32$  Kips/in  
 $Y = 4.18$  inches  
 $P_U = 15$  Kips

$T_U = 120$  Kips

$x = f - d/2 + t_f/2$  for  $f = 6.00$  inches  
 $d = 9.00$   
 $t_f = 0.94$  inches (Wide Flange - Thickness)

$x = 1.97$  inches

$B = 18.00$  inches (Base Plate - Width)  
 $f_y = 50.00$  Ksi

$t_p = 1.08$  inches

132.708

d) Governing Base Plate Thickness Requirement

$t_p = 1.55$  inches (Yielding Limit at **Bearing** Interface) = >  $t_p = 1.55$  inches  
 $= 1.08$  inches ( " Limit at **Tension** Interface)

**Use a Base Plate 1.63 inch Thick x 18.00 inch Wide x 16.00 inch Long**

**BASE PLATE DESIGN -  
ANCHOR ROD DESIGN FOR TENSION**

**DESIGN OF BASE PLATE ANCHORAGE IN CONCRETE - SMRF 3 AT GRIDLINE 10**  
 ACI 318-11 APPENDIX D REQUIREMENTS - ANCHORING IN CONCRETE  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**1. Parameters**

Column: **W8x67** => d = 9.00 inches (Wide Flange - Depth)  
 b<sub>f</sub> = 8.28 inches (Wide Flange - Width)  
 t<sub>f</sub> = 0.94 inches (Wide Flange - Thickness)

Bolts: D<sub>b</sub> = **1.00** inches (Bolt Diameter)  
 h<sub>ef</sub> = **24.00** inches (Bolt Embedment w/ Washer)

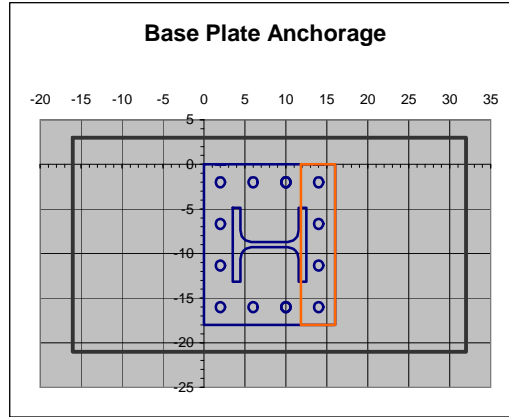
N<sub>BL</sub> = **4** (Number of Bolts - Longitudinal - Max 7)  
 N<sub>BT</sub> = **4** ( " - Transverse - " )

Grade of Bolt = **55** Ksi (Grade 36, 55, or 105)  
 d<sub>o</sub> = **2.00** inches (distance from bolt C<sub>L</sub> to edge of Plate)

**AISC 360-10 Table 14-2 Requirements :**

Max Hole Diameter = **1.81** inches  
 Min Washer Size = **3.00** inches  
 Min Washer Thickness = **0.38** inches

Loading : T<sub>U</sub> = **120** Kips (from required Base Plate Thickness Calcs)  
 S<sub>DS</sub> = **1.09** g's (Site Design Coefficient - Short Period)  
 P<sub>U</sub> = **15.00** Kips (+ is Compression, - is Tension)  
 M<sub>U</sub> = **1,519** Kip-in



**Base Plate Dimensions:**

Plate Size :  
 N = **16.00** inches (Base Plate - Length)  
**OK**  
 B = **18.00** inches (Base Plate - Width)  
**OK**  
 A<sub>2</sub> = **288** in<sup>2</sup> (Area of Concrete Support)

**Material Properties:**

f<sub>y</sub> = **50.00** Ksi  
 f<sub>c</sub> = **3.25** Ksi  
 Ψ<sub>3</sub> = **1.25** (ACI 318-08 Appendix D5.2.6 ;  
 Cast in place Anchors,  
 1.25 for uncracked concrete,  
 1.0 Otherwise)

Thickness (t <sub>p</sub> )	Plate Availability
t <sub>p</sub> ≤ 4 in.	ASTM A36 <sup>®</sup> ASTM A572 Gr 42 or 50 ASTM A588 Gr 42 or 50
4 in. < t <sub>p</sub> ≤ 6 in.	ASTM A36 <sup>®</sup> ASTM A572 Gr 42 ASTM A588 Gr 42
t <sub>p</sub> > 6 in.	ASTM A36

<sup>®</sup> Preferred material specification

**Foundation Dimensions:**

L<sub>F</sub> = **17.50** feet (foundation Length)  
 W<sub>F</sub> = **2.00** feet (foundation Width)  
 H<sub>F</sub> = **3.00** feet (foundation Depth)  
**OK**

**Design Parameters :**

Concrete :

Steel Anchor in Concrete:

**Capacity Factors :**

Φ<sub>EC</sub> = **0.75** (Steel Anchor - Seismic Region - ACI Section D.3.3.3)  
 Φ<sub>SA,T</sub> = **0.75** (Steel Anchor - Tension, Ductile Steel Element - ACI D.4.4)  
 Φ<sub>SA,CB</sub> = **0.70** (Steel Anchor - Concrete Condition B - ACI D.4.4)

Note: Supplementary reinforcement not provided for pullout and pryout strength.

**Material Properties :**

f<sub>c</sub> = **3.25** Ksi  
 f<sub>y</sub> = **60.00** Ksi

**Material Properties :**

f<sub>yt</sub> = **60.00** Ksi (PCA Notes Table 34-1 - ASTM A307)

**DESIGN OF BASE PLATE ANCHORAGE IN CONCRETE - SMRF 3 AT GRIDLINE 10**  
 ACI 318-11 APPENDIX D REQUIREMENTS - ANCHORING IN CONCRETE  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**2. Adequacy of Footing - Anchor Pull-out in New Footing**

$T_u = 120$  Kips on  $N = 4$  (Number of Bolts - Transverse - Max 7)

a) Bolt Design Strength - Tension (ACI 318-08 D3.3.3, D4.4, D5.1)

$\phi_{EQ} \phi_{sa,t} N_{sa} = \phi_{EQ} \phi_{sa,t} \pi A_{se,N} f_{uta}$  (D-3)

Where  $\phi_{EQ} = 0.75$  (Steel Anchor - Seismic Region - ACI Section D.3.3.3)

$\phi_{sa,t} = 0.75$  (Steel Anchor - Tension, Ductile Steel Element - ACI Section D.4.4)

$A_{se,N} = \pi t_{HD}^2$  for  $t_{HD} = 1.00$  inches (Diameter of Holdown Anchor)

$A_{se,N} = 0.79$  in<sup>2</sup>

$f_{uta} = \text{Min}(1.6 f_{ya}, 125)$  for  $f_{ya} = 60.00$  Table 34-1 - ASTM A307

$f_{uta} = 96.00$  Ksi

$\phi_{EQ} \phi_{sa,t} N_{sa} = 42$  Kips (Bolt Design Strength - Tension)

b) Concrete Breakout Strength - Tension (ACI 318-08 Section D5.2)

Note: Condition B is assumed per Section D4.4, where Supplementary reinforcement is not present in failure prism.

$\phi_{EQ} \phi_{sa,cb} N_{cb} = \phi_{EQ} \phi_{sa,cb} N_b A_{NC} / A_{NCO} \Psi_1 \Psi_2 \Psi_3 \Psi_4$  (D-4)

Where  $\phi_{EQ} = 0.75$  (Steel Anchor - Seismic Region - ACI Section D.3.3.3)

$\phi_{sa,cb} = 0.70$  (Steel Anchor - Concrete Breakout Category 2 - ACI D.4.4)

$N_b$  = Basic concrete Break-out Strength of a single anchor in Tension in Cracked Concrete (ACI D.5.2.2)

$= K_C f'_c{}^{0.5} H_{ef}{}^{1.5} \lambda$  and  $K_C = 24$  Cast-in Anchors (D5.2.2)

$f'_c = 3.25$  Ksi  
 $= 3,250$  Psi

$H_{ef} = 24.00$  inches (Embedment depth of Holdown Anchor)

$\lambda = 1.00$  (1.0 for NWC, 0.75 for LWCC)

Note: NWC - Normal Weight Concrete Assumed

$N_b = 160.87$  Kips

$A_{NC}$  = Projected Concrete Failure Area - Actual (ACI D5.2.1)

$= (C_{a1x} + S_x + C_{a2x}) (C_{a1y} + S_y + C_{a2y})$

for  $C_{a1x} = C_{a2x} = (L_F - N)/2 + d_o < 1.5 h_{ef}$

Where  $L_F = 210.00$  inches (foundation Length)

$N = 16.00$  inches (Base Plate - Length)

$d_o = 2.00$  inches (distance from bolt  $C_L$  to edge of Plate)

$1.5 h_{ef} = 36.00$  inches

$C_{a1x} = 36.00$  inches

$S_x = N - 2 d_o < 3.0 h_{ef}$

Where  $N = 16.00$  inches (Base Plate - Length)

$d_o = 2.00$  inches (distance from bolt  $C_L$  to edge of Plate)

$3.0 h_{ef} = 72.00$  inches

$S_x = 12.00$  inches

$C_{a1y} = C_{a2y} = (W_F - B)/2 + d_o < 1.5 h_{ef}$

Where  $W_F = 24.00$  feet (foundation Width)

$B = 18.00$  inches (Base Plate - Width)

$d_o = 2.00$  inches (distance from bolt  $C_L$  to edge of Plate)

$1.5 h_{ef} = 36.00$  inches

$C_{a1y} = 5.00$  inches

$S_y = B - 2 d_o < 3.0 h_{ef}$

Where  $B = 18.00$  inches (Base Plate - Width)

$d_o = 2.00$  inches (distance from bolt  $C_L$  to edge of Plate)

$3.0 h_{ef} = 72.00$  inches

$S_y = 14.00$  inches

$A_{NC} = 2,016$  in<sup>2</sup>

$A_{NCO}$  = Projected Concrete Failure Area - Ideal (ACI D5.2.1)

$= 9 h_{ef}^2$  (D-6) and  $H_{ef} = 24.00$  inches (Embedment depth of Holdown Anchor)

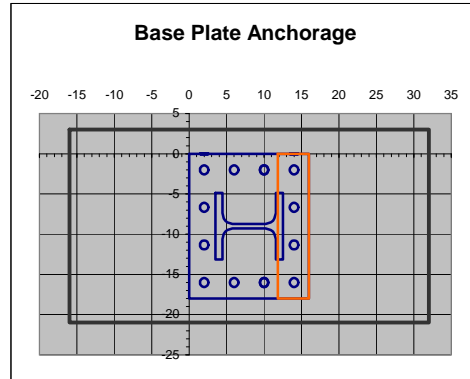
$A_{NCO} = 5,184$  in<sup>2</sup>

$\Psi_1 = \Psi_{ec,N}$  = Modification for Anchor Groups loaded Eccentrically in Tension (ACI D.5.2.4)

$= 1 / (1 + 2 e'_N / 3 H_{ef})$  and  $e'_N = 0$  (All anchors in group loaded in Tension - No eccentricity)

$H_{ef} = 24.00$  inches (Embedment depth of Holdown Anchor)

$\Psi_1 = \Psi_{ec,N} = 1.0$  Modification for Anchor Groups loaded Eccentrically in Tension (ACI D.5.2.4)



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$\Psi_2 = \Psi_{ed,N}$  = Modification for Edge Effects (ACI D.5.2.5)  
 = 1.0 if  $C_{a,min} \geq 1.5 H_{ef}$  Where  $C_{a1} = 5.00$  inches (Distance from Wall CL to Left Edge of Existing Footing Wall)  
 =  $0.7 + 0.3 C_{a,min} / (1.5 H_{ef})$  if  $C_{a,min} < 1.5 H_{ef}$   $C_{a2} = 5.00$  inches (Distance from Wall CL to Right Edge of Existing Footing Wall)  
 $C_{a,min} = 5.00$  inches  
 $1.5 H_{ef} = 36.00$  inches

$\Psi_1 = \Psi_{ed,N} = 0.74$  Modification for Edge Effects (ACI D.5.2.5)

$\Psi_3 = \Psi_{c,N}$  = Modification for Uncracked Concrete (ACI D.5.2.6)  
 = 1.25 Note: Cracking is not expected at Service Load levels  
 $\Psi_2 = \Psi_{c,N} = 1.25$  Modification for Uncracked Concrete (ACI D.5.2.6)

$\Psi_4 = \Psi_{cp,N}$  = Modification for Post-Installed Anchors (ACI D.5.2.7)  
 = 1.0 for Cast-in Anchors  
 $\Psi_3 = \Psi_{cp,N} = 1.00$  Modification for Post-Installed Anchors (ACI D.5.2.7)

$\phi_{EQ} \phi_{sa,cb} N_{cb} = 30.45$  Kips (Concrete Break-out Strength - Tension)

c) Pull-out Strength of Anchor - Tension (ACI 318-08 Section D5.3)

Note: Condition B is assumed per Section D4.4, where Supplementary reinforcement is not present in failure prism.

$\phi_{EQ} \phi_{sa,po} N_p = \phi_{EQ} \phi_{sa,po} N_p \Psi_4$  (D-14)

Where  $\phi_{EQ} = 0.75$  (Steel Anchor - Seismic Region - ACI Section D.3.3.3)

$\phi_{sa,po} = \phi_{sa,cb} = 0.70$  (Steel Anchor - Concrete Breakout/Pullout - ACI D.4.4)

$N_p$  = Pull-out Strength of a single anchor in Tension in Cracked Concrete (ACI D.5.3.4)

=  $8 A_{brg} f_c$  (D-15)

and  $A_{brg}$  = Bearing Area of Anchor Bolt, or Washer if provided

=  $L_{PL}^2$  for  $L_{PL} = 3.0$  inches (Min Washer Size - AISC 360-10 Table 14-2)

Note:  $D_B = 1.00$  inches (Bolt Diameter)

$A_{brg} = 9.00$  in<sup>2</sup> (Bearing Area of Anchor Bolt Washer)

$f_c = 3.25$  Ksi  
 = 3,250 Psi

$N_p = 234.0$  kips

$\Psi_4 = \Psi_{c,p}$  = Modification for Uncracked Concrete (ACI D.5.3.6)  
 = 1.4 Note: Cracking is not expected at Service Load levels

$\Psi_4 = \Psi_{c,p} = 1.4$  Modification for Uncracked Concrete (ACI D.5.3.6)

$\phi_{EQ} \phi_{sa,po} N_p = 172.0$  Kips (Concrete Pull-out Strength - Tension)

d) Concrete Side-face Blowout Strength of Anchor - Tension (ACI 318-08 Section D5.4)

$\phi_{EQ} \phi_{sa,sf} N_p = \phi_{EQ} \phi_{sa,po} N_p$

Where  $\phi_{EQ} = 0.75$  (Steel Anchor - Seismic Region - ACI Section D.3.3.3)

$\phi_{sa,sf} = \phi_{sa,cb} = 0.70$  (Steel Anchor - Concrete Breakout/Pullout/Side Blowout - ACI D.4.4)

$N_p = 160 C_{a1} A_{brg}^{0.5} \lambda f_c^{0.5}$

Where  $C_{a1} = 5.00$  inches (Distance from Wall CL to Left Edge of Existing Footing Wall)

$C_{a2} = 5.00$  inches (Distance from Wall CL to Right Edge of Existing Footing Wall)

$C_{a,min} = 5.00$  inches

$A_{brg} = 9.00$  in<sup>2</sup> (Bearing Area of Anchor Bolt)

$\lambda = 1.00$  (1.0 for NWC, 0.75 for LWC)

Note: NWC - Normal Weight Concrete Assumed

$f_c = 3.25$  Ksi  
 = 3,250 Psi

$N_p = 136.8$  Kips

$\phi_{EQ} \phi_{sa,sf} N_p = 71.8$  Kips (Concrete Side-face Blowout Strength - Tension)

e) Limiting Governing Strength per Anchor - Tension Only

$T_{UC} = \text{Min} (\phi_{EQ} \phi_{sa,t} N_{sa}, \phi_{EQ} \phi_{sa,cb} N_{cb}, \phi_{EQ} \phi_{sa,po} N_p, \phi_{EQ} \phi_{sa,sf} N_p)$

Where  $\phi_{EQ} \phi_{sa,t} N_{sa} = 42.4$  Kips (Bolt Design Strength)

$\phi_{EQ} \phi_{sa,cb} N_{cb} = 30.4$  Kips (Concrete Break-out Strength)

$\phi_{EQ} \phi_{sa,po} N_p = 172.0$  Kips (Concrete Pull-out Strength)

$\phi_{EQ} \phi_{sa,sf} N_p = 71.8$  Kips (Concrete Side-face Blowout Strength)

$T_{UC} = 30.45$  Kips

f) Limiting Governing Strength of Anchor Group - Tension Only

$T_{UC} = n T_{UC}$  where  $n = 4$  (number of anchors in group)

$T_{UC} = 30.45$  Kips

$T_{UC} = 122$  Kips

Note:  $T_U = 120$  Kips on  $N = 4$  (Number of Bolts - Transverse - Max 7)

OK

Use 4 - 1.00" Diameter Bolts ea Side of Column Flange



BASE PLATE DESIGN -  
DESIGN FOR SHEAR

**COLUMN BASE PLATE DESIGN FOR SHEAR - SMRF 3 AT GRIDLINE 10**  
 LRFD APPROACH - AISC 360-10 AND STEEL DESIGN GUIDE 1  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**1. Parameters**

**Column:** W8x67 => d = 9.00 inches (Wide Flange - Depth)  
 b<sub>f</sub> = 8.28 inches (Wide Flange - Width)  
 t<sub>f</sub> = 0.94 inches (Wide Flange - Thickness)

**Bolts:** D<sub>b</sub> = 1.00 inches (Bolt Diameter)  
 N<sub>BL</sub> = 4 (Number of Bolts - Longitudinal)  
 N<sub>BT</sub> = 4 ( " - Transverse)  
 Grade of Bolt = 55 Ksi (Grade 36, 55, or 105)  
 d<sub>b</sub> = 2.00 inches (distance from bolt C<sub>L</sub> to edge of Plate)

**Loading:**

Note: Shear resistance is assumed to be **Parallel** to Column Axis, along Length of Base Plate.

S<sub>DS</sub> = 1.09 g's (Site Design Coefficient - Short Period)  
 V<sub>U</sub> = 5 Kips  
 P<sub>U</sub> = 15 Kips (+ is Compression, - is Tension)

**Base Plate Dimensions:**

N = 16.00 inches (Base Plate - Length)  
 B = 18.00 inches (Base Plate - Width)  
 t<sub>p</sub> = 1.63 inches (Base Plate - Thickness)

**Material Properties:**

f<sub>y</sub> = 36.00 Ksi  
 f'<sub>c</sub> = 4.00 Ksi

**Foundation Dimensions:**

L<sub>F</sub> = 4.00 feet (foundation Length)  
 W<sub>F</sub> = 2.00 feet (foundation Width)  
 H<sub>F</sub> = 3.00 feet (foundation Depth)

**Shear Lug Data:**

h<sub>lug</sub> = 3.75 in (Height of Lug plate)  
 t<sub>lug</sub> = 1.25 in (Thickness of Lug Plate)  
 W<sub>lug</sub> = 9.00 in (Width of Lug Plate)

**Grout Bed Data:**

h<sub>g</sub> = 2.00 in (Height of Grout Bed)  
 h<sub>ce</sub> = 2.00 in (Embedment Depth - above Foundation)  
 f'<sub>cg</sub> = 6.00 Ksi (Grout value)

**Design Parameters:**

φ<sub>v</sub> = 0.75 (AISC 360-10 Section J8)  
 μ = 0.55 (Steel on Grout)  
 = 0.70 (Steel on Concrete)  
 φ<sub>b</sub> = 0.90 (AISC 360-10 Section J8)  
 φ<sub>w</sub> = 0.75 (AISC 360-10 Section Table J2.5 - Welds)  
 F<sub>ex</sub> = 70 ksi (Weld Strength)

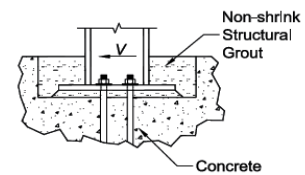
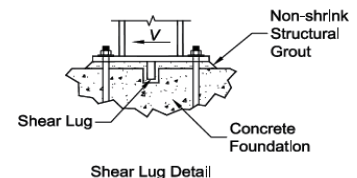
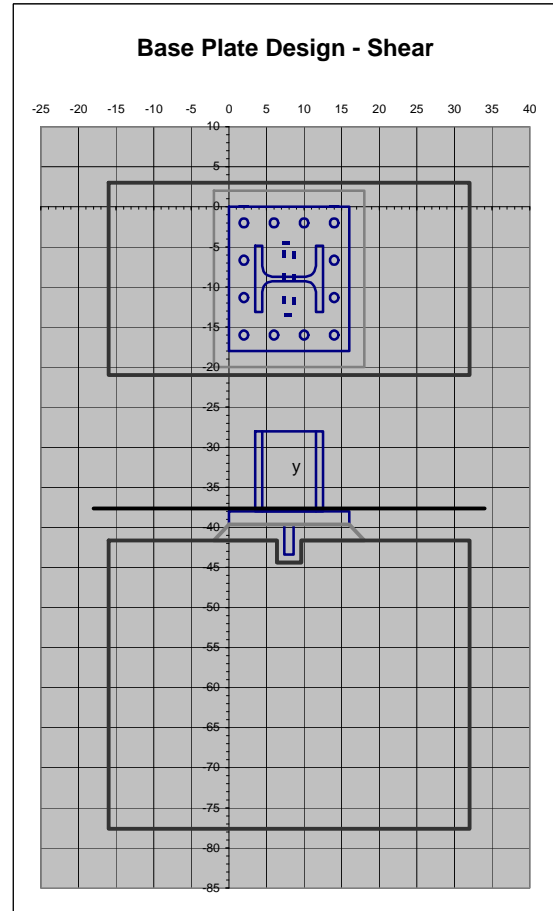


Figure 3.5.1. Transfer of base shears through bearing.

**COLUMN BASE PLATE DESIGN FOR SHEAR - SMRF 3 AT GRIDLINE 10**  
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**2. Shear Strength Components**

**A. Friction Component between Base Plate and Grout/Concrete Surface (ACI 318-08)**

$$\phi V_f = \phi \mu P_U \leq 0.2 f'_c A_c \quad \text{Where } \phi = 0.75$$

$$\mu = 0.55 \quad (\text{Steel on Grout})$$

$$P_U = 15 \text{ Kips} \quad (+ \text{ is Comp, } - \text{ is Tension})$$

$$= \text{MIN}(6,346)$$

$$\phi V_f = 6 \text{ Kips}$$

**Limit Values:**

$$f'_c = 6.00 \text{ Ksi}$$

$$A_c = N B \quad \text{for } N = 16.00 \text{ inches}$$

$$B = 18.00 \text{ inches}$$

$$A_c = 288 \text{ in}^2$$

$$0.2 f'_c A_c = 346 \text{ Kips}$$

$$\phi V_f = 6 \text{ Kips}$$

**B. Bearing Component between Steel and Concrete Surfaces**

a) Bearing on Column or Side of Base Plate

$$\phi V_b = \text{Bearing on Base Plate} + \text{Bearing on Column Flange}$$

$$= 0.55 f'_c (A_{bp} + A_{cf}) \quad \text{Where } f'_c = 6.00 \text{ Ksi}$$

$$A_{bp} = \text{Bearing on Base Plate}$$

$$= B \text{ MIN}(t_p, h_{ce}) \quad \text{for } B = 18.00 \text{ inches (Base Plate - Width)}$$

$$t_p = 1.63 \text{ inches (Base Plate - Thickness)}$$

$$h_{ce} = 2.00 \text{ in (Embedment Depth - above Foundation)}$$

$$A_{bp} = 29.25 \text{ in}^2 \quad (\text{Bearing on Base Plate})$$

$$A_{cf} = \text{Bearing on Column Flange}$$

$$= b_f h_f \quad \text{for } b_f = 8.28 \text{ inches (Wide Flange - Width)}$$

$$h_f = \text{MIN}(h_{ce} - t_p, 0) \quad \text{and } h_{ce} = 2.00 \text{ in (Embedment Depth - above Base Plate)}$$

$$t_p = 1.63 \text{ inches (Base Plate - Thickness)}$$

$$h_f = 0.38 \text{ inches} \quad (\text{Flange embedment Length})$$

$$A_{cf} = 3.11 \text{ in}^2 \quad (\text{Bearing on Column Flange})$$

$$= 3.30 (29.3 + 3.1)$$

$$= (97 + 10)$$

$$\phi V_b = 107 \text{ Kips}$$

b) Bearing on Shear Lug

i) Ultimate **Bearing Strength** of Concrete in contact w/ Shear Lug :

$$\phi P_b = 0.80 f'_c A_{sl} \quad \text{Where } f'_c = 4.00 \text{ Ksi}$$

$$A_{sl} = \text{Bearing on Shear Lug}$$

$$= h'_e W_{lug} \quad \text{for } h'_e = h_{lug} - h_g \quad \text{and } h_{lug} = 3.75 \text{ in (Height of Lug plate)}$$

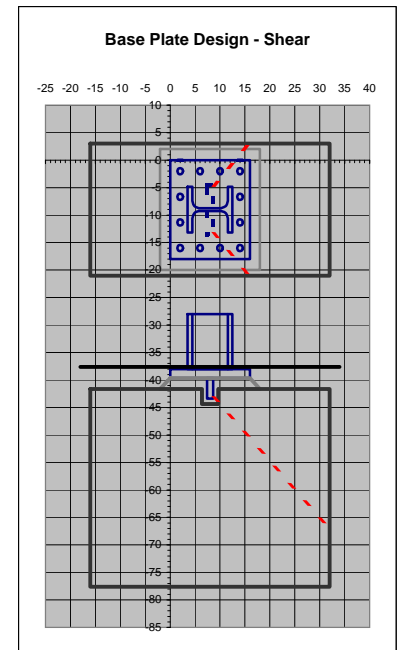
$$h_g = 2.00 \text{ in (Height of Grout Bed)}$$

$$h'_e = 1.75 \text{ in} \quad (\text{Effective Height of Lug plate})$$

$$W_{lug} = 9.00 \text{ in (Width of Lug Plate)}$$

$$A_{sl} = 15.75 \text{ in}^2 \quad (\text{Bearing on Shear Lug})$$

$$\phi P_b = 50 \text{ Kips}$$



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ii) Ultimate **Shear Strength** of Concrete in contact w/ Shear Lug

$$\phi V_n = 4.0 \phi_v f_c^{0.50} A_v \quad \text{Where } \phi_v = 0.75 \quad (\text{AISC 360-10 Section J8})$$

$$f_c = 4.00 \text{ Ksi}$$

$$= 4,000 \text{ psi}$$

$$A_v = L_{FP} H_{FP} - A_{sl}$$

Where  $L_{FP}$  = Length of Concrete Failure Plane

$$= W_F \quad \text{for } W_F = 2.00 \text{ feet (foundation Width)}$$

$$= 24.00 \text{ inches}$$

$$L_{FP} = 24.00 \text{ inches}$$

$H_{FP}$  = Height of Concrete Failure Plane

$$= (h_{lug} - h_g) + (L_F - t_p) / 2 \quad \text{for } h_{lug} = 3.75 \text{ in (Height of Lug plate)}$$

$$h_g = 2.00 \text{ in (Height of Grout Bed)}$$

$$= 1.75 + 23.38$$

$$L_F = 4.00 \text{ feet (foundation Length)}$$

$$= 48.00 \text{ inches}$$

$$t_{lug} = 1.25 \text{ in (Thickness of Lug Plate)}$$

$$H_{FP} = 25.13 \text{ inches}$$

$$A_{sl} = 15.75 \text{ in}^2 \quad (\text{Bearing Area on Shear Lug})$$

$$A_v = 587 \text{ inches}$$

$$\phi V_n = 111 \text{ Kips}$$

iii) Bending **Strength** Check of Shear Lug

$$M_U = \phi V_{lug} (h_g + h'_e / 2)$$

$$\text{Where } \phi V_{lug} = \text{MIN} (\phi P_b, \phi V_n)$$

$$\phi P_b = 50 \text{ Kips (Ultimate Concrete Strength - Bearing)}$$

$$\phi V_n = 111 \text{ Kips (Ultimate Concrete Strength - Shear)}$$

$$\phi V_{lug} = 50 \text{ Kips}$$

$$h_g = 2.00 \text{ in (Height of Grout Bed)}$$

$$h'_e = 1.75 \text{ in (Effective Height of Lug plate)}$$

$$M_U = 145 \text{ Kip-in (Flexural demands on Shear Lug)}$$

$$\phi M_n = \phi F_y Z$$

$$\text{Where } \phi_b = 0.90 \quad (\text{AISC 360-10 Section J8})$$

$$f_y = 55.00 \text{ Ksi for Grade of Bolt} = 55 \text{ Ksi (Grade 36, 55, or 105)}$$

$$Z = W_{lug} t_{lug}^2 / 4 \quad W_{lug} = 9.00 \text{ in (Width of Lug Plate)}$$

$$t_{lug} = 1.25 \text{ in (Thickness of Lug Plate)}$$

$$Z = 3.52 \text{ in}^3$$

$$\phi M_n = 174 \text{ Kip-in (Flexural Capacity of Shear Lug)}$$

**OK**

**COLUMN BASE PLATE DESIGN FOR SHEAR - SMRF 3 AT GRIDLINE 10**  
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iv) Required **Weld** between Shear Lug and Base Plate

i) **Weld Stress Demands**

$$f_v = (f_c^2 + f_v'^2)^{0.5}$$

where  $f_c = M_U / (t_{lug} W_{lug})$

for  $M_U = 145$  Kip-in (Flexural demands on Shear Lug)

$t_{lug} = 1.25$  in (Thickness of Lug Plate)

$W_{lug} = 9.00$  in (Width of Lug Plate)

$f_c = 12.88$  Kips/in

$f_v = V_U / (2 W_{lug})$

for  $V_U = 50$  Kips

$W_{lug} = 9.00$  in (Width of Lug Plate)

$f_v = 2.80$  Kips/in

$f_v = 13.18$  Kips/in

ii) **Check Min and Max Size of Fillet Weld**

$t_{min} = 1.25$  inches

for  $t_{lug} = 1.25$  in (Thickness of Lug Plate)

$t_p = 1.63$  inches (Base Plate - Thickness)

$t_w \text{ min} = 0.313$  inches (Table J2.4)

$t_w \text{ max} = 1.563$  inches (Section J2.2b)

AISC 360-10 Table J2.4		
Thinner Part	Min Size of Fillet	
t (inches)	t <sub>w</sub> min (inches)	t min (inches)
< 1/4"	1/8"	0.125
1/4" < t < 1/2"	3/16"	0.188
1/2" < t < 3/4"	1/4"	0.250
> 3/4"	5/16"	0.313

AISC 360-10	
Max Size of Fillet	
t (inches)	t <sub>w</sub> min (inches)
< 1/4"	t
> 1/4"	t - 1/16"

iii) **LRFD Weld Strength**

$R_n = \phi F_w A_w = \phi (0.6 F_{ex}) (0.707 t_w n_w L_w)$

Where  $\phi = 0.75$  (AISC 360-10 Section Table J2.5)

$F_{ex} = 70$  ksi (Weld Strength)

$n_w = 2$  Number of welds

t <sub>w</sub>	5/16	3/8	7/16	1/2	9/16	5/8	11/16	3/4
D	5	6	7	8	9	10	11	12
R <sub>n</sub> /L (kips/inch)	6.96	8.35	9.74	11.14	12.53	13.92	15.31	16.70
R <sub>n</sub> (kips)	14	17	19	22	25	28	31	33

(Number of 1/16")

(Weld Strength/inch/weld)

Use  $t_w = 5/16$  inches  $R_n = 14$  kips  
 OK, >Min, < Max OK, R<sub>n</sub> > f<sub>v</sub>'

**Use 5/16" fillet welds between Shear Lug and Base Plate**

c) Anchorage Shear Strength due to Confinement

Note : In the following equation, the term 1.2 (N<sub>y</sub> - P<sub>a</sub>) is taken as zero if assembly is in compression.

$\phi V_{conf} = 1.2 (N_y - P_a)$

N<sub>y</sub> = Yield Strength of tension Anchors

$N_y = n A_{se} f_y$

for  $n = 2 N_{BT} + 2 (N_{BL}-2)$

and  $N_{BL} = 4$  (N Bolts - Long)

$N_{BT} = 4$  (N Bolts - Transv)

$n = 12$  bolts

$A_{se} = 0.79$  in<sup>2</sup>

for  $D_B = 1.00$  inches (Bolt Diameter)

$f_y = 55.00$  Ksi

for Grade of Bolt = 55 Ksi (Grade 36, 55, or 105)

$N_y = 518$  Kips

P<sub>a</sub> = Factored external axial load on anchorage, Zero if in Compression

= - P<sub>U</sub> for P<sub>U</sub> = 15 Kips (+ is Compression, - is Tension)

$P_a = 0$  Kips

$\phi V_{conf} = 0$  Kips

**COLUMN BASE PLATE DESIGN FOR SHEAR - SMRF 3 AT GRIDLINE 10**  
 LRFD APPROACH - AISC 360-10 AND STEEL DESIGN GUIDE 1  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**3. Connection Shear Capacity - Summary**

Connection Demands :

$$V_U = 5 \text{ Kips}$$

$$\text{for } P_U = 15 \text{ Kips} \quad (+ \text{ is Compression, } - \text{ is Tension})$$

Connection Capacity :

$$\phi V_n = \phi V_f + \phi V_b + \phi V_{lug} + \phi V_{conf}$$

Where  $\phi V_f = 6 \text{ Kips}$  ( Friction Component - Base Plate and Grout/Concrete Surface )

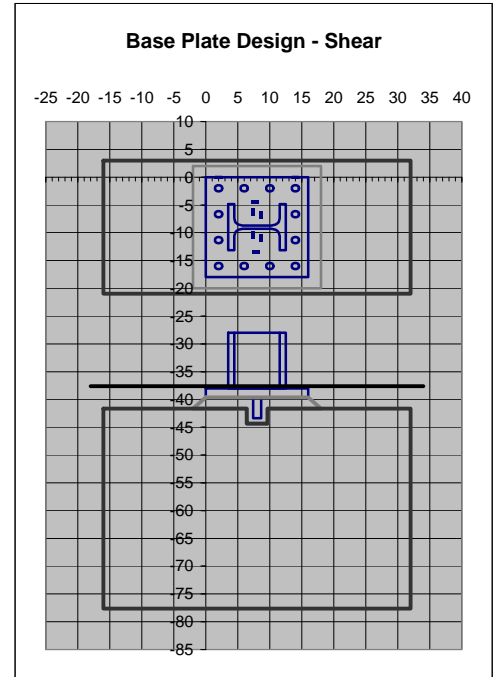
$\phi V_b = 107 \text{ Kips}$  ( Bearing on Column or Side of Base Plate )

$\phi V_{lug} = 50 \text{ Kips}$  ( Bearing on Shear Lug )

$\phi V_{conf} = 0 \text{ Kips}$  ( Anchorage Shear Strength due to Confinement )

$\phi V_n = 163 \text{ Kips}$
-------------------------------

**OK**



## NEW FOOTING DESIGN - SMRF 1 AT GRIDLINE I

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1  
 DETERMINATION OF VERTICAL AND LATERAL LOADS TO FOUNDATION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**Assumptions**

- Existing walls are treated as pinned Columns. Footing is assumed rigid.
- Column loads are located in transverse center of footing; limit of 2 columns w/o flexure.
- Footing has no shear reinforcement.
- Concrete is Normal Weight Concrete with uncoated bars.

**1. Lateral Loads and Load Effects**

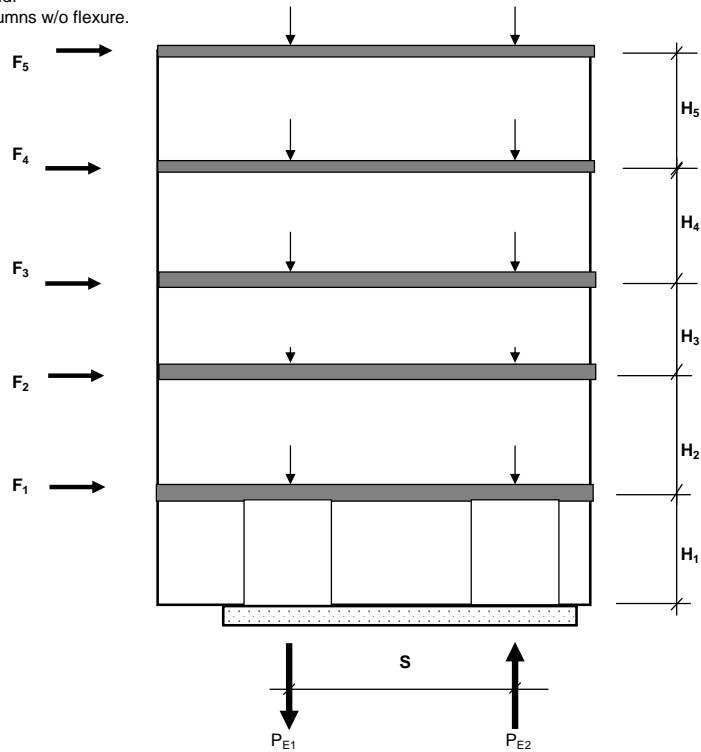
V = 6.00 kips (Base Shear - A4 ASD)

S = 14.50 feet (Separation between Wall centerlines)

Floor Level	Height (feet)	Loading ID	V <sub>x</sub> /V	Shear (Kips)	Force (Kips)
		5			
		4			
R	10.00	3	0.59	3.56	3.56
3	10.00	2	0.83	4.96	1.40
2	13.00	1	1.00	6.00	1.04

From summation of moments :

**P<sub>E1</sub> = -11.26 Kips**  
**P<sub>E2</sub> = 11.26 Kips**



**2. Vertical Loads and Load Effects**

Column	Floor Level	Floor Tributary Loads					Wall Tributary Loads				
		DL (psf)	Length (feet)	Width (feet)	Area (ft <sup>2</sup> )	Weight (kips)	WL (psf)	Length (feet)	Height (feet)	Area (ft <sup>2</sup> )	Weight (kips)
1											
	R	20	10.88	2.00	22	0.44	14	10.88	10.00	109	1.52
	3	30	10.88	2.00	22	0.65	14	10.88	10.00	109	1.52
	2	30	10.88	2.00	22	0.65	14	10.88	13.00	141	1.98

Sum of Floor Weight = 1.74 Kips      Sum of Wall Weight = 5.02 Kips

**P<sub>D1</sub> = 6.76 Kips**

Column	Floor Level	Floor Tributary Loads					Wall Tributary Loads				
		DL (psf)	Length (feet)	Width (feet)	Area (ft <sup>2</sup> )	Weight (kips)	WL (psf)	Length (feet)	Height (feet)	Area (ft <sup>2</sup> )	Weight (kips)
2											
	R	20	10.88	2.00	22	0.44	14	10.88	10.00	109	1.52
	3	30	10.88	2.00	22	0.65	14	10.88	10.00	109	1.52
	2	30	10.88	2.00	22	0.65	14	10.88	13.00	141	1.98

Sum of Floor Weight = 1.74 Kips      Sum of Wall Weight = 5.02 Kips

**P<sub>D2</sub> = 6.76 Kips**



**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
 ACI 318-11 LOADS AND DESIGN  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**Assumptions**

1. Column loads are located in transverse center of footing; limit of 2 columns w/o flexure.
2. Footing has no shear reinforcement.
3. Concrete is Normal Weight Concrete with uncoated bars.

**Footing Parameters :**

Footing Size :

$L_x = 17.25$  feet  
 $L_y = 2.00$  feet  
 $h_f = 3.00$  feet

Column Sizes :

$C_{1x} = 0.8$  feet (column length)  
 $C_{1y} = 0.7$  feet (column width)  
 $x_1 = 1.38$  feet (distance from edge of footing to  $C_1$  Centerline)  
 $C_{2x} = 0.8$  feet (column length)  
 $C_{2y} = 0.7$  feet (column width)  
 $x_2 = 15.88$  feet (distance from edge of footing to  $C_2$  Centerline)

Note:  $S = 14.50$  feet (Separation between column centerlines)

Interconnected Slab at Sides:

Note : Slabs at sides are used only to reduce soil bearing pressure; footing is designed to take all loads.

Side : Left Right

$t$  \_\_\_\_\_ Inches (Slab Thickness)

$X$  \_\_\_\_\_ Feet (distance to other Slab Edge Support)

$f'_c$  \_\_\_\_\_ Ksi

Conn Type \_\_\_\_\_ (D= Dowel, C= Continuous)

5.9

Footing Loads :

$V_x = 6.00$  kips (Base Shear - A4 ASD)  
 $V_y = 0.60$  kips

Load Factors : Strength =  $S$  (S for Strength, OS for Over-Strength)

$\Omega = 3.00$  (Overstrength Factor - SMRF)

Load	Unfactored Loads			Service Loads				Strength Loads			
	D	L	EQ	1.0 D + EQ	0.6 D + EQ	L	$P_s$	1.2 D + 1.4 EQ	0.9 D + 1.4 EQ	1.6 L	$P_U$
$P_1$	7		-11	-4	-7	0	-7	-8	-10	0	-10
$P_2$	7		11	18	15	0	18	24	22	0	24

Capacity Factors :

$\phi_v = 0.75$  (Shear)  
 $\alpha = 40$  (40 for interior columns, 30 for edge columns, 20 for corner columns)

Concrete :

$f'_c = 3.25$  Ksi  
 $f_y = 60.00$  Ksi  
 $\rho_c = 0.150$  kip/ft<sup>3</sup>

Reinforcement:

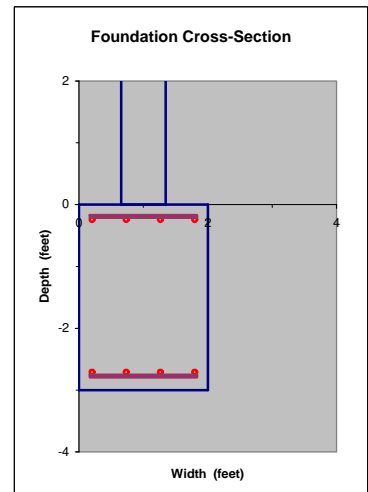
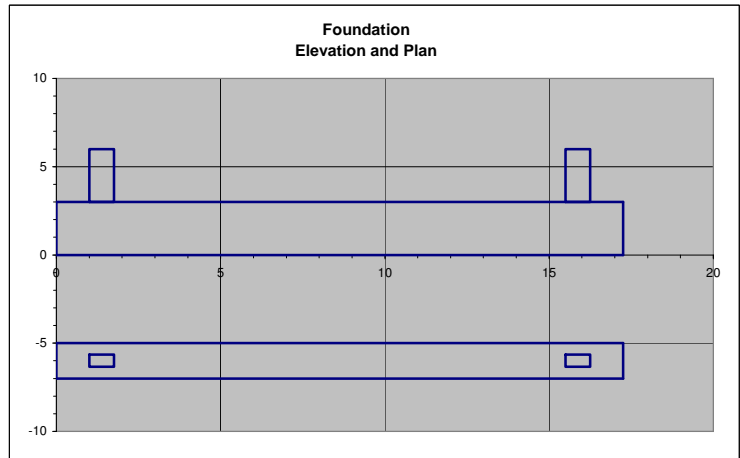
$d_c = 2.00$  inches (bar clearance - top)  
 $= 3.00$  inches (bar clearance - bottom)  
 $= 2.00$  inches (bar clearance - sides)

	Orientation	Bar Size	N Bars	Bottom Layer	d (inches)	Bar Spacing (inches)	Bar Diameter (inches)	Bar Area	
								Per Bar (in <sup>2</sup> )	Total (in <sup>2</sup> )
Top Mat	x	7	4	x	33.13	6.38	0.88	0.60	2.40
	y	4	65		33.00	3.16	0.50	0.20	13.00
Bottom Mat	x	7	4		31.63	6.38	0.88	0.60	2.40
	y	4	65	x	33.50	3.16	0.50	0.20	13.00

Note: Used for placing top bars only.

Soil Parameters :

Soil density = 120 pcf  
 $\sigma_{allow} = 2.00$  ksf (allowable bearing pressure)  
 $\sigma_p = 0.30$  ksf/ft (Passive Soil Pressure)  
 $\mu = 0.25$  ksf (Coefficient of Friction)



**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
 ACI 318-11 LOADS AND DESIGN  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**2. Lateral Resistance of Foundation**

**2A. Longitudinal Loading**

$$F_{Rx} = 0.5 L'_y h'_i{}^2 \sigma_p + 0.6 (W_f + P) \mu$$

Where  $L'_y = L_y + 2 t_{nw}$

and  $L_y = 2.0$  feet

$t_{nw} = 0.83$  feet (Thickness of (E) connected walls at ends)

$L'_y = 3.67$  feet (Bearing Width at Ends of Footing)

$h'_i = h_t + h_{sk}$  and  $h_t = 3.0$  feet

$h_{sk} = 0.00$  feet (Additional height of Shear Key at Footing End)

$h'_i = 3.0$  feet (Bearing Height at Ends of Footing)

$\sigma_p = 0.30$  ksf/ft (Passive Soil Pressure)

$W_f = \rho_c L_x L_y h_t$  and  $\rho_c = 0.150$  kip/ft<sup>3</sup>

$L_x = 17.3$  feet

$L_y = 2.0$  feet

$h_t = 3.0$  feet

$W_f = 15.53$  Kips (Footing Weight)

$P = P_1 + P_2$  and  $P_1 = 6.8$  Kips

$P_2 = 6.8$  Kips

$P = 13.5$  Kips (Service Load)

$\mu = 0.25$  ksf (Coefficient of Friction)

Note :  $V_x = 6.00$  kips

$F_{Rx} = 9.31$  kips  
**OK**

**Foundation OK for Sliding**

**3. Soil Pressure due to Applied Loads - Service and Strength Loading**

a) Applied soil stress - uniform

$$q = (P_1 + P_2)/L_x$$

	Service	Strength
Where $P_1 =$	-7	-10
$P_2 =$	18	24
$L_x =$	17.3	feet

$q = 0.63$  kip/ft (Service)  
 $= 0.82$  kip/ft (Strength)

b) Centroid of Factored Loads - from Left Edge of Footing

$$X_R = (x_1 P_1 + x_2 P_2 + W_f L_x/2) / (P_1 + P_2 + W_f)$$

	Service	Strength
Where $X_1 =$	1.38	1.38
$P_1 =$	-7	-10
$X_2 =$	15.88	15.88
$P_2 =$	18	24
$W_f =$	15.53	Kips (Footing Weight)
$L_x =$	17.3	feet

$X_R = 15.57$  feet (Service)  
 $= 16.81$  feet (Strength)

c) Applied soil stress - Trapezoidal

Note: This conditions applies when  $\Delta q < q$ , and  $L_b = L_x$

$$\Sigma M_o = -X_1 P_1 - X_2 P_2 + (q - \Delta q) L_x^2/2 + 1/2 (2 \Delta q) L_x L_{\Delta q}$$

$$\Rightarrow \Delta q = (q L_x^2/2 - X_1 P_1 - X_2 P_2) / (L_x^2/2 - L_x L_{\Delta q})$$

**<= Does not apply**

	Service	Strength
Where $X_1 =$	1.38	1.38
$P_1 =$	-7	-10
$X_2 =$	15.88	15.88
$P_2 =$	18	24
$q =$	0.63	0.82
$L_x =$	17.3	feet

$$L_{\Delta q} = L_x/3 \quad \text{if } X_R < 0.5 L_x$$

$$= 2 L_x/3 \quad \text{if } X_R > 0.5 L_x$$

$L_{\Delta q} = 11.50$  feet (Service)  
 $= 11.50$  feet (Strength)

Incremental Soil Bearing Stresses :

$\Delta q = 3.69$  (Service)  
**Soil Stress is NOT Trapezoidal**

$\Delta q = 4.91$  kips/ft (Strength)  
**Soil Stress is NOT Trapezoidal**

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
**ACI 318-11 LOADS AND DESIGN**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

d) Applied soil stress - **Triangular** <= **Governs**

Notes: This condition applies when  $\Delta q \geq q$ , and  $L_b \leq L_x$

$$X_R = 15.57 \text{ feet} = > \text{Large Rotation to Right} \quad \text{Service}$$

$$= 16.81 \text{ feet} \quad \text{Strength}$$

$$0.5 L_x = 8.6 \text{ feet}$$

i) Rotation to Left - Footing Bearing Length

$$L_b = 3 (0.5 L_x - e) \quad \text{Where } 0.5 L_x = 8.6 \text{ feet}$$

$$e = X_R - 0.5 L_x$$

$$\text{and } X_R = 15.57 \text{ feet} \quad \text{Service}$$

$$X_R = 16.81 \text{ feet} \quad \text{Strength}$$

$$e = 6.94 \text{ feet} \quad \text{Service}$$

$$= 8.18 \text{ feet} \quad \text{Strength}$$

Service  
Strength

$$L_b = \text{NA} \text{ feet}$$

$$= \text{NA} \text{ feet}$$

ii) Rotation to Right - Footing Bearing Length

$$L_b = 3 (0.5 L_x - e) \quad \text{Where } 0.5 L_x = 8.6 \text{ feet}$$

$$e = X_R - 0.5 L_x$$

$$\text{and } X_R = 15.57 \text{ feet} \quad \text{Service}$$

$$X_R = 16.81 \text{ feet} \quad \text{Strength}$$

$$e = 6.94 \text{ feet} \quad \text{Service}$$

$$= 8.18 \text{ feet} \quad \text{Strength}$$

$$L_b = 5.05 \text{ feet} \quad \text{Service}$$

$$1.33 \text{ feet} \quad \text{Strength}$$

iii) Resulting Soil Bearing Length and Triangular Pressure

$$\Delta q = 2(P_1 + P_2)/L_b \quad \text{Service} \quad \text{Strength}$$

Where  $P_1 = -7 \quad -10$  kips  
 $P_2 = 18 \quad 24$  kips  
 $L_b = 5.05 \quad 1.33$  feet

$$\Delta q = 4 \text{ kips/ft} \quad \text{Service}$$

$$= 21 \text{ kips/ft} \quad \text{Strength}$$

e) Applied Soil Stresses - Governing

**Service Loads :**

Note: Large Rotation to Right

$$q = 0.00 \text{ kips/ft} \quad X_R = 15.57 \text{ feet}$$

$$\Delta q = 4.28 \text{ kips/ft} \quad 0.5 L_x = 8.63 \text{ feet}$$

$$L_b = 5.05 \text{ feet}$$

Note:  $L_o = 12.20$  feet (location of soil zero value)

**Strength Loads :**

Note: Large Rotation to Right

$$q = 0.00 \text{ kips/ft} \quad X_R = 16.81 \text{ feet}$$

$$\Delta q = 21.43 \text{ kips/ft} \quad 0.5 L_x = 8.63 \text{ feet}$$

$$L_b = 1.33 \text{ feet}$$

Note:  $L_o = 15.92$  feet (location of soil zero value)

f) Check of Soil Bearing Stress

**Service Loads :**

$$\sigma_b = q_{max} / L_y \leq \sigma_b \quad \text{Where } q_{max} = 4.28 \text{ kips/ft}$$

$$L_y = b = 2.00 \text{ feet}$$

$$\sigma_b = 2.14 \text{ Ksf} \quad \text{Service}$$

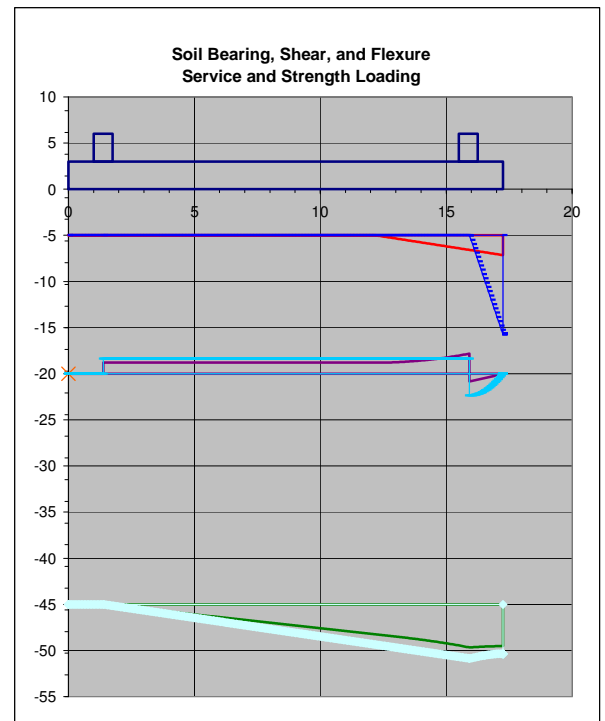
**NG**

**Strength Loads :**

$$\sigma_{bu} = q_u / L_y \leq \sigma_b \quad \text{Where } q_u = 21.43 \text{ kips/ft}$$

$$L_y = b = 2.00 \text{ feet}$$

$$\sigma_b = 10.72 \text{ Ksf} \quad \text{Strength}$$



Note: Bearing Stress OK as (N) footing connected to (E) Footing on 3 sides.

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
 ACI 318-11 LOADS AND DESIGN  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**4. Applied Loading and Demands on Footing - Strength Loads**

	Left End	Left Column Centerline	Inflection Point	Right Column Centerline	Right End
Location (feet)	0	1.38		15.88	17.25
Load (kips)	-	-7	-	18	-
$V_L$ (kips)	0	0		10	
$V_R$ (kips)	-	10	-	-14	-
$M_L$ (kip-ft)	0	0	-	-140	-
$M_R$ (kip-ft)	-	0		-141	

**5. Adequacy of Footing - Shear**

**5A. Check of Flexural/One-Way Shear (ACI 15.5.2 and 11.1.3.1)**

Shear demands:  $V_{max} = 14$  Kips @  $x = 15.88$  feet

$$V_u = V_{max} - q(d + C/2)$$

Where  $V_{max} = 14$  Kips

$q_u = 3.11$  Kips/ft @  $x = 15.88$  feet

$d = h_t - d_c - d_b$  and  $h_t = 3.0$  feet  
 $= 36.00$  inches  
 $d_c = 3.00$  inches  
 $d_b = 0.5$  inches

$$d = 32.50 \text{ inches} = 2.71 \text{ feet}$$

$C = 0.00$  feet

$$V_u = 6 \text{ Kips}$$

b) Shear Strength provided by Concrete (ACI 11.3.1.1)

$$\phi V_c = \phi 2 f'_c{}^{0.5} b_w d$$

Where  $\phi = 0.75$   
 $f'_c = 3,250$  psi  
 $b = L_y = 2.0$  feet  
 $= 24.0$  inches  
 $d = 32.50$  inches

$$\phi V_c = 67 \text{ kips}$$

**OK, > Vu**

Note: if footing shear reinforcement is needed, use EQ (11-5) in ACI 11.3.2.1.

**5B. Punching/Two Way Shear (ACI 11.5.5.2, 11.12.1.2)**

**A. Left Column**

Shear demands:  $V_u = 10$  Kips

a) Failure Perimeter

$$b_0 = 2(b_1 + b_2) \quad \text{Where } b_1 = X_1 + 0.5(C_{2x} + d) \leq C_{2x} + d$$

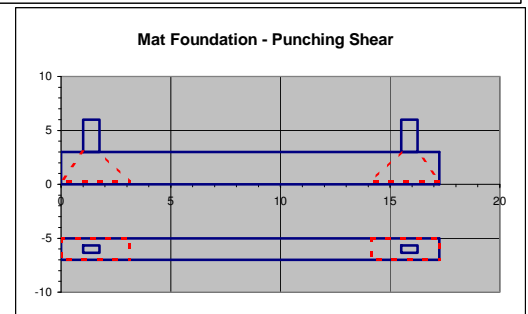
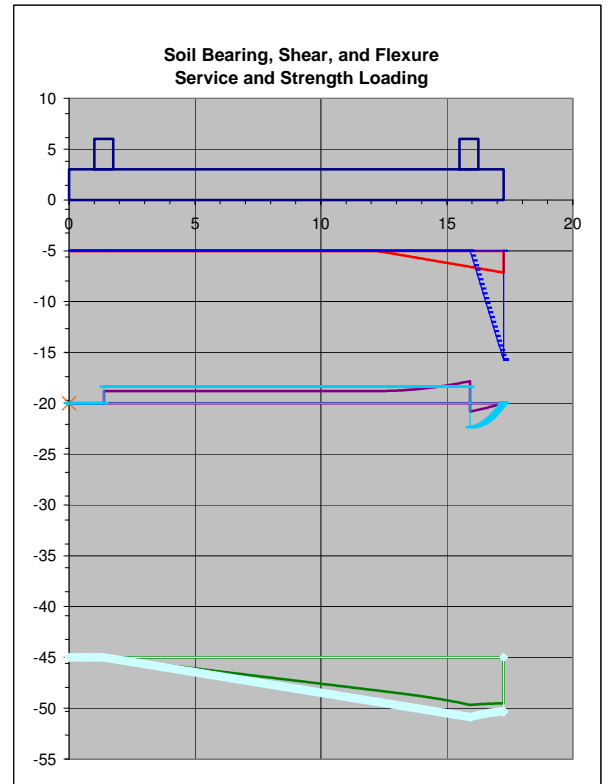
and  $X_1 = 1.38$  feet  
 $= 16.50$  inches  
 $C_{2x} = 9.00$  inches  
 $d = 32.50$  inches

$$b_1 = 37.25 \text{ inches}$$

$b_2 = C_{2y} + d \leq L_y$  and  $C_{2y} = 8.28$  inches  
 $d = 32.50$  inches  
 $L_y = 24.0$  inches

$$b_2 = 24.00 \text{ inches}$$

$$b_0 = 98.5 \text{ inches}$$



**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
 ACI 318-11 LOADS AND DESIGN  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

b) Factored Shear Capacity (ACI 11.12.2.1)

$$\phi V_c = \phi \text{Min} \left[ 2 + \frac{4}{\beta}, \frac{\alpha d}{b_o} + 2, 4 \right] \sqrt{f'_c} b_o d$$

Where  $\phi = 0.75$   
 $\beta = C_{max}/C_{min}$  and  $C_{max} = 9.00$  inches  
 $C_{min} = 8.28$  inches

$\beta = 1.09$

$\alpha = 30$  (40 for interior columns, 30 for edge columns, 20 for corner columns)

$d = \text{Min}(d_1, d_2)$   $d_1 = 31.63$  inches  
 $d_2 = 33.50$  inches

$d = 31.63$  inches

$b_o = 98.5$  inches  
 $f'_c = 3,250$  psi

$\phi V_c = 533$  kips  
**OK, > Vu**

**B. Right Column**

Shear demands:  $V_u = 14$  Kips

a) Failure Perimeter

$b_o = 2(b_1 + b_2)$  Where  $b_1 = 0.5(C_{2x} + d) + (L_x - X_2) \leq C_{2x} + d$

and  $L_x = 17.3$  feet  
 $X_2 = 15.88$  feet

$L_x - X_2 = 1.38$  feet  
 $= 16.50$  inches

$C_{2x} = 9.00$  inches  
 $d = 32.50$  inches

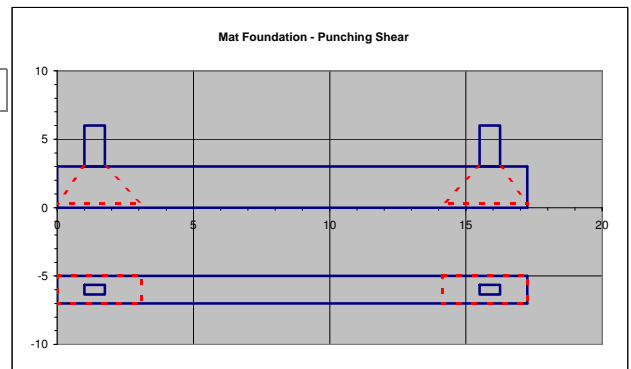
$b_1 = 37.25$  inches

$b_2 = C_{2y} + d \leq L_y$

and  $C_{2y} = 8.28$  inches  
 $d = 32.50$  inches  
 $L_y = 24.0$  inches

$b_2 = 24.00$  inches

$b_o = 98.5$  inches



b) Factored Shear Capacity (ACI 11.12.2.1)

$$\phi V_c = \phi \text{Min} \left[ 2 + \frac{4}{\beta}, \frac{\alpha d}{b_o} + 2, 4 \right] \sqrt{f'_c} b_o d$$

Where  $\phi = 0.75$   
 $\beta = C_{max}/C_{min}$  and  $C_{max} = 9.00$  inches  
 $C_{min} = 8.28$  inches

$\beta = 1.09$

$\alpha = 30$  (40 for interior columns, 30 for edge columns, 20 for corner columns)

$d = \text{Min}(d_1, d_2)$   $d_1 = 31.63$  inches  
 $d_2 = 33.50$  inches

$d = 31.63$  inches

$b_o = 98.5$  inches  
 $f'_c = 3,250$  psi

$\phi V_c = 533$  kips  
**OK, > Vu**

**Footing OK for Shear**

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
 ACI 318-11 LOADS AND DESIGN  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**6. Adequacy of Footing - Flexure**

**6A. Longitudinal Top Reinforcement Check**

Flexural demands:  $M_u = 0$  Kip-ft @  $x =$  feet (Inflection Point)

a) Required Reinforcement Ratio (ACI 10.2)

$$\rho_r = \frac{0.85 f'_c}{f_y} \left[ 1 - \sqrt{1 - \frac{2 M_u}{0.765 b d^2 f'_c}} \right]$$

Where  $f'_c = 3.25$  Ksi  
 $f_y = 60.00$  Ksi  
 $M_u = 0$   
 $= 0$  kip-in  
 $b = L_y = 2.0$  feet  
 $= 24$  inches  
 $d_{top} = 33.13$  inches

$\rho_r = 0.0000$

b) Maximum Reinforcement Ratio (ACI 10.3.4)

$$\rho_t = 0.85 \beta_1 \frac{f'_c}{f_y} \left[ \frac{\epsilon_c}{\epsilon_c + \epsilon_s} \right]$$

Where  $f'_c = 3.25$  Ksi  
 $f_y = 60.00$  Ksi  
 $\beta_1 = 0.85$   
 $= 0.85 - 0.05 (f'_c - 4.0), \geq 0.65$   
 $\epsilon_c = 0.003$  (ACI Section 10.3.4)  
 $\epsilon_s = 0.005$

$\beta_1 = 0.85$

$\rho_t = 0.0147$

c) Minimum Reinforcement of Flexural Members (ACI 10.5, 7.12.2.1)

$$\rho_{min} = \text{Max} \left[ 3 f'_c \frac{0.005}{f_y}, 200/f_y \right] \leq \text{Max} [1.33 \rho_t, 0.0018]$$

$$= \text{Max} [0.0029, 0.0033] \leq \text{Max} [0.0000, 0.0018]$$

$$= \text{Max} [0.0033] \leq \text{Max} [0.0018]$$

$\rho_{min} = 0.0018$

Where  $f'_c = 3,250$  psi  
 $f_y = 60,000$  psi  
 $\rho_r = 0.0000$  (Required Reinforcement Ratio)

d) Required Reinforcement Area

$$A_{s1} = \rho L_y d_2$$

Where  $\rho = \rho_r$  if  $\rho_r \leq \rho_{max}$  and  $\rho_r \geq \rho_{min}$  and  $\rho_r = 0.00000$   
 $= \rho_{max}$  if  $\rho_r > \rho_{max}$   $\rho_{max} = 0.01468$   
 $= \rho_{min}$  if  $\rho_r < \rho_{min}$   $\rho_{min} = 0.00180$

Where  $\rho_r = 0.0018$

$L_y = 2.0$  feet  
 $= 24.0$  inches  
 $d_{top} = 33.13$  inches

$A_{s1} = 1.43$  in<sup>2</sup>

Note:  $A_{s1} = 2.40$  in<sup>2</sup> (reinforcement provided)  
**OK**

**4 - No. 7 Longitudinal Top Bars OK**

**6B. Longitudinal Bottom Reinforcement Check**

a) Flexural Demands (ACI 15.4.2)

$M_u = 0$  Kip-ft @  $x = 1.38$  feet (at face of Left Column)  
 $= -141$  Kip-ft @  $x = 15.88$  feet (at face of Right Column)

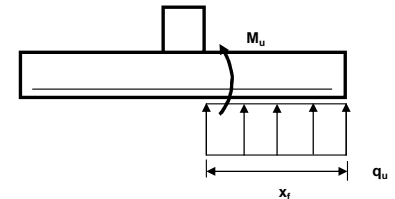
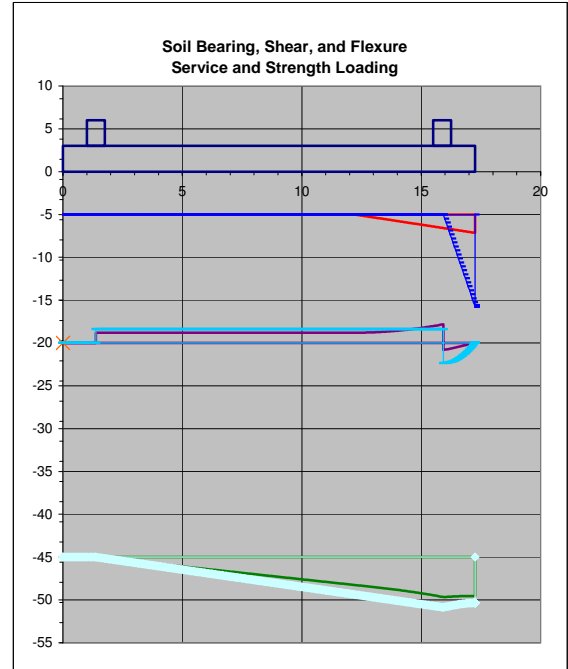
$M_u = 141$  kip-ft  
 $= 1,689$  kip-in

b) Required Reinforcement Ratio (ACI 10.2)

$$\rho_r = \frac{0.85 f'_c}{f_y} \left[ 1 - \sqrt{1 - \frac{2 M_u}{0.765 b d^2 f'_c}} \right]$$

Where  $f'_c = 3.25$  Ksi  
 $f_y = 60.00$  Ksi  
 $M_u = 1,689$  kip-in  
 $b = L_y = 2.0$  feet  
 $= 24$  inches  
 $d_{bott} = 31.63$  inches

$\rho_r = 0.0013$



**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
 ACI 318-11 LOADS AND DESIGN  
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c) Required Reinforcement of Flexural Members

Note:  $A_{sb} = 2.40 \text{ in}^2$  (Bottom flexural steel provided)

$A_{req} = \rho b d$

Where  $\rho = \rho_r$  for  $\rho_r \leq \rho_r$  and  $\rho_r \geq \rho_{min}$   
 $= \rho_{min}$  for  $\rho_r \leq \rho_{min}$   
 $= 0$  Otherwise

Where  $\rho_r = 0.0013$   
 $\rho_r = 0.0147$   
 $\rho_{min} = 0.0018$

$\rho = 0.0018$

Note: for  $\rho_r \leq \rho_{min}$  condition, check Minimum Reinforcement exception (ACI 10.5.3)

$A_{min} = 1.33 \rho_r b d$

Where  $\rho_r = 0.0013$  (required reinforcement ratio)

$b = L_y = 24.0$  inches

$d = d_{bot} = 31.63$  inches

$A_{min} = 1.33 \text{ in}^2$

$b = L_y = 24.0$  inches

$d = d_{bot} = 31.63$  inches

$A_{req} = \text{in}^2$

**4 - No. 7 Longitudinal Bottom Bars OK**

**6C. Transverse Bottom Reinforcement Check**

a) Flexural Demands (ACI 15.4.2)

i) At Left Column

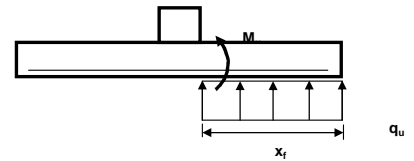
$M_u = q_u x_l^2 / 2$

Where  $q_u = 0$  Kip/ft @  $x = 1.38$  feet (at Left Column)

$x_l = L_y / 2 - C_{1y} / 2$  and  $L_y = 2.0$  feet  
 $C_{1y} = 0.7$  feet

$x_l = 0.66$  feet

$M_u = 0$  kip-ft



ii) At Right Column

$M_u = q_u L_x x_l^2 / 2$

Where  $q_u = 3$  Kip/ft @  $x = 15.88$  feet (at Right Column)

$x_l = L_y / 2 - C_{2y} / 2$  and  $L_y = 2.0$  feet  
 $C_{2y} = 0.7$  feet

$x_l = 0.66$  feet

$M_u = 1$  kip-ft

iii) Governing Value

$M_u = 1$  kip-ft  
 $= 8$  kip-in

b) Required Reinforcement Ratio (ACI 10.2)

$\rho_r = \frac{0.85 f'_c}{f_y} \left[ 1 - \sqrt{1 - \frac{2 M_u}{0.765 b d^2 f'_c}} \right]$

Where  $f'_c = 3.25$  Ksi  $b = L_x = 17.3$  feet  
 $f_y = 60.00$  Ksi  $= 207$  inches  
 $M_u = 8$  kip-in  $d_{bot} = 31.63$  inches

$\rho_r = 0.0000$

c) Required Reinforcement of Flexural Members

Note:  $A_{sb} = 13.00 \text{ in}^2$  (Bottom flexural steel provided)

$A_{req} = \rho b d$

Where  $\rho = \rho_r$  for  $\rho_r \leq \rho_r$  and  $\rho_r \geq \rho_{min}$   
 $= \rho_{min}$  for  $\rho_r \leq \rho_{min}$   
 $= 0$  Otherwise

Where  $\rho_r = 0.0000$   
 $\rho_r = 0.0147$   
 $\rho_{min} = 0.0018$

$\rho = 0.0018$

Note: for  $\rho_r \leq \rho_{min}$  condition, check Minimum Reinforcement exception (ACI 10.5.3) - for  $L_y > 5.0'$

$A_{min} = 1.33 \rho_r b d$

Where  $\rho_r = 0.0000$  (required reinforcement ratio)

$b = L_x = 207.0$  inches

$d = d_{bot} = 33.50$  inches

$A_{min} = \text{NA}$  in<sup>2</sup>

$b = L_y = 207.0$  inches

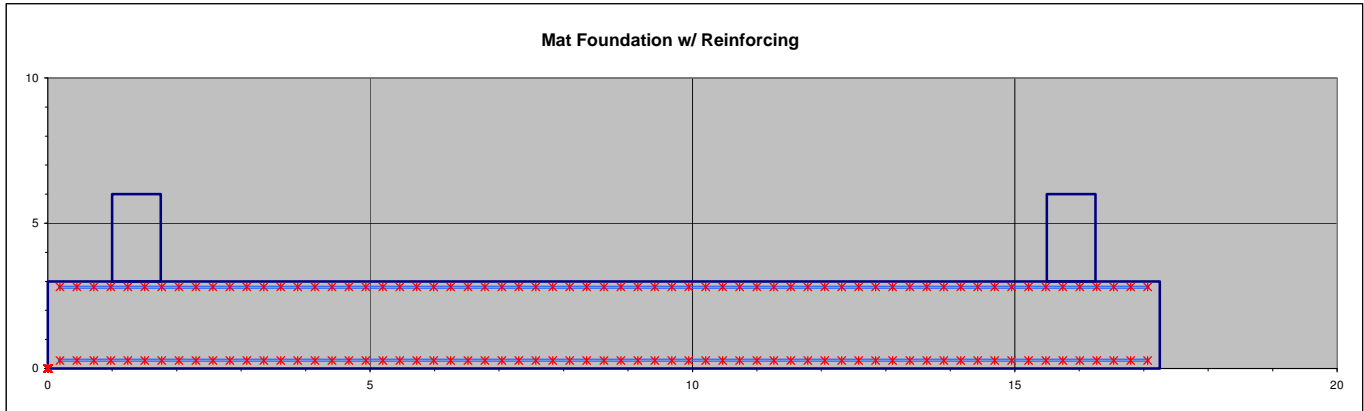
$d = d_{bot} = 33.50$  inches

$A_{req} = 12.48 \text{ in}^2$

**65 - No. 4 Transverse Bottom Bars OK**

SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1  
 ACI 318-11 LOADS AND DESIGN  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT

**7. Footing Reinforcement Summary**



**Footing Parameters :**

Footing Size :  
 $L_x = 17.3$  feet  
 $L_y = 2.0$  feet  
 $h_t = 3.0$  feet

Reinforcement Summary:  $d_c = 2.00$  inches (bar clearance - top)  
 = 3.00 inches (bar clearance - bottom)  
 = 2.00 inches (bar clearance - sides)

	Orientation	Bar Size	N Bars	Bottom Layer	d (inches)	Bar Spacing (inches)	Bar Diameter (inches)	Bar Area	
								Per Bar (in <sup>2</sup> )	Total (in <sup>2</sup> )
Top Mat	x	7	4	x	33.13	6.38	0.88	0.60	2.40
	y	4	65		33.00	3.16	0.50	0.20	13.00
Bottom Mat	x	7	4		31.63	6.38	0.88	0.60	2.40
	y	4	65	x	33.50	3.16	0.50	0.20	13.00

Note: Used for placing top bars only.

**1. Design of Slab-to-Footing Connections**

Interconnected Slab at Sides:

Note : Slabs at sides are used only to reduce soil bearing pressure; footing is designed to take all loads.

Side : Left Right

t Inches (Slab Thickness)  
 X Feet (distance to other Slab Edge Support)  
 $f'_c$  Ksi

Conn Type (D= Dowel, C= Continuous)

RC Slab not Needed

**2. Lateral Resistance of Foundation**

Foundation OK for Sliding

**3. Soil Pressure due to Applied Loads**

$\sigma_b = 2.14$  Ksf  
 NG

Note:  $\sigma_{allow} = 2.00$  ksf (allowable bearing pressure)

**5. Adequacy of Footing - Shear**

Footing OK for Shear

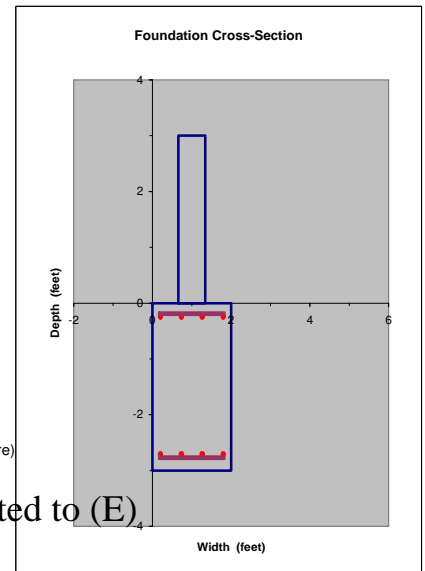
**6. Adequacy of Footing - Flexure**

Note: Bearing Stress OK as (N) footing connected to (E)  
 Footing on 3 sides.

4 - No. 7 Longitudinal Top Bars OK

4 - No. 7 Longitudinal Bottom Bars OK

65 - No. 4 Transverse Bottom Bars OK





**ADDITIONAL FOUNDATION REINFORCEMENT  
FOR RESISTING FIXED BASE COLUMN CONNECTION**

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1**  
**DETERMINATION OF ADDITIONAL REINFORCEMENT REQUIRED - FIXED BASE COLUMN CONDITION**  
**785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**1. Parameters**

Footing Size :

$L_x = 17.25$  feet  
 $L_y = 2.00$  feet  
 $h_f = 3.00$  feet

Base Plate Dimensions:

**Note:** Base Plate design done elsewhere.

$N = 16.00$  inches (Base Plate - Length)  
 $B = 18.00$  inches (Base Plate - Width)  
 $t_{PL} = 1.50$  inches (Base Plate - Thickness)

Column: **W8x67**

$d = 9.00$  inches (Wide Flange - Depth)  
 $b_f = 8.28$  inches (Wide Flange - Width)  
 $t_f = 0.94$  inches (Wide Flange - Thickness)  
 $Z_x = 70.1$  in<sup>3</sup> (Wide Flange - Plastic Section)  
 $A = 19.70$  in<sup>2</sup> (Wide Flange - Area)  
 $F_y = 50$  Ksi

Concrete :  
 $f'_c = 3.25$  Ksi  
 $f_y = 60.00$  Ksi  
 $\rho_c = 0.15$  kip/ft<sup>3</sup>

Reinforcement:  
 $d_c = 2.00$  inches (bar clearance - top)  
 = 3.00 inches (bar clearance - bottom)  
 = 2.00 inches (bar clearance - sides)

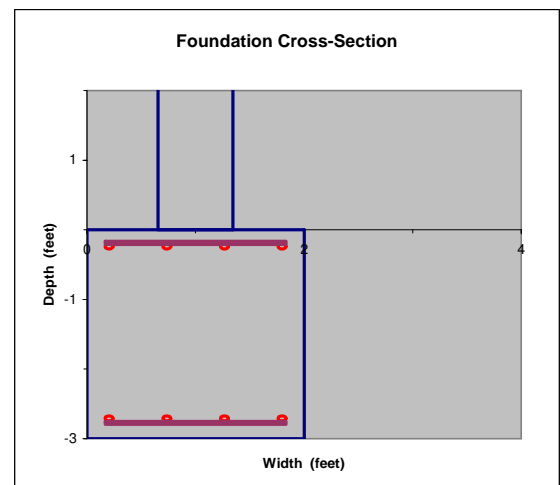
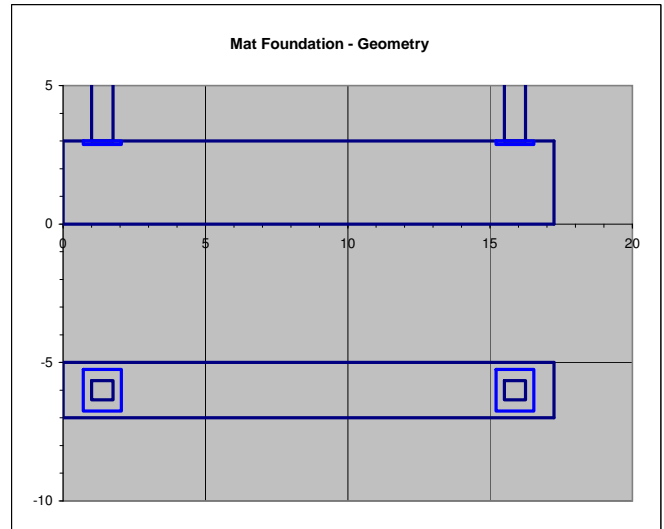
						Bar Area			
	Orientation	Bar Size	N Bars	Bottom Layer	d (inches)	Bar Spacing (inches)	Bar Diameter (inches)	Per Bar (in <sup>2</sup> )	Total (in <sup>2</sup> )
Top Mat	x	7	4	x	33.13	6.38	0.88	0.60	2.40
Bottom Mat	x	7	4	0	31.63	6.38	0.88	0.60	2.40

Soil Parameters :

Soil density = 120 pcf  
 $\sigma_{allow} = 2.00$  ksf (allowable bearing pressure)  
 $\sigma_p = 0.30$  ksf/ft (Passive Soil Pressure)  
 $\mu = 0.25$  ksf (Coefficient of Friction)

Design Parameters :

$\phi_v = 0.75$  (Shear; ACI 318-11 9.3.2.3)  
 $\Omega = 3.00$  (Overstrength Factor - SMRF)



**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1  
 DETERMINATION OF ADDITIONAL REINFORCEMENT REQUIRED - FIXED BASE COLUMN CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**2. Additional Required Reinforcement at Columns**

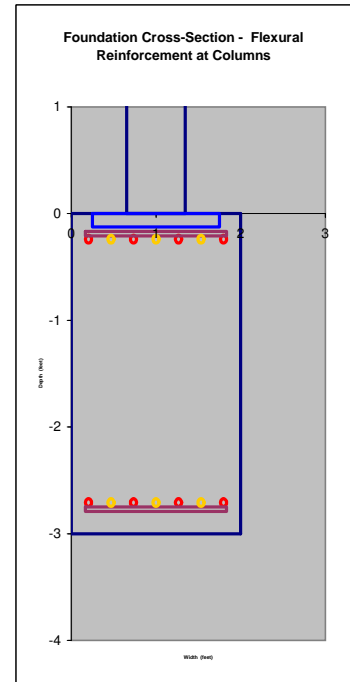
a) Column Probable Expected Flexural Capacity

$$M_{FB} = 100\% \text{ of Column Flexural Capacity}$$

$$= 1.0 Z_x F_y \quad \text{Where } Z_x = 70.1 \text{ in}^3 \text{ (Wide Flange - Plastic Section)}$$

$$F_y = 50 \text{ Ksi}$$

$M_{FB} = 3,505 \text{ Kip-in}$
$= 292.1 \text{ Kip-ft}$



b) Required Reinforcement Ratio (ACI 10.2)

$$\rho_r = \frac{0.85 f'_c}{f_y} \left[ 1 - \sqrt{1 - \frac{2 M_u}{0.765 b d^2 f'_c}} \right] \quad \text{Where } f'_c = 3.25 \text{ Ksi}$$

$$f_y = 60.00 \text{ Ksi}$$

$$M_u = M_F + M_{FB} \quad \text{for } M_F = 1,689 \text{ kip-in (Footing Flexural Demands)}$$

$$M_{FB} = 3,505 \text{ kip-in (Column Flexural Capacity)}$$

$$M_u = 5,194 \text{ kip-in}$$

$$b = L_y = 2.0 \text{ feet}$$

$$= 24 \text{ inches}$$

$$d_x = 31.63 \text{ inches}$$

$\rho_r = 0.00420$
--------------------

c) Reinforcement Ratio Provided

$$\rho_w = A_{sx} / (L_y d_x) \quad \text{Where } A_{sx} = A_F + A_{FB} \quad \text{Where } A_F = 2.40 \text{ in}^2 \text{ (Reinforcement Provided - Footing Flexure)}$$

$$A_{FB} = \text{Reinforcement Required for Resisting Fixed Base Column Flexural Capacity}$$

$$= (N-1) A_b \quad \text{for } N = 4 \text{ bars provided}$$

$$A_b = 0.60 \text{ in}^2 \quad \text{for } 7 \text{ bars}$$

Note:  $db = 0.88 \text{ in}^2 \text{ (Bar Diameter)}$

$$A_{FB} = 1.80 \text{ in}^2$$

$A_{sx} = 4.20 \text{ in}^2$
------------------------------

$$L_y = L_B = 2.0 \text{ feet}$$

$$= 24.0 \text{ inches}$$

$$d = 31.63 \text{ inches}$$

$\rho_w = 0.00553$	(reinforcement ratio provided)	Note:	D/C Ratio = 0.76	(Demand to Capacity Ratio - Flexure)
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OK

**Use Additional 3 - # 7 Bars for Column Flexure with DC Ratio = 0.76**

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1  
 DETERMINATION OF ADDITIONAL REINFORCEMENT REQUIRED - FIXED BASE COLUMN CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

d) Flexural reinforcement development length (ACI 12.2.2 and 12.2.5)

i) Development Length (ACI 12.2.2 - 12.2.4)

Bar Size = 7

$d_s = S - d_b$       Where  $S = 3.22$  inches (Bar spacing provided)  
 $d_b = 0.88$  inches

$d_s = 2.34$  inches (Clear spacing provided)

$d_c = 2.00$  inches (Clear Cover provided)

	Provided (inches)	Lower Limit	Upper Limit
Clear Cover	2.00	$d_b = 0.88$ inches OK	$2 d_b = 1.75$ inches OK
Clear Spacing	2.34	$2 d_b = 1.75$ inches OK	$4 d_b = 3.50$ inches NG
Equations		$l_d = \left( \frac{f_y \Psi_s \Psi_1 \Psi_e \lambda}{25 \sqrt{f'_c}} \right) d_b$	$l_d = \frac{3}{40} \left( \frac{f_y \Psi_s \Psi_1 \Psi_e \lambda}{2.5 \sqrt{f'_c}} \right) d_b$
Values		$l_d = 52.62 d_b$ $l_d = 46.0$ inches	$l_d = 31.57 d_b$ $l_d = 27.6$ inches

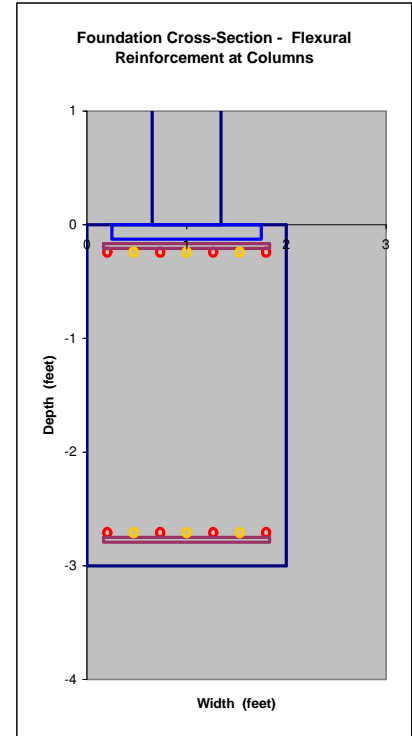
Note: Normal Weight Concrete with uncoated bars is assumed.

Where  $f_y = 60.00$  Ksi  
 $\Psi_s = 1.00$  (ACI 12.2.4)

$\Psi_1 = \Psi_e = \lambda = 1.00$

$f'_c = 3.25$  Ksi

$d_b = 0.88$  inches



ii) Excess Reinforcement (ACI 12.2.5)

$l'_d = l_d \rho_r / \rho_w$       Where  $l_d = 46.0$  inches  
 $\rho_r = 0.0042$  (required reinforcement ratio)  
 $\rho_w = 0.0055$  (reinforcement ratio provided)

$l'_d = 34.9$  inches (Required development length)

iii) Available Anchorage length

$L_{-da} = x_f - d_{cs} > l'_d$       Where  $x_f = 1.38$  feet (Cantilever Length at Column Centerline)  
 $= 16.50$  inches

$d_{cs} = 2.00$  inches (bar clearance - sides)

$L_{-da} = 14.50$  inches  
 NG

**Use Additional 3 - # 7 Bars for Column Flexure; Use 0 in Development Length beyond Ends of Base Plates - Bend Bars at Footing Ends and connect T and B bars together to form Cage.**

**SPREAD FOOTING DESIGN - SMRF 1 AT GRIDLINE I (N-S EQ LOADS) - CASE N-1  
 DETERMINATION OF ADDITIONAL REINFORCEMENT REQUIRED - FIXED BASE COLUMN CONDITION  
 785 CORBETT AVENUE, SAN FRANCISCO - SEISMIC RETROFIT**

**3. Foundation Demands at Fixed Base Columns**

a) Column Fixed Base Plastic Shear Demands

$$V_P = M_P / d \quad \text{Where } M_P = F_y Z_x \quad \text{for } F_y = 50 \text{ Ksi}$$

$$Z_x = 70.1 \text{ in}^3 \text{ (Wide Flange - Plastic Section)}$$

$$M_P = 3,505 \text{ Kip-in}$$

$$d = 31.63 \text{ inches (Effective depth of footing)}$$

$$V_P = 110.8 \text{ Kips}$$

b) Amplified Column Axial Demands - Overstrength Shear Demands on Foundation

$$P_U = \text{Max ( Abs ( } P_1 \text{), Abs ( } P_2 \text{) )} \quad \text{Where } P_1 = -10 \text{ Kips}$$

$$P_2 = 24 \text{ Kips}$$

$$P_U = 23.9 \text{ Kips}$$

$$V_O = \Omega P_U \quad \text{Where } \Omega = 3.00 \text{ (Overstrength Factor - SMRF)}$$

$$P_U = 23.9 \text{ Kips}$$

$$V_O = 71.6 \text{ Kips}$$

c) Controlling Shear Demands on Foundation

$$V_U = \text{Max ( } V_P \text{, } V_O \text{) } \quad \text{Where } V_P = 110.8 \text{ Kips (Column Plastic Shear)}$$

$$V_O = 71.6 \text{ Kips (Column Overstrength Demands)}$$

$$V_U = 110.8 \text{ Kips}$$

**4. Foundation Capacity at Fixed Base Columns**

a) Shear Strength provided by Concrete (ACI 11.3.1.1)

$$V_C = 2 f_c^{0.5} b_w d \quad \text{Where } f_c = 3.25 \text{ Ksi}$$

$$= 3,250 \text{ psi}$$

$$b = L_y = 2.0 \text{ feet}$$

$$= 24.0 \text{ inches}$$

$$d = 31.63 \text{ inches (Effective depth of footing)}$$

$$V_C = 65 \text{ kips}$$

b) Shear Strength provided by Shear Reinforcement (ACI 11.3.1.1)

Note: Assume transverse flexural reinforcement provided for footing is part of a reinforcement cage.

$$V_S = A_s F_y d / S \quad (11-15) \quad A_s = 0.40 \text{ for No. 4 bars } \Rightarrow \text{hoops (from Footing Design)}$$

$$\leq 4 V_C \quad F_y = 50 \text{ Ksi}$$

$$d = 31.63 \text{ inches (Effective depth of footing)}$$

$$S = 3.16 \text{ inches (bar spacing - from Footing Design)}$$

$$V_S = 199.9 \text{ kips}$$

b) Factored Shear Capacity of Footing (ACI 11.1)

$$\phi V_n = \phi ( V_C + V_S ) \quad \text{Where } \phi = 0.75 \text{ (Shear; ACI 318-11 9.3.2.3)}$$

$$V_C = 65 \text{ kips}$$

$$V_S = 199.9 \text{ kips}$$

$$\phi V_n = 198.6 \text{ Kips}$$

Note:  $V_U = 110.8 \text{ Kips}$

OK

**Footing OK for Shear ; Use # 4 hoops @ 3.0" to reinforce Footings at Column locations.**